



# Sensitivity of interval $V_p/V_s$ analysis of seismic data

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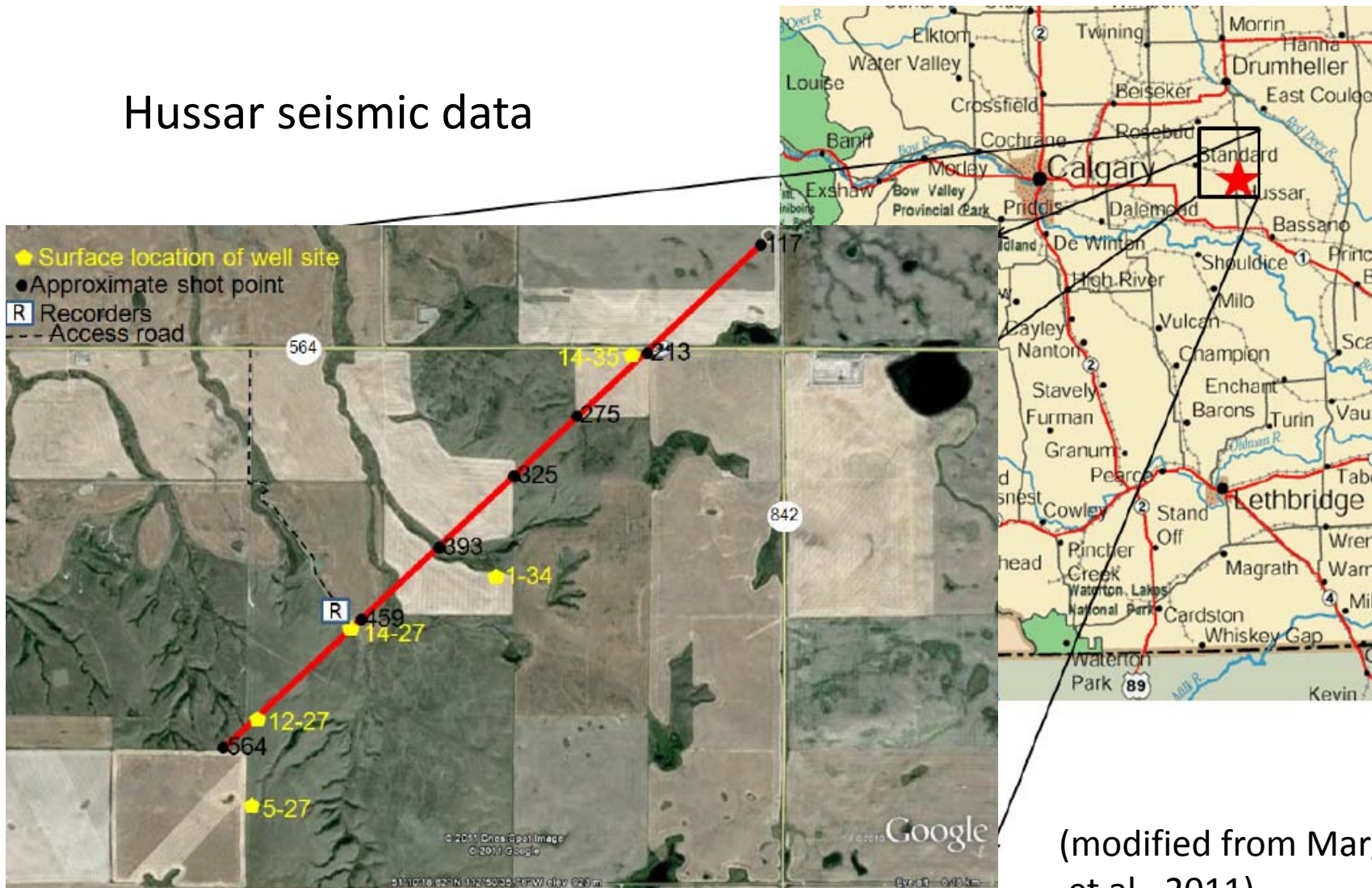
- Objective
- Introduction
  - Area of Study
  - Input Data
- Data Interpretation
  - Horizon Interpretation
  - Vp/Vs Analysis
- Sensitivity analysis
  - Synthetic model
- Conclusions
- Acknowledgements

# Objectives

- Perform a Vp/Vs analysis of the Hussar data.
- Suggest a minimum interval time for robust Vp/Vs analysis.
- Provide recommendations on horizons interpretation in order to reduce uncertainty in interval Vp/Vs
- Understand the sensitivity of Vp/Vs to interval time.

# Area of Study

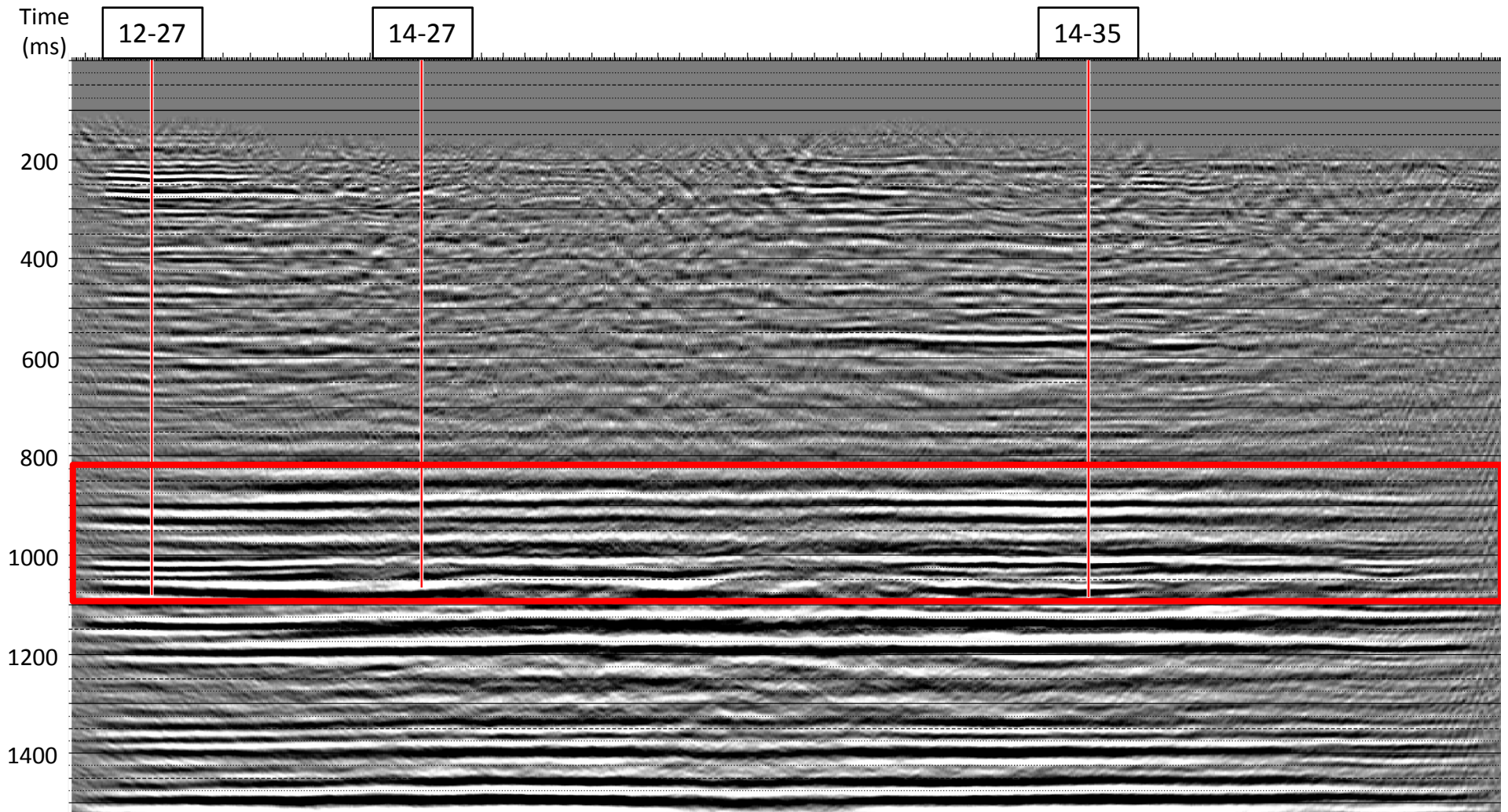
## Hussar seismic data



(modified from Margrave  
et al., 2011)

