


# **STATICS DECONVOLUTION VS INTERFEROMETRY**



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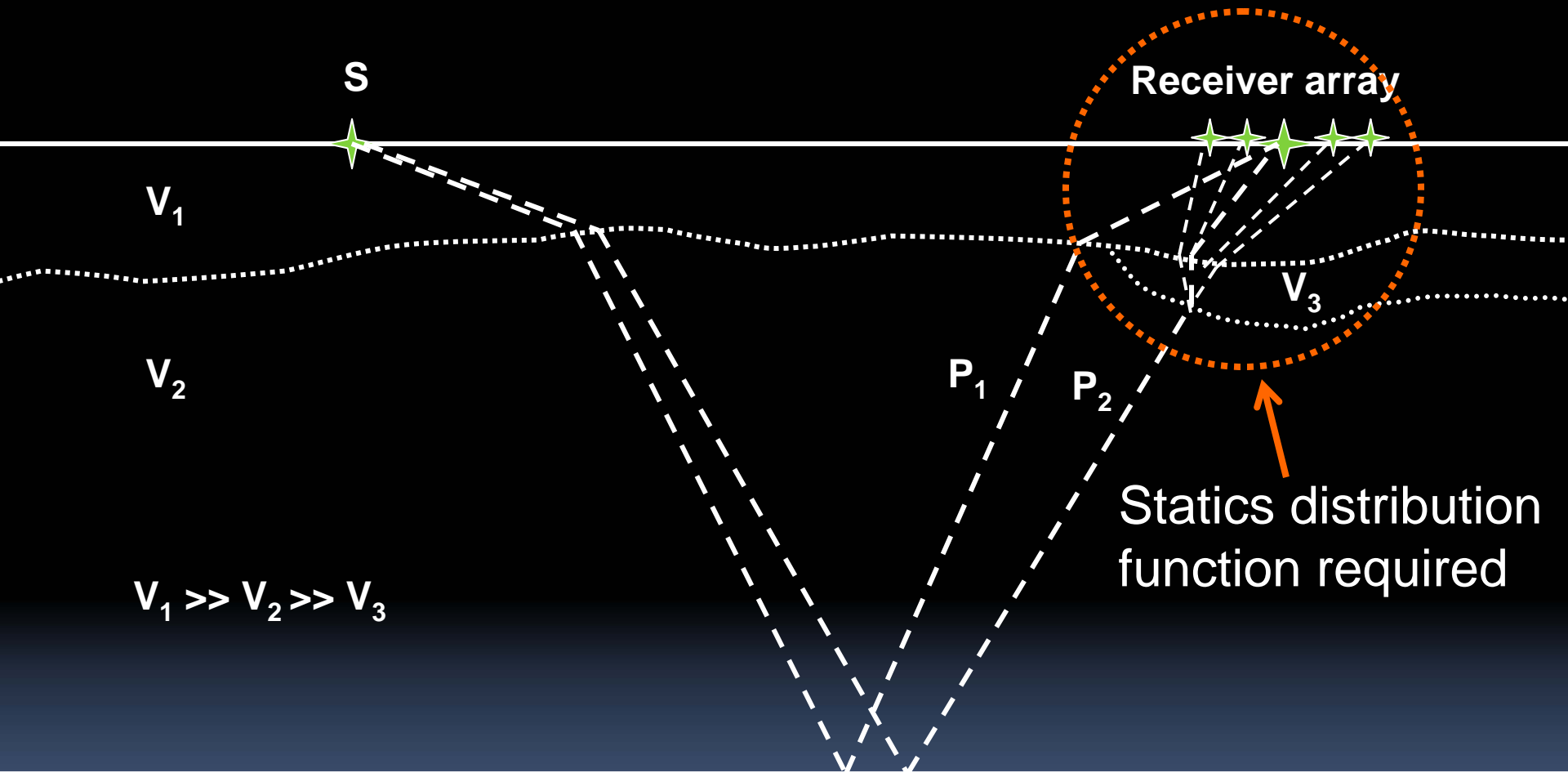
# Outline

- Motivation—**similarity** between techniques **gives insight** for further development
  - Statics deconvolution—the basics
  - Seismic interferometry—the basics
  - Comparing the techniques on field data
  - Conclusions and conjectures
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# Statics deconvolution

- Simple **time shift** model replaced by more general '**statics distribution function**' model
- Statics distribution functions for seismic traces estimated from **cross-correlations** of raw traces with 'pilot traces'
- **Match filter** or inverse filter derived for each statics distribution function
- Application of **unique** filter corrects each trace

# Conventional statics assumptions *violations*



Raypath segments beneath surface points not vertical; Sources and receivers can be **arrays**, with **different statics** for each point in the array. **Multiple raypaths** possible between source and receiver location ( $P_1$  and  $P_2$ ), due to buried velocity anomalies ( $V_3$ )

**Ideal seismic trace**

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**Actual statics distribution function**

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**Input seismic trace**

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**Estimated statics distribution function**

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**Desired statics distribution function**