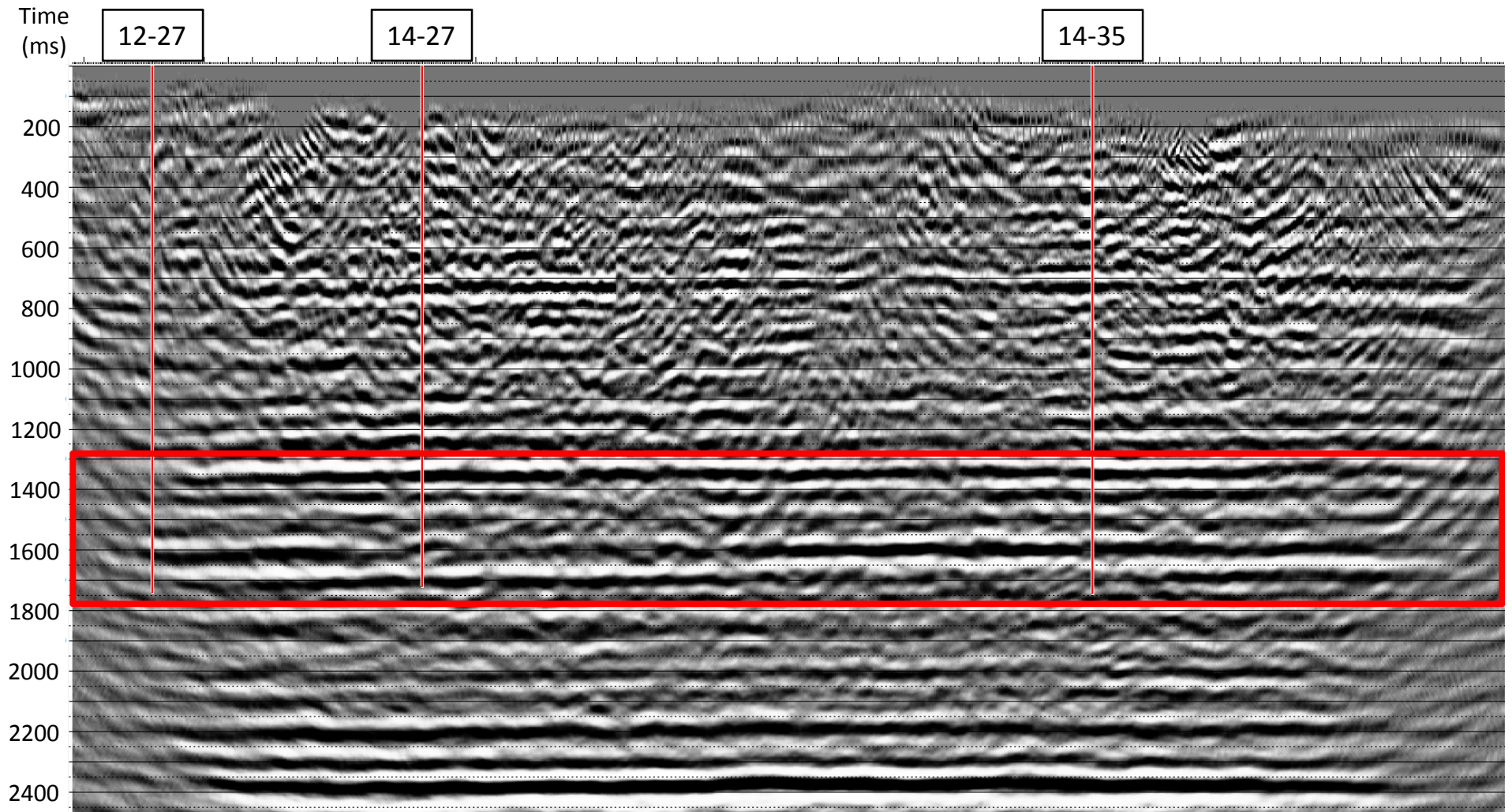
# Input Data

## PP Volume



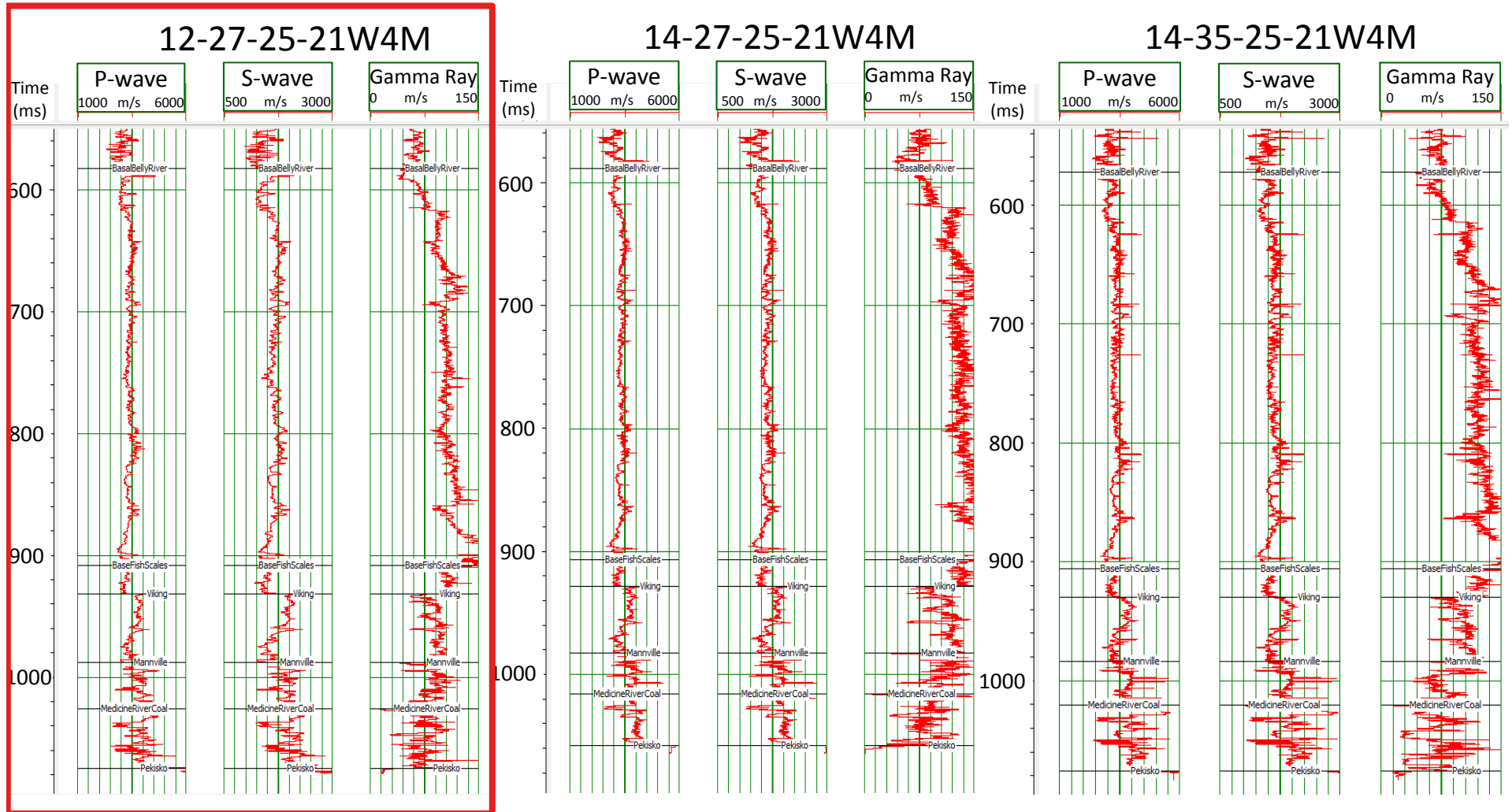
# Input Data

## PS Volume



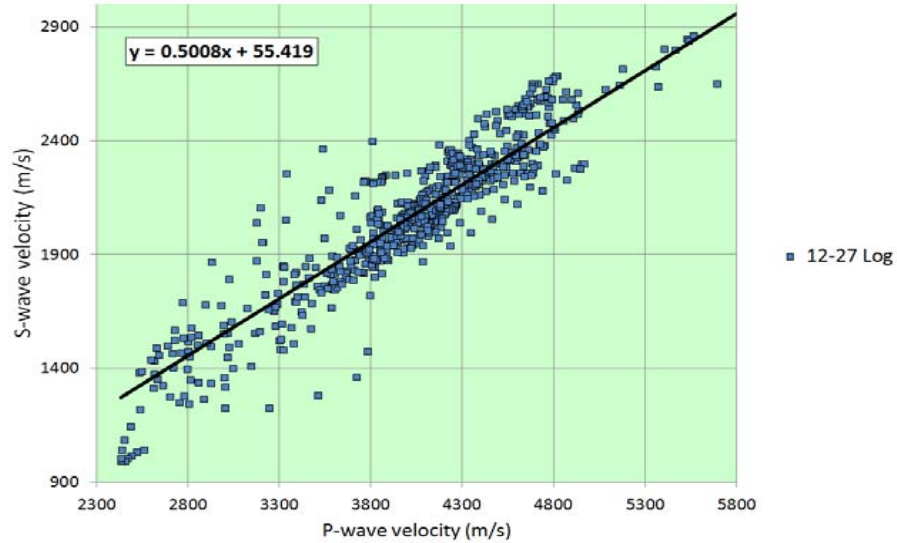