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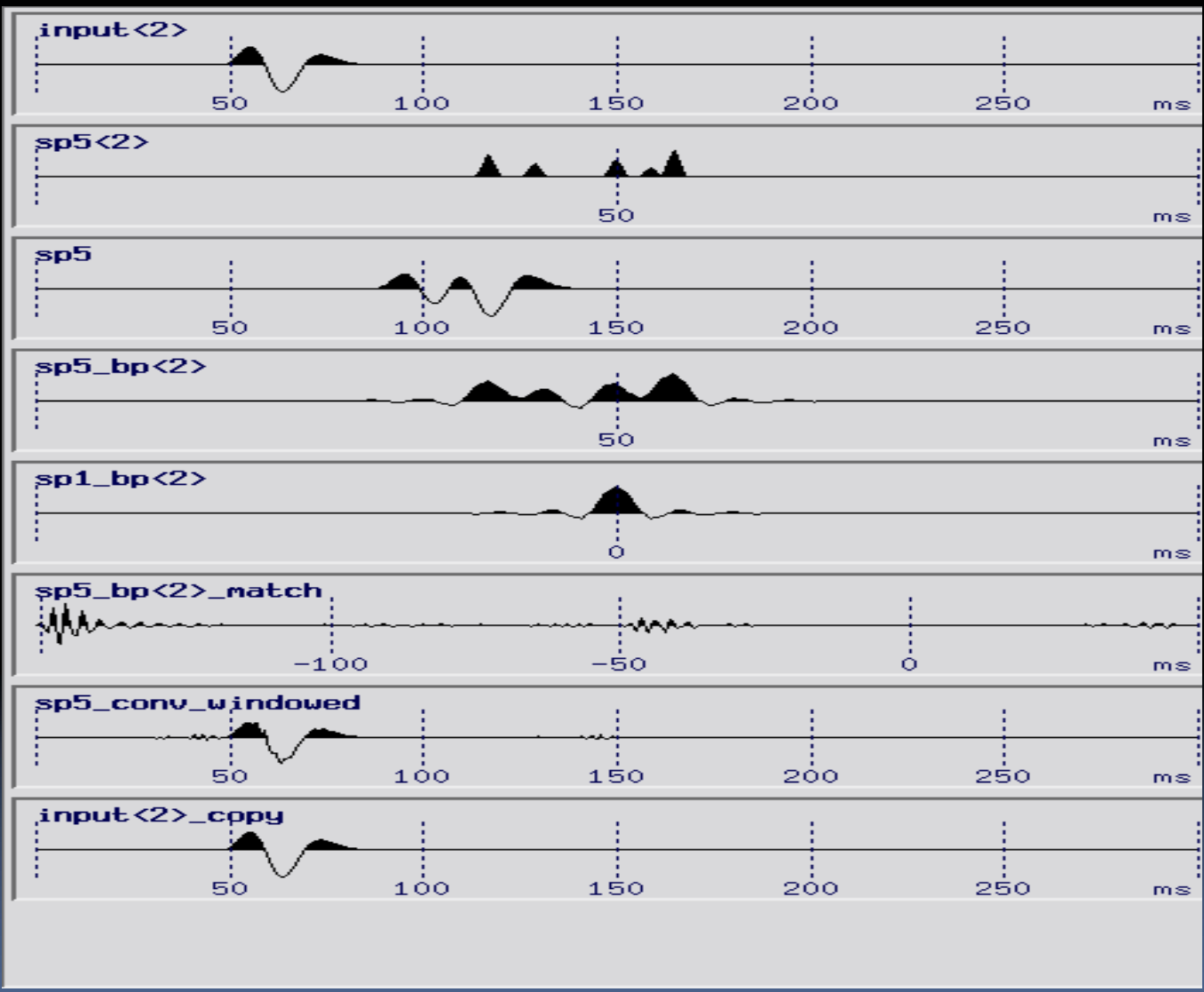
**Match filter**

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**Match filtered seismic trace**

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**Ideal seismic trace**



The static deconvolution principle

# Statics deconvolution

$$T_{k\beta}(t) = w(t) * s_k(t) * R_{k\beta}(t) * r_\beta(t)$$

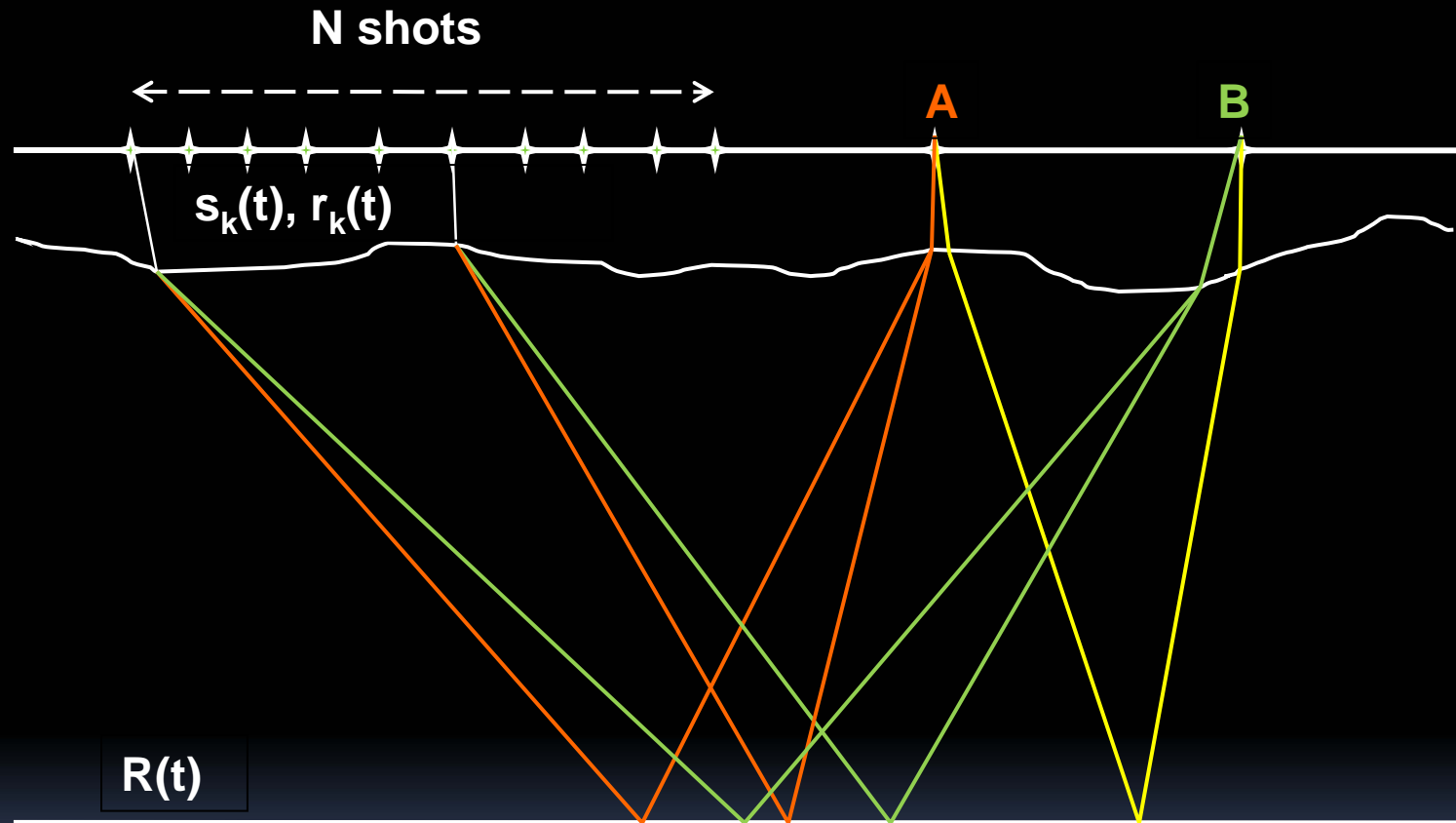
Raw seismic trace

$$\hat{T}_{\alpha\beta}(t) = T_{\alpha\beta}(-t) * T_{\alpha\beta}(t) * \sum_{k=1}^N T_{k\beta}(t) .$$

Corrected seismic trace

# Seismic interferometry

- The principles of **reciprocity** and **time reversal** are used to create '**virtual traces**' from recorded traces
- Time-reversed portion of a raw trace is used as a **filter** to remove surface-related effects
- **Sum of filtered traces** over an aperture creates a new trace with a '**virtual**' source and **no surface-related effects**



Raw trace pairs from receiver gathers at **A** and **B** (common source  $k$ ) **cross-correlated** to cancel source phase  $s_k(t)$ . Cross-correlations **convolved (as match filters)** with traces of receiver gather **A** to cancel receiver phase  $r_A(t)$ , then **summed** over shot aperture  $N$  to approximately cancel residual source phase  $s_k(t)$ . This is a 'virtual trace', between **A** and **B** for a virtual source (receiver) gather.



# Seismic interferometry

$$\mathbf{T}_{k\beta}(t) = w(t) * s_k(t) * R_{k\beta}(t) * r_\beta(t)$$

Raw seismic trace

$$\hat{\mathbf{T}}_{\alpha\beta}(t) = \sum_{k=1}^N [\mathbf{T}_{k\alpha}(-t) * \mathbf{T}_{k\alpha}(t)] * \mathbf{T}_{k\beta}(t)$$

Virtual seismic trace

# How they're related

$$\hat{\mathbf{T}}_{\alpha\beta}(t) = \mathbf{T}_{\alpha\beta}(-t) * \mathbf{T}_{\alpha\beta}(t) * \sum_{k=1}^N \mathbf{T}_{k\beta}(t).$$