# Input Data

## Wells (Husky Energy)

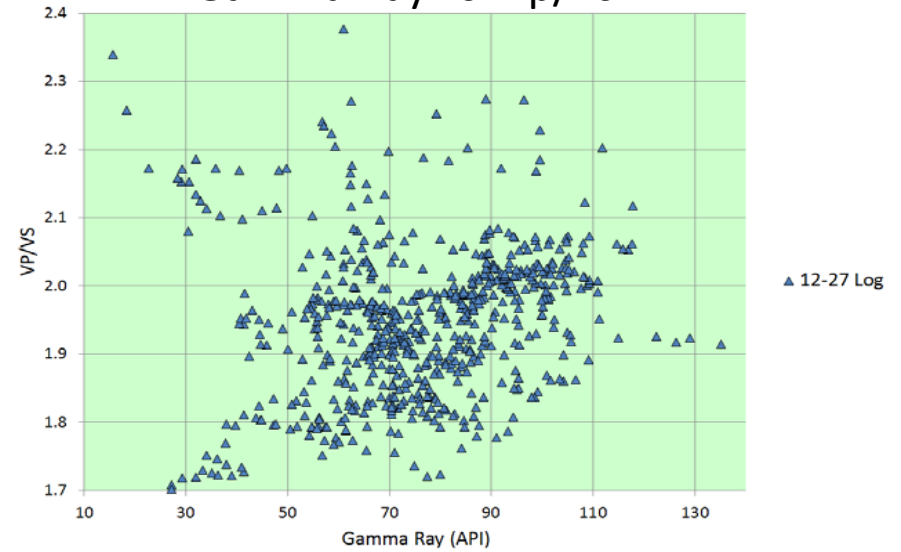


# Input Data well 12-27

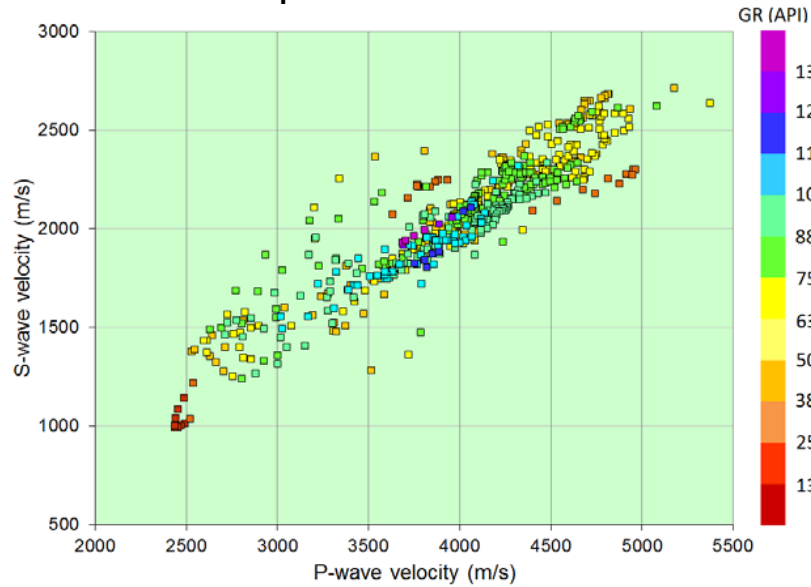
Vp vs. Vs



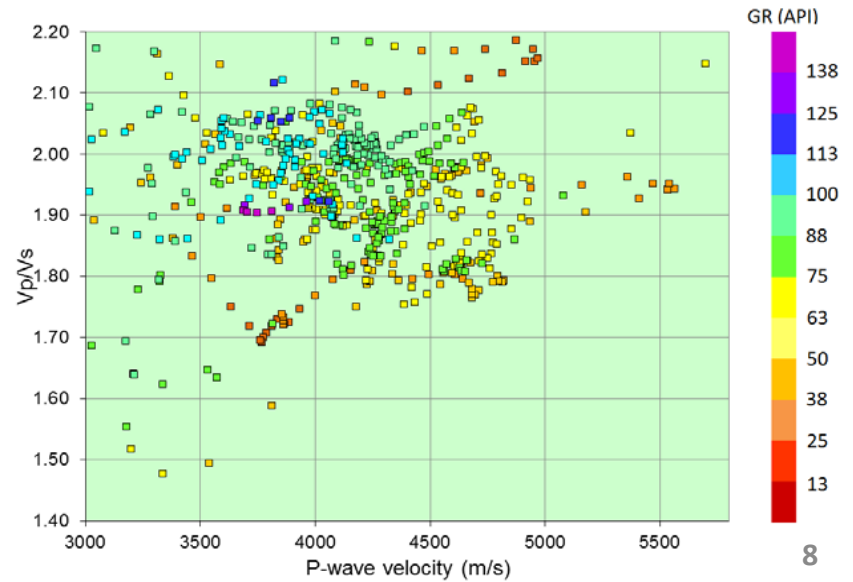
Gamma Ray vs. Vp/Vs



Vp vs. Vs and G.R.