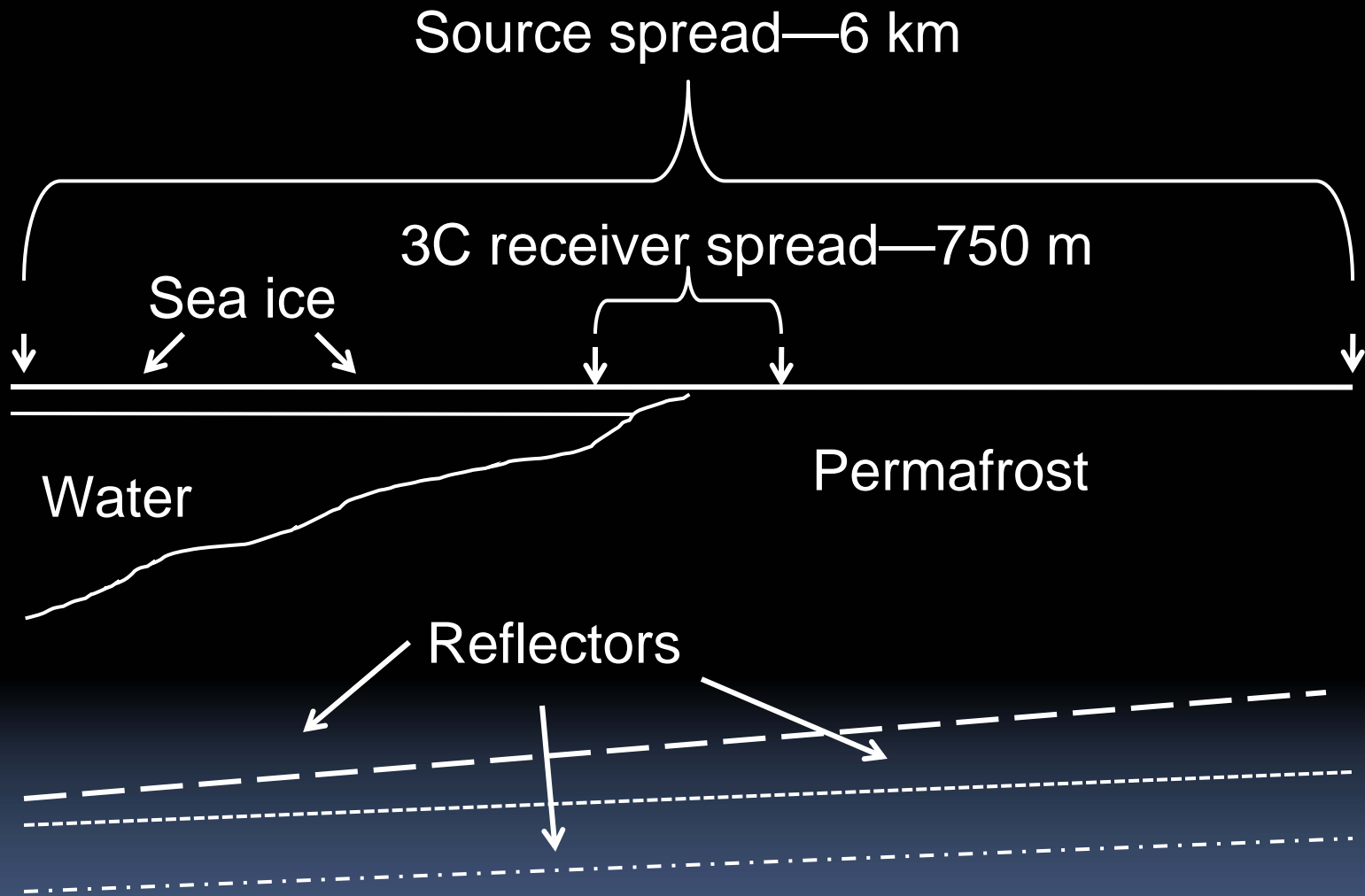
Statics deconvolution

$$\hat{\mathbf{T}}_{\alpha\beta}(t) = \sum_{k=1}^N \left[ \mathbf{T}_{k\alpha}(-t) * \mathbf{T}_{k\alpha}(t) \right] * \mathbf{T}_{k\beta}(t)$$

Seismic interferometry

# Hansen Harbour field example

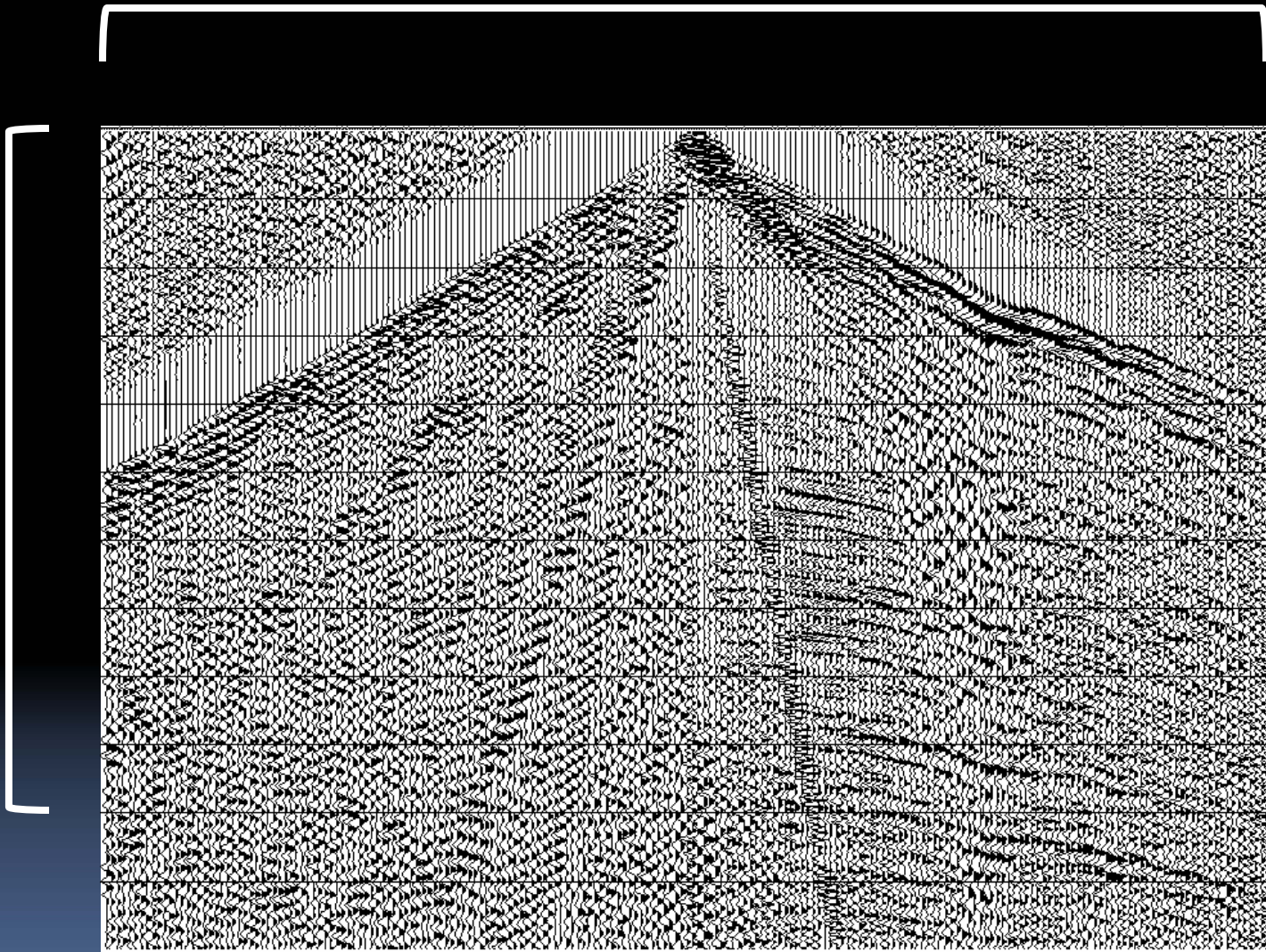
- Receiver spread only **50 stations (15m interval)**, no appreciable surface functions
- Source spread **200 stations (30m interval)**, visible variations in coupling, statics
- Raw receiver gathers show source statics and coupling variations, as well as coherent noise



Hansen Harbour 3C seismic line geometry

750 m

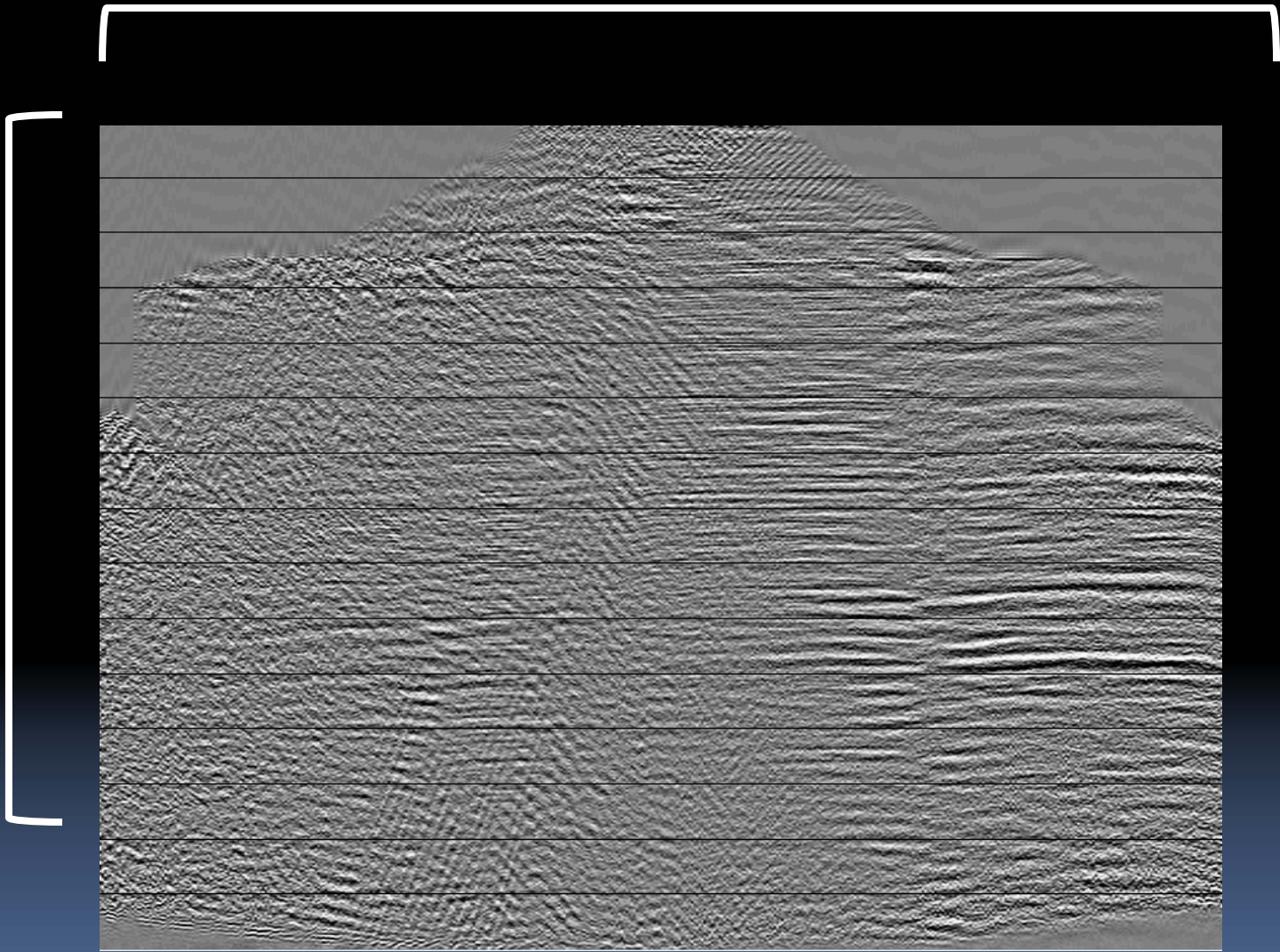
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Hansen Harbour receiver gather, bandpass, AGC