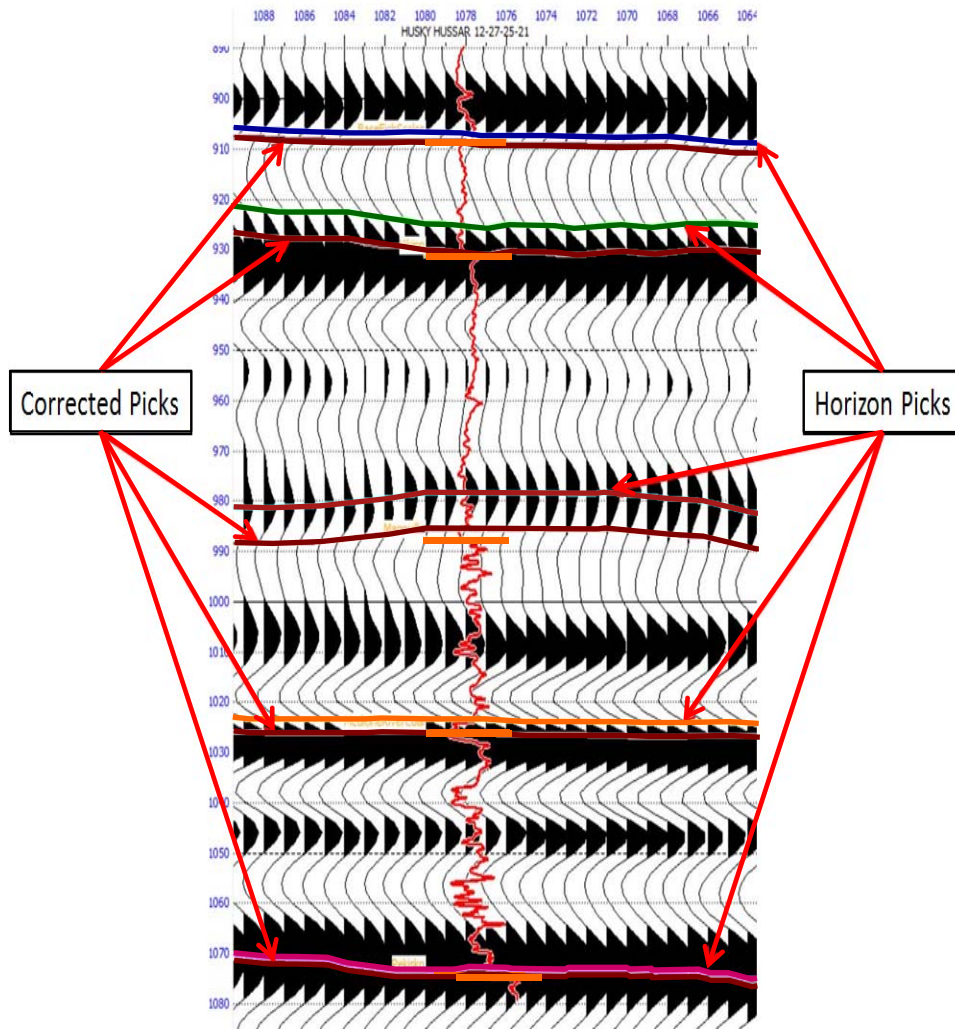
Vp/Vs vs. Vp and G.R.



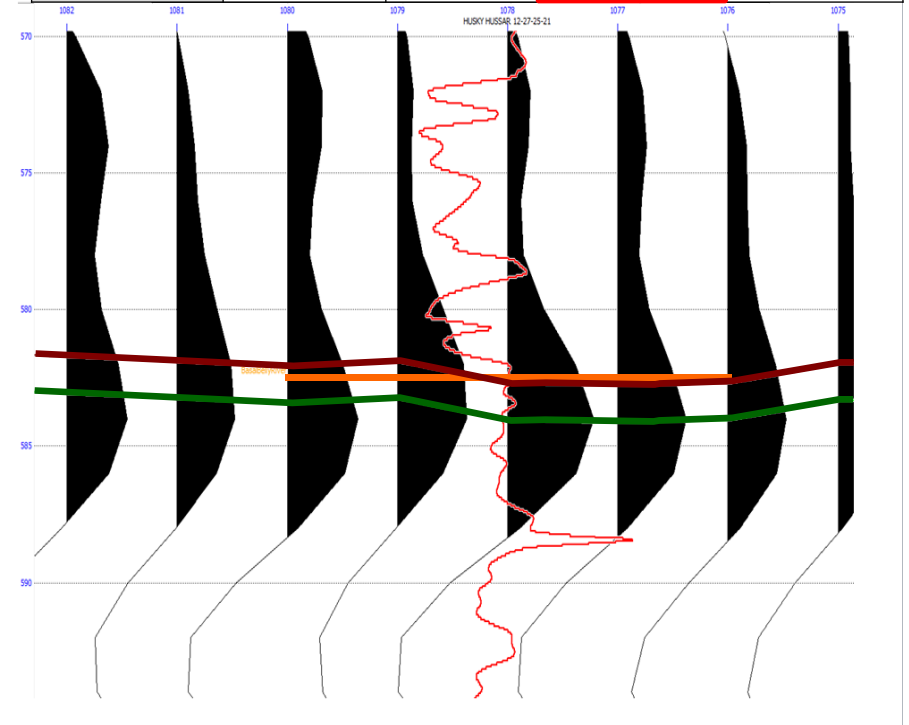


# Hussar Data

## Horizon Interpretation



	12-27 Log			All Logs
	Horizon Time	Top Time	Time Diff.	Average Corr.
BasalBellyRiver	584.02	582.51	-1.51	-1.35
BasalBellyRiver Corr.	582.67	582.51	-.16	--

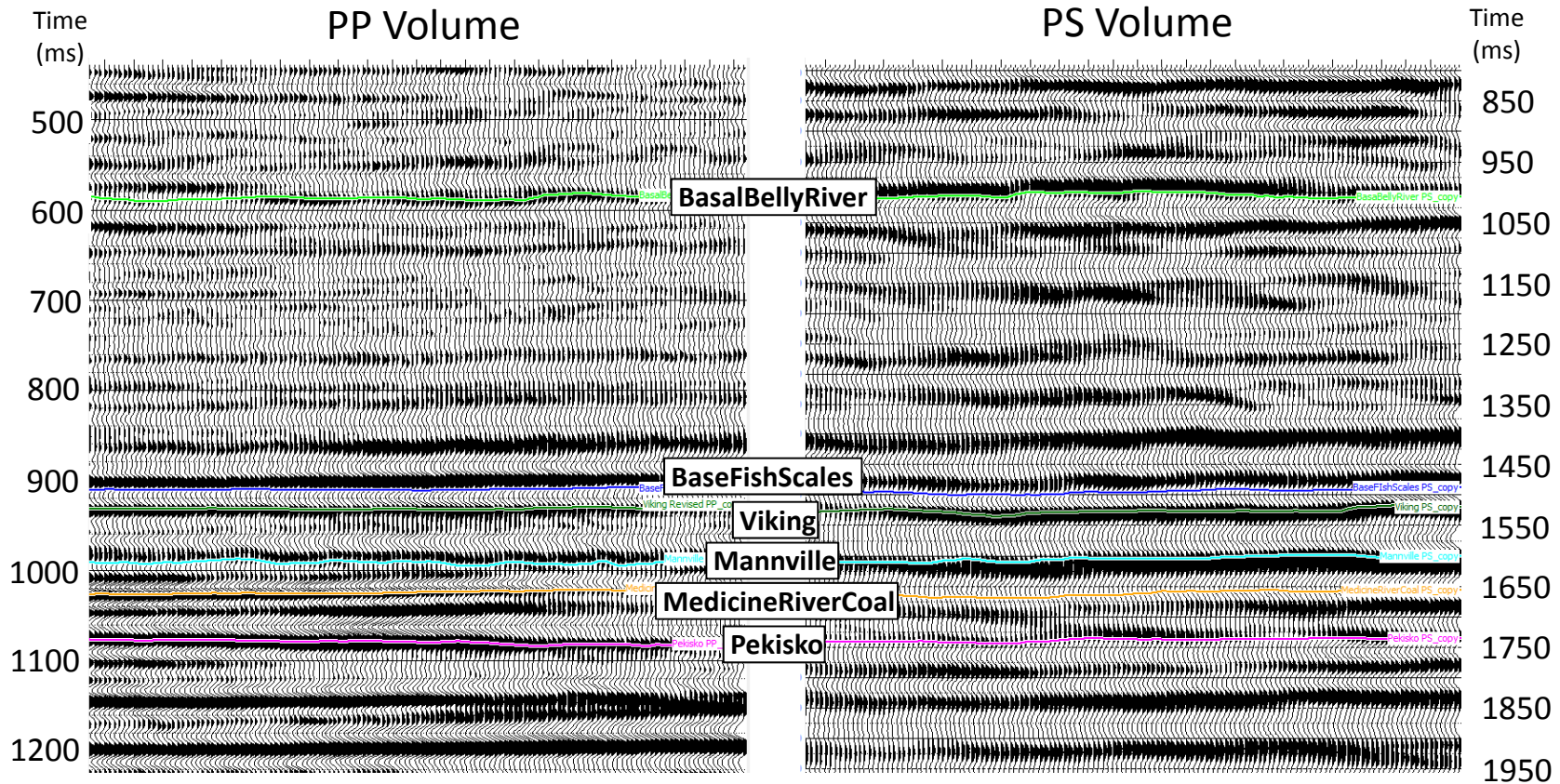


# Hussar Data

## Horizon Interpretation

Vp/Vs values were calculated using the following relationship (Garotta, 1987)