750 m

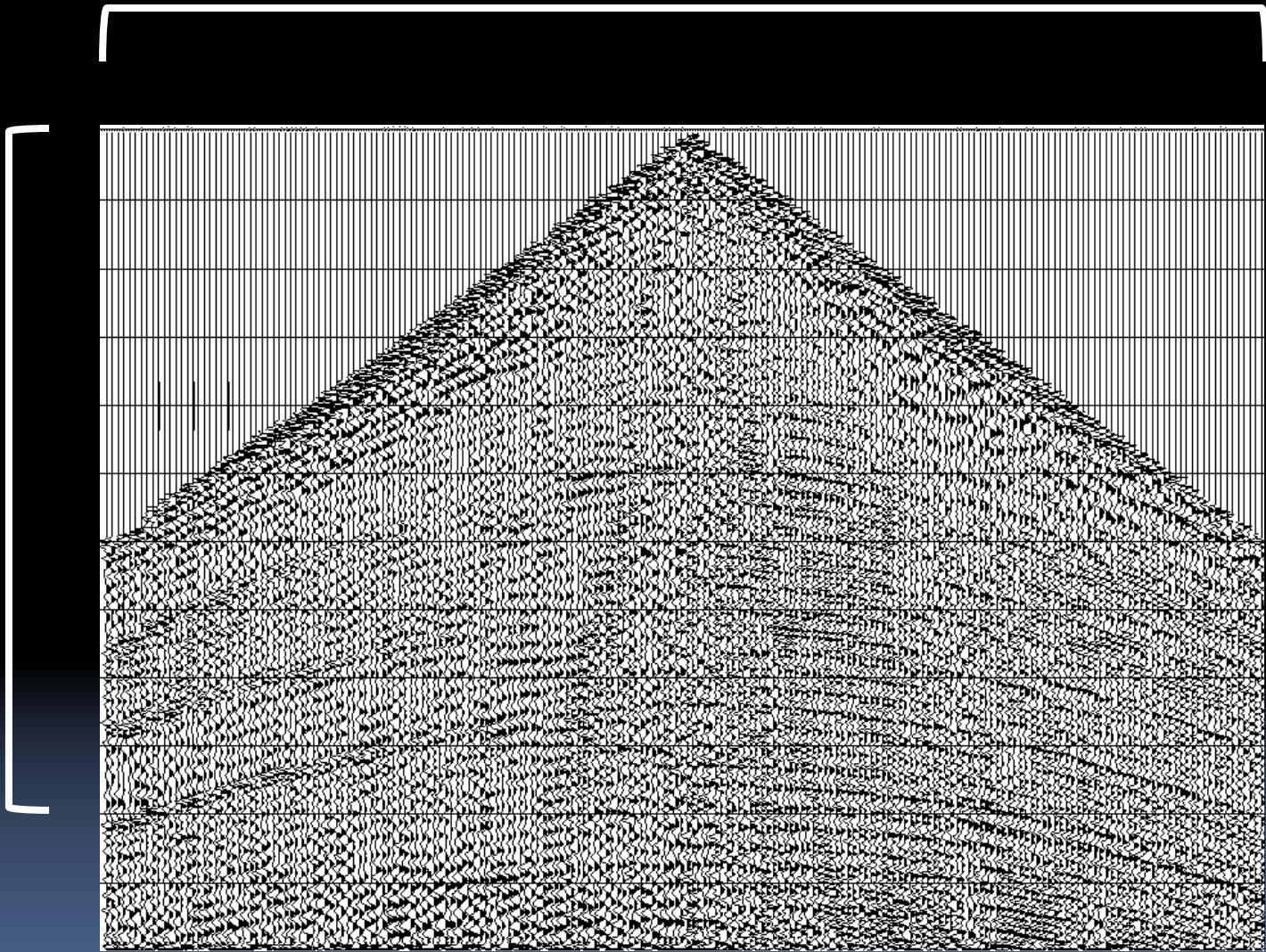
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Hansen Harbour stack—no filtering, no statics

750 m

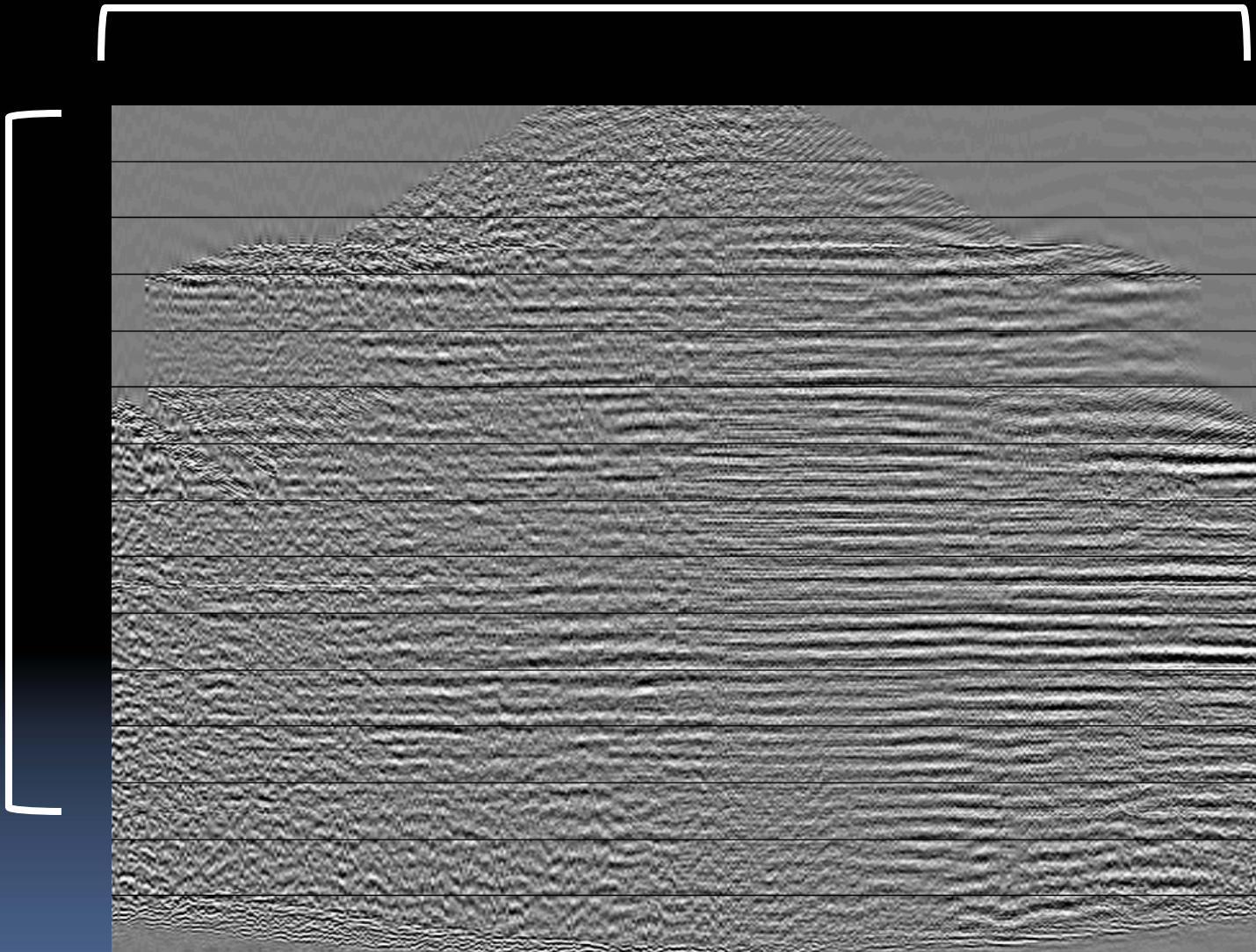
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Hansen Harbour receiver gather after **coherent noise attenuation** and **statics deconvolution**