$$Vp/Vs = \frac{(2\Delta Tps - \Delta Tpp)}{\Delta Tpp}$$

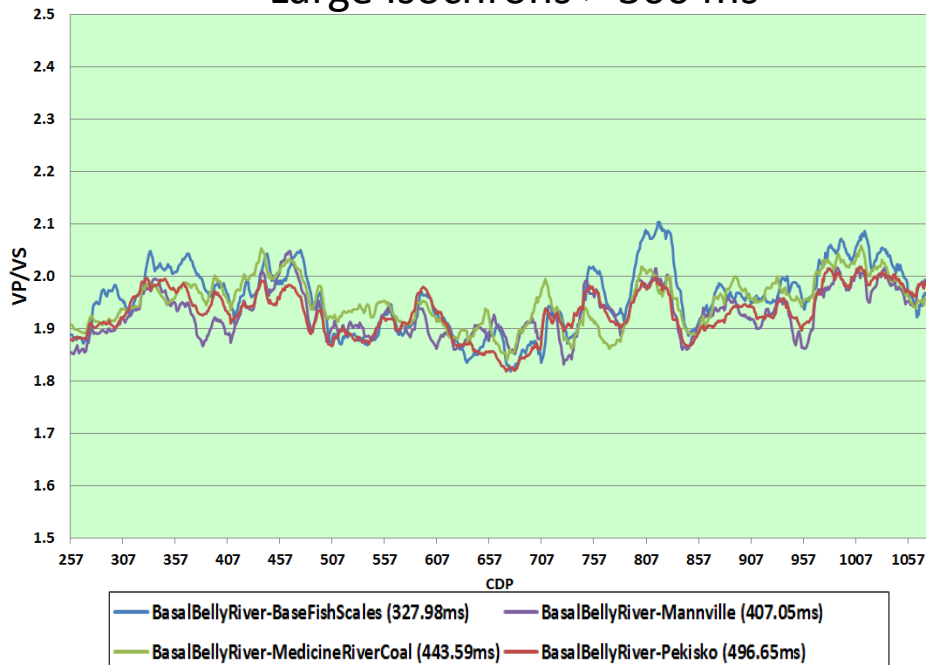


# Hussar Data

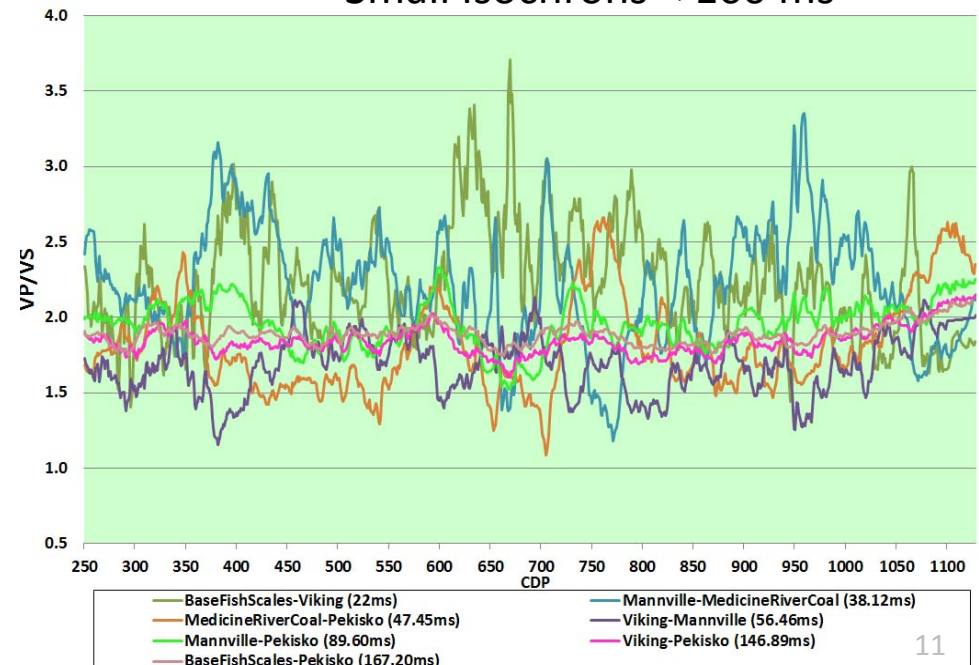
	PP Time Interval $\Delta T$ (ms)
	Average
BasalBellyRiver-BaseFishScales	327.98
BaseFishScales-Viking	22.55
Viking-Manville	56.46
Mannville-MedicineRiverCoal	38.12
MedicineRiverCoal-Pekisko	47.45
BasalBellyRiver-Pekisko	496.65
BasalBellyRiver-MedicineRiverCoal	443.59
BasalBellyRiver-Mannville	407.05
BaseFishScales-Pekisko	167.20
Mannville-Pekisko	89.60
Viking- Pekisko	146.89

- Total of 6 Horizons Interpreted.
- 11 Isochrons range from approximately 22 ms to 500 ms.

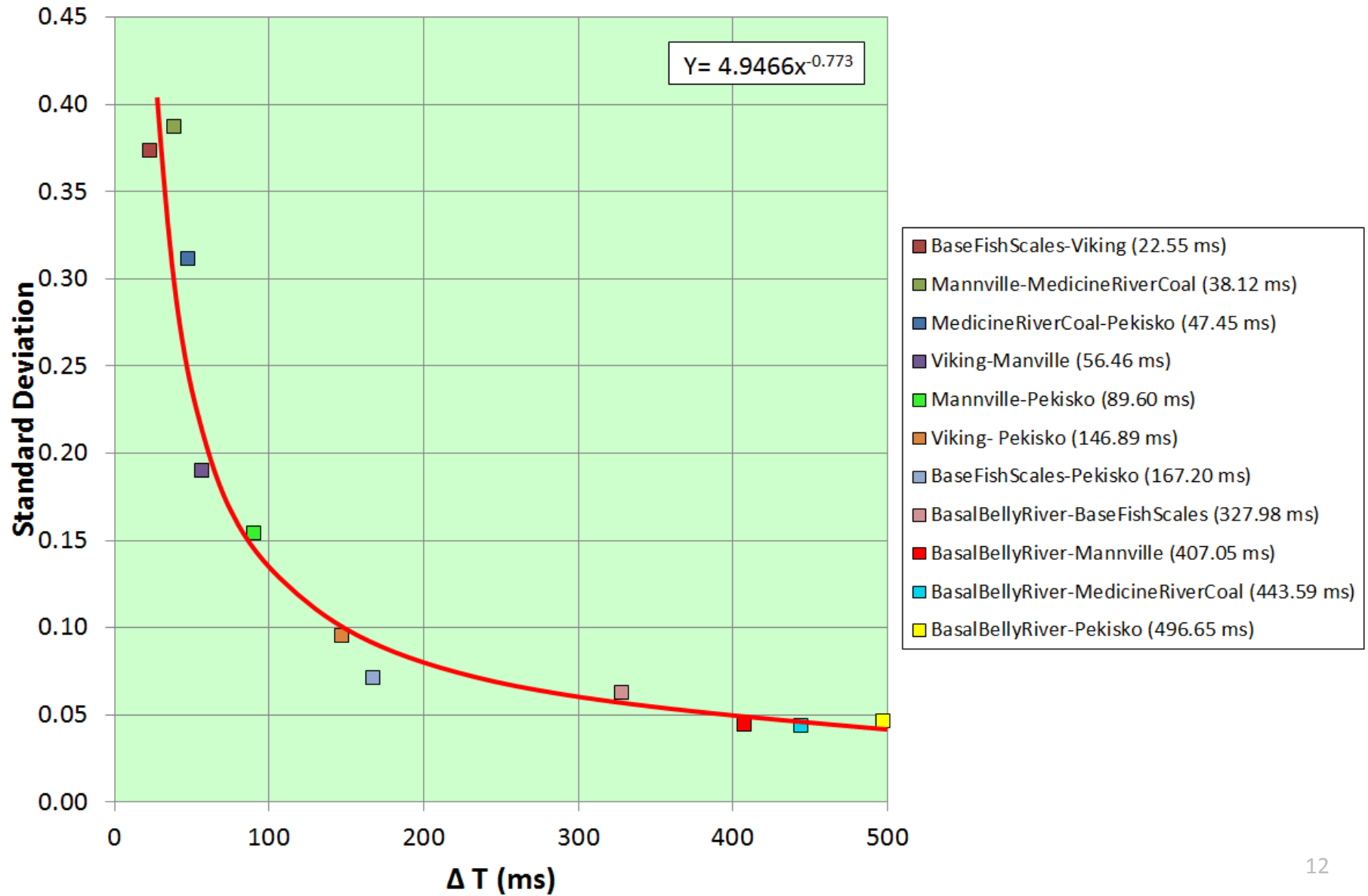
Large Isochrons > 300 ms



Small Isochrons < 160 ms



# Sensitivity Analysis



# Sensitivity Analysis

First step:

Examine the equation

$$(y) \rightarrow \frac{V_p}{V_s} = \frac{(2\Delta T_{ps} - \Delta T_{pp})}{\Delta T_{pp}} = \frac{2\Delta T_{ps}}{\Delta T_{pp}} - 1$$

(x) points to  $2\Delta T_{ps}$   
(z) points to  $\Delta T_{pp}$

Assumptions:  $\pm 2$ ms uncertainty in the horizons interpretation

# Sensitivity Analysis

First step:

Examine the equation

$$(y) \rightarrow \frac{V_p}{V_s} = \frac{(2\Delta T_{ps} - \Delta T_{pp})}{\Delta T_{pp}} = \frac{2\Delta T_{ps}}{\Delta T_{pp}} - 1$$

(x)

(z)

Assumptions:  $\pm 2\text{ms}$  uncertainty in the horizons interpretation

Second step:

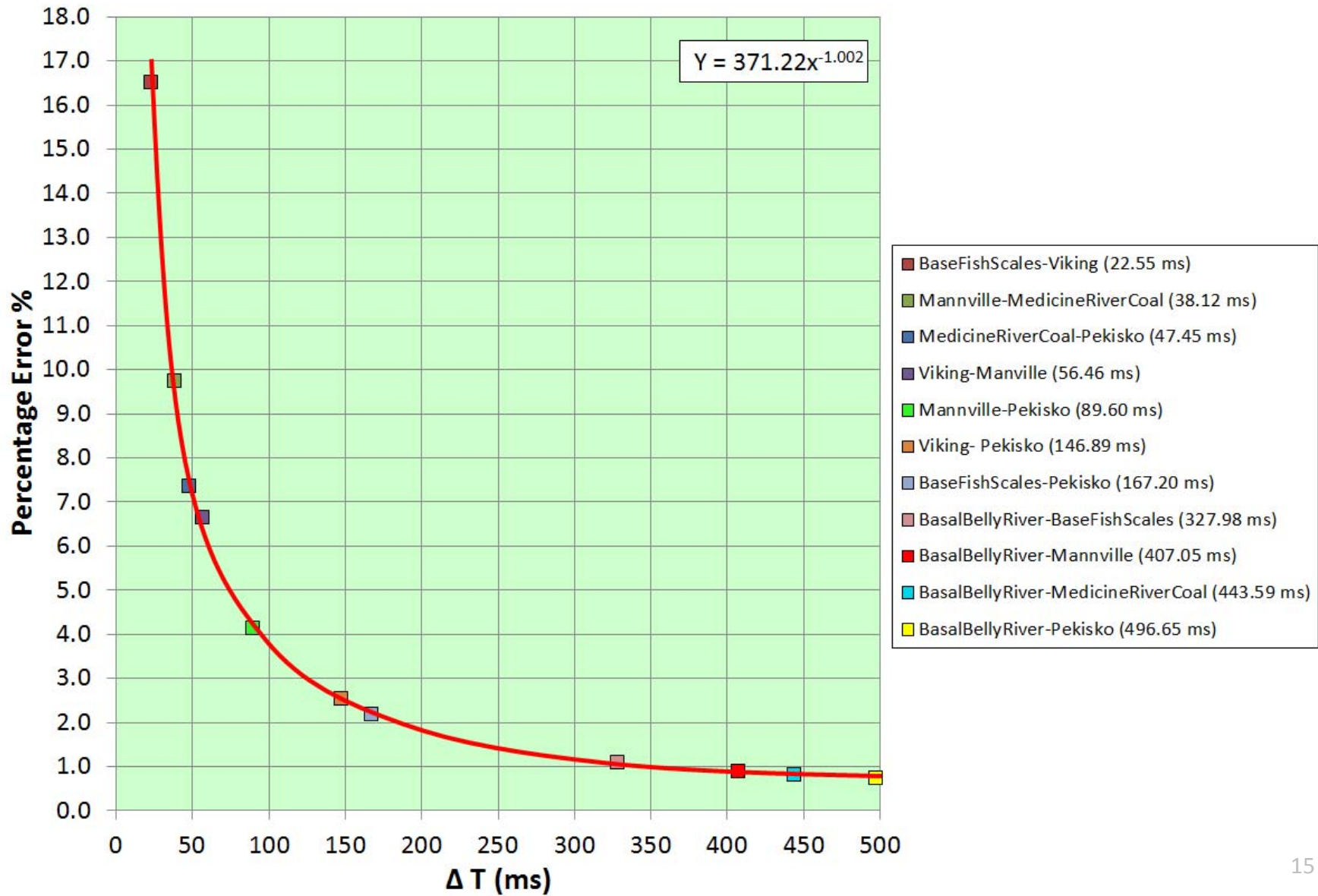
Evaluate the propagation of error equation

$$u(y) = \sqrt{c_1^2 u(x_1)^2 + c_2^2 u(x_2)^2 + \dots + c_n^2 u(x_n)^2} \quad (\text{Louro, 2014})$$

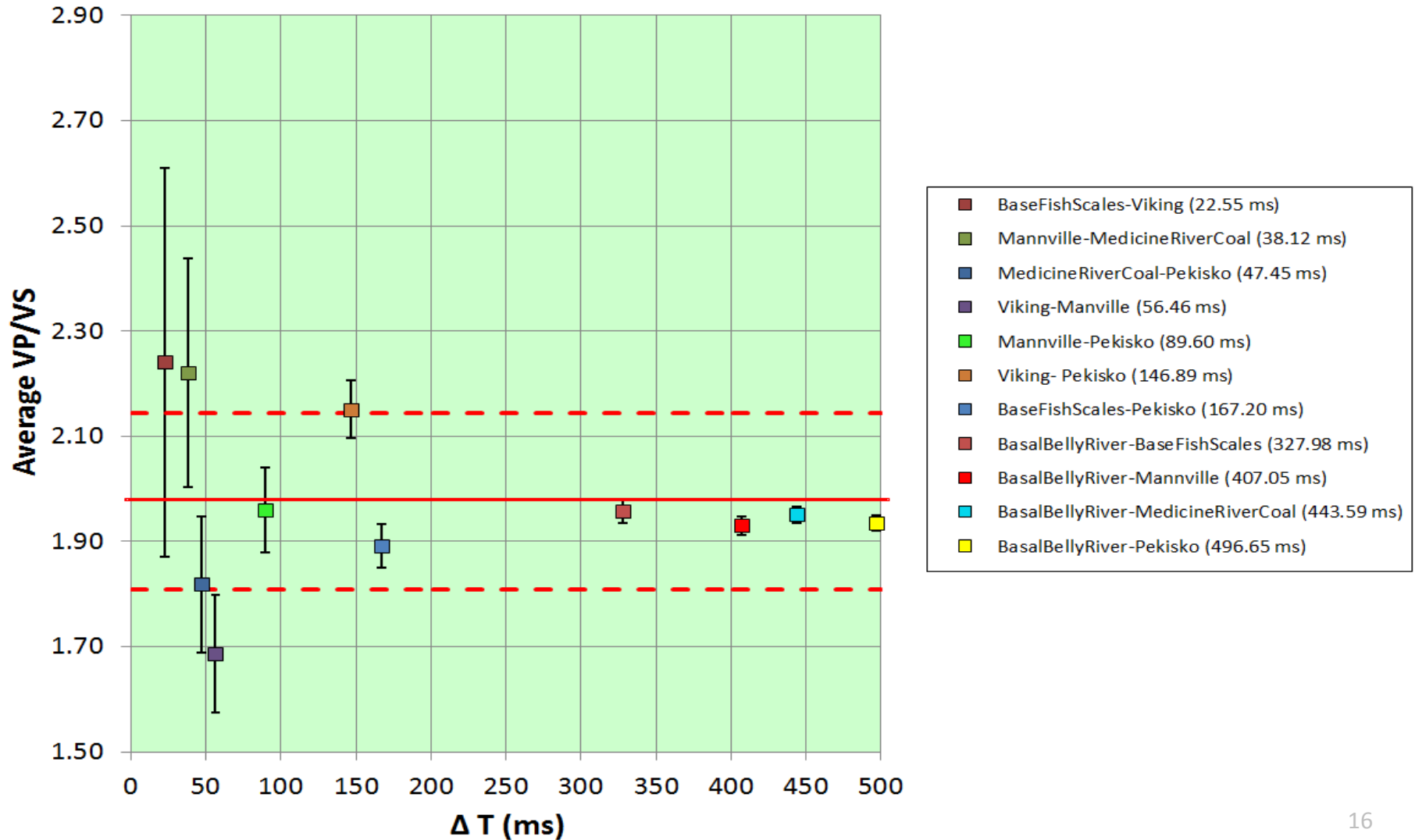
Sensitivity Coefficient  $\rightarrow c_i = \frac{\partial y}{\partial x_i}$