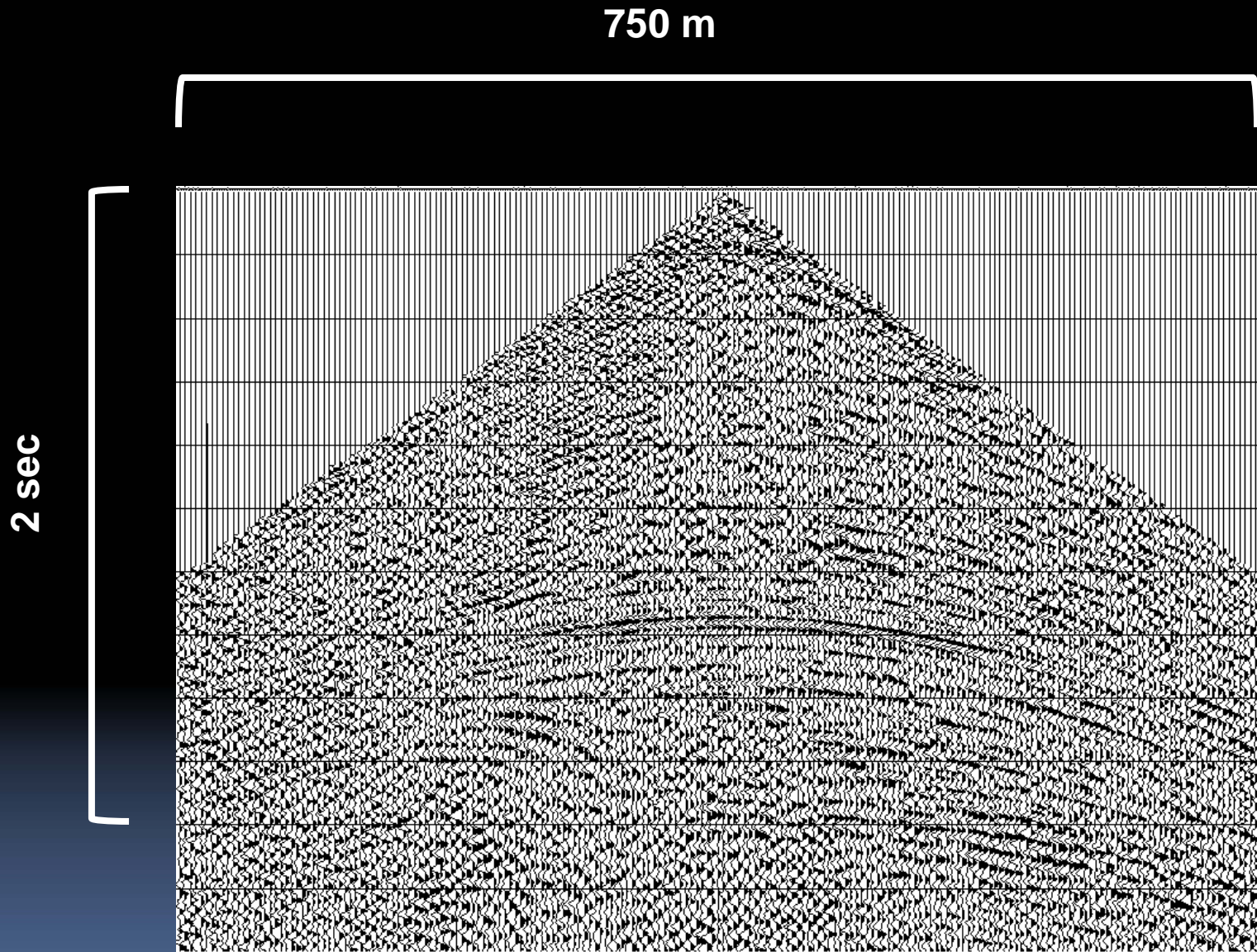
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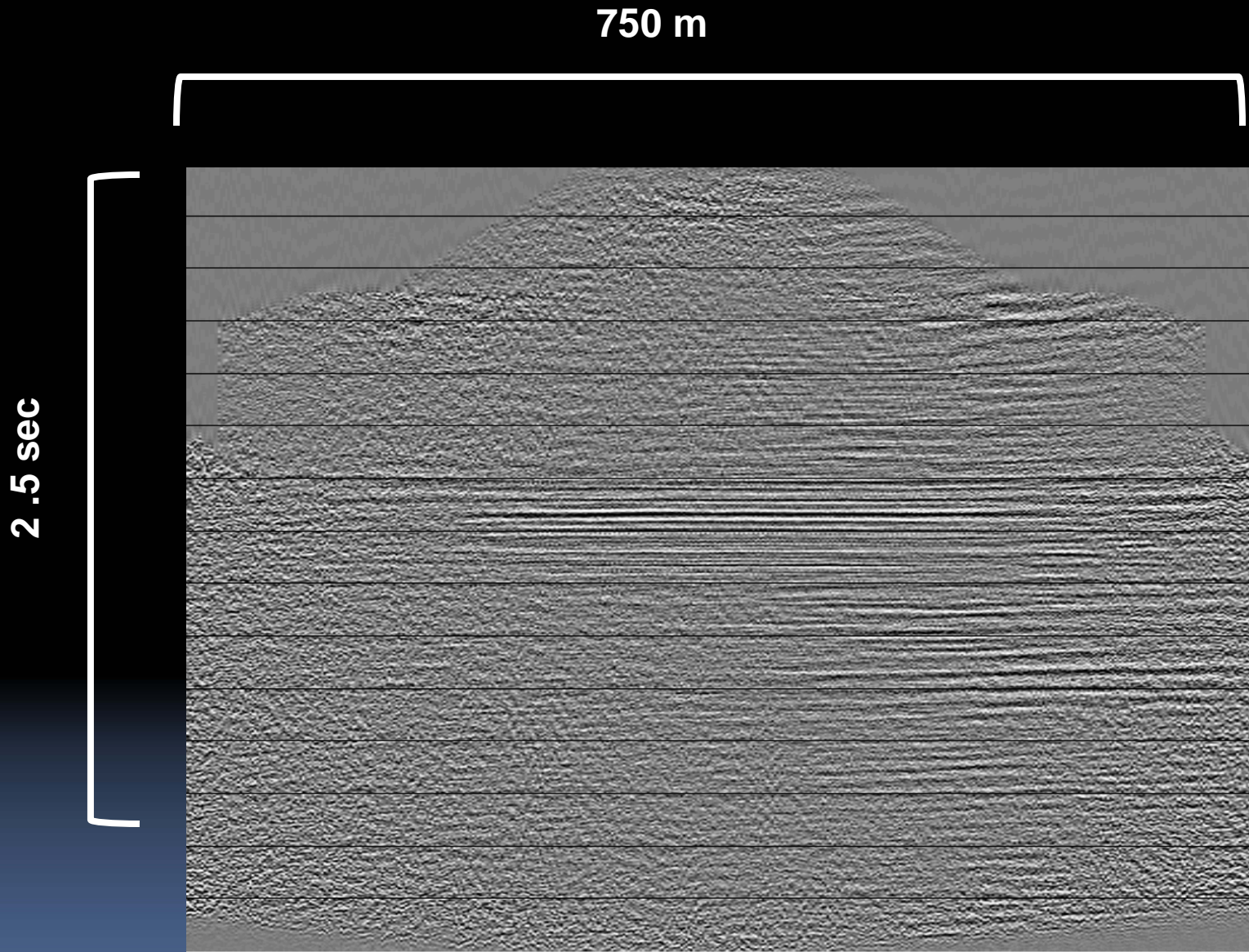


Hansen Harbour stack—**coherent noise attenuated,**  
**statics deconvolved**





Hansen Harbour **virtual receiver gather** from raw traces, **no noise attenuation**



Hansen Harbour stack—**virtual receiver gathers,**  
**no noise attenuation**

# Conclusions and conjectures

- **Statics deconvolution** and **interferometry** obviously *similar* in their effects
- **Cross-correlation** or **match-filtering** is the key to removing phase effects of surface functions
- *Coherent noise attenuation an unexpected benefit of interferometry*
- Further exploration of interferometry for correcting surface effects is warranted



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