$$v_p/v_s (\text{error}) = \sqrt{\frac{4}{z^2} u(x)^2 + \frac{4x^2}{z^4} u(z)^2}; \quad = 4 \sqrt{\frac{1}{\Delta T_{pp}^2} + \frac{\Delta T_{ps}^2}{\Delta T_{pp}^4}}$$

# Sensitivity Analysis

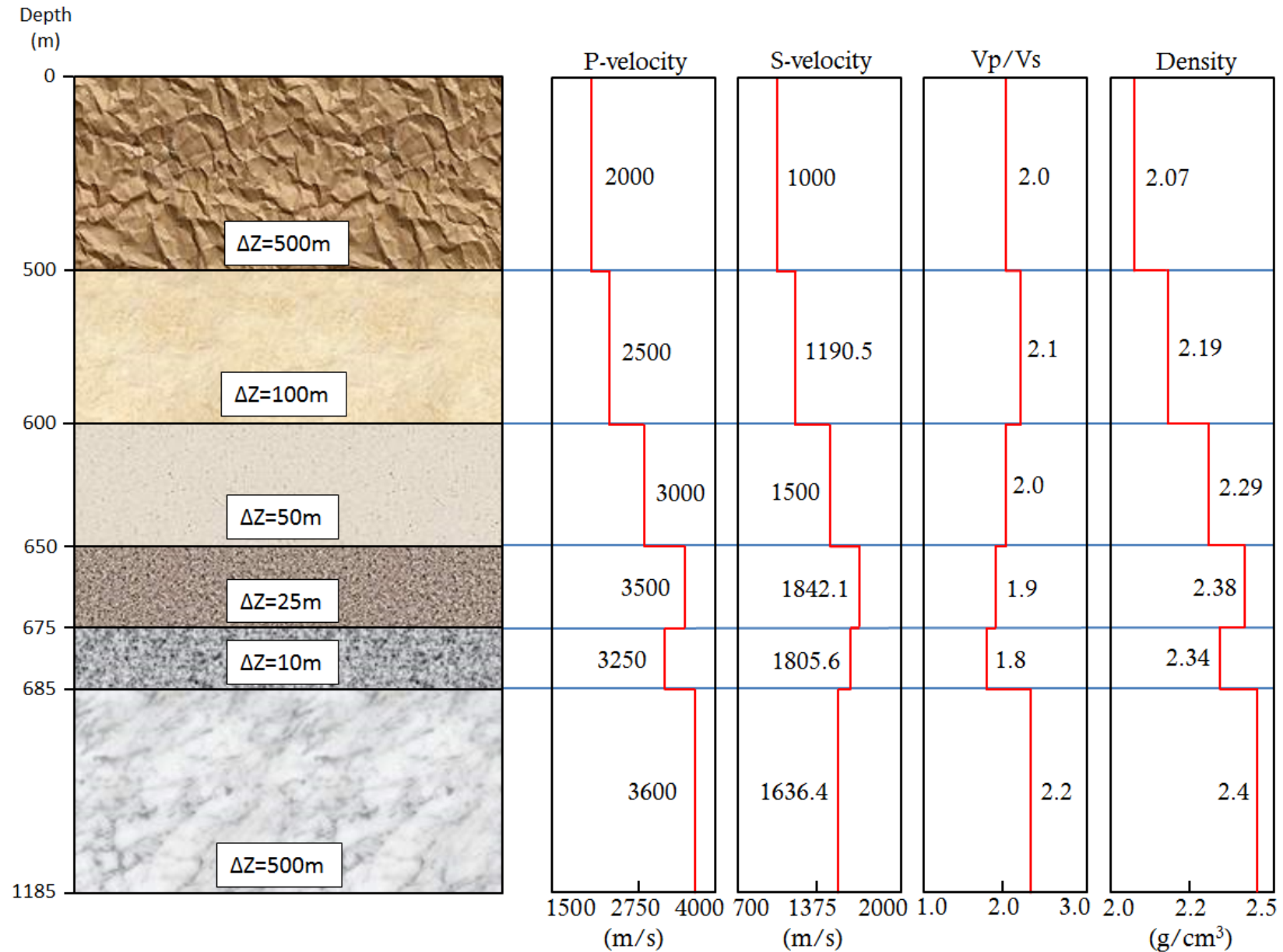


# Sensitivity Analysis



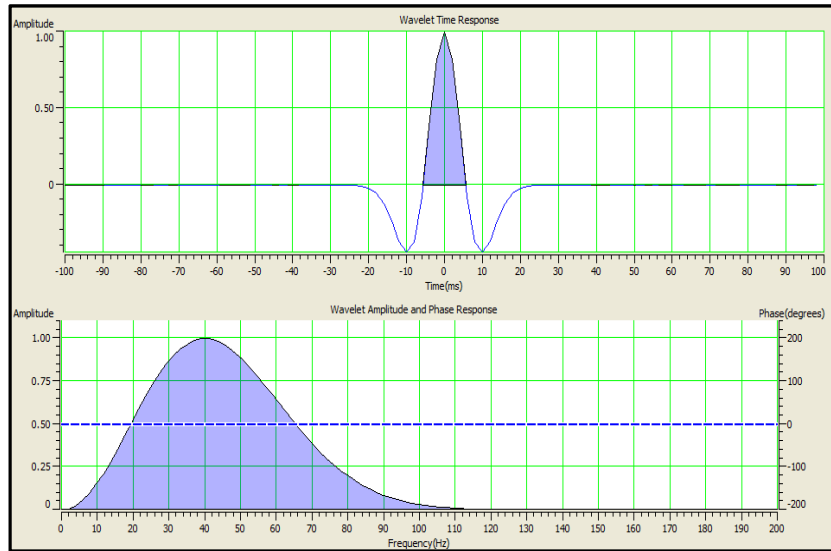


# Synthetic Model

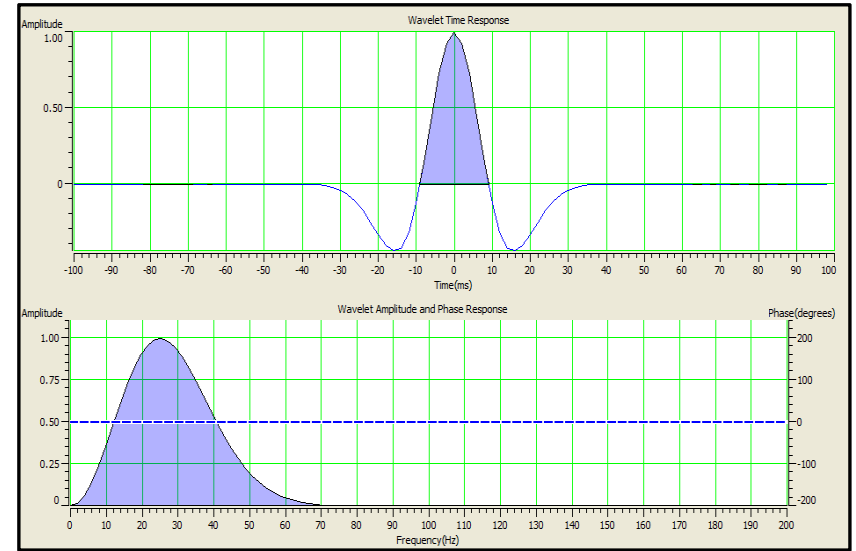


# Synthetic Model

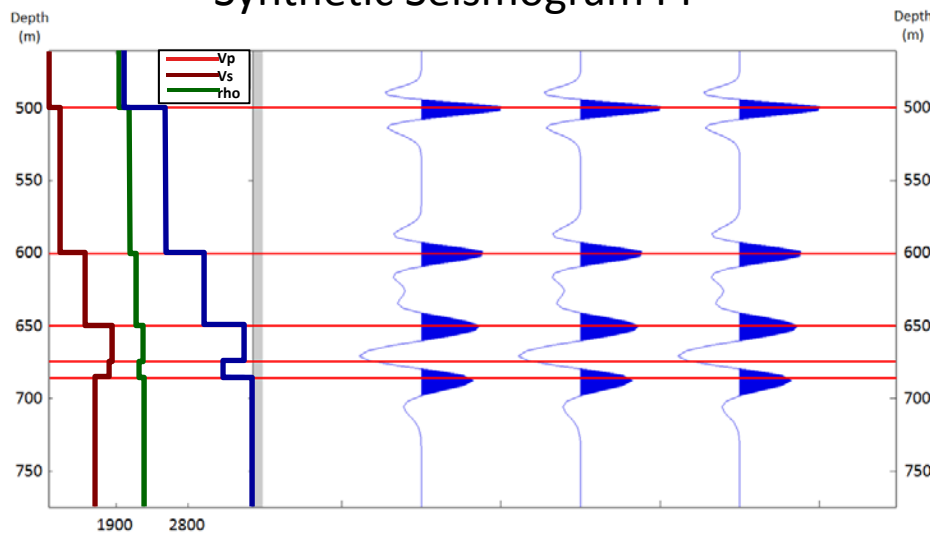
PP Wavelet



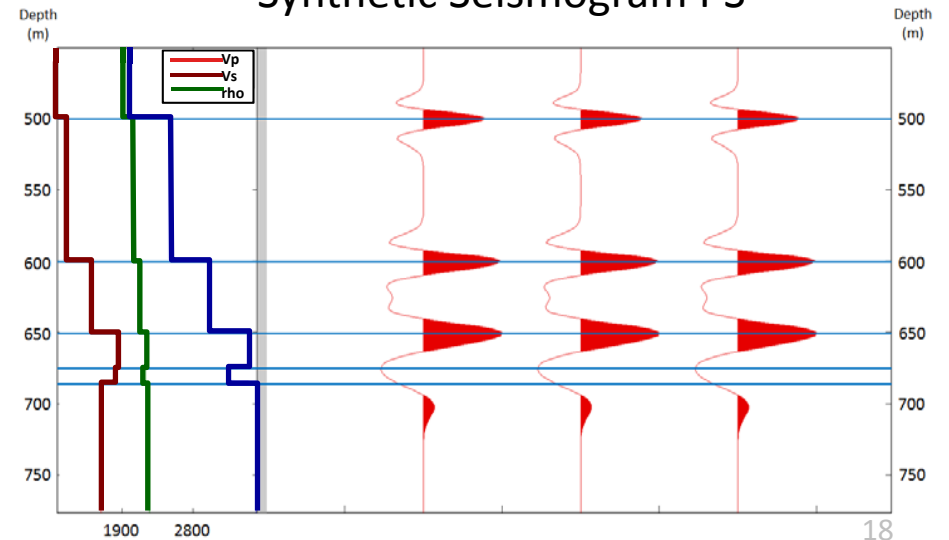
PS Wavelet



Synthetic Seismogram PP

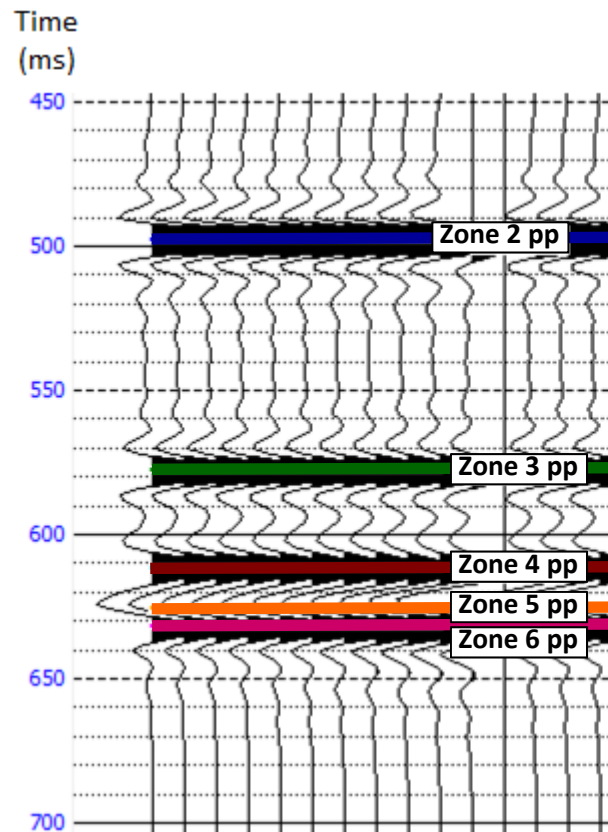


Synthetic Seismogram PS

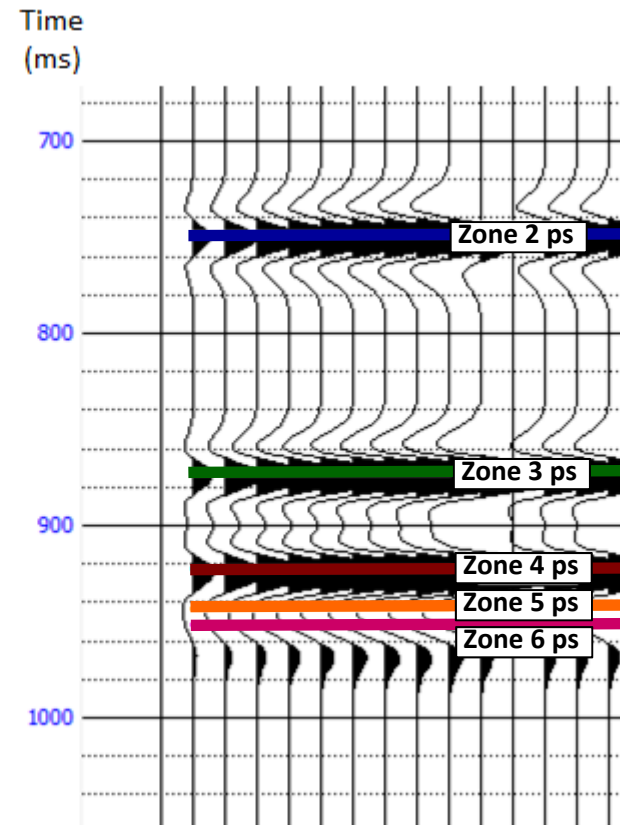


# Synthetic Model

## PP Seismic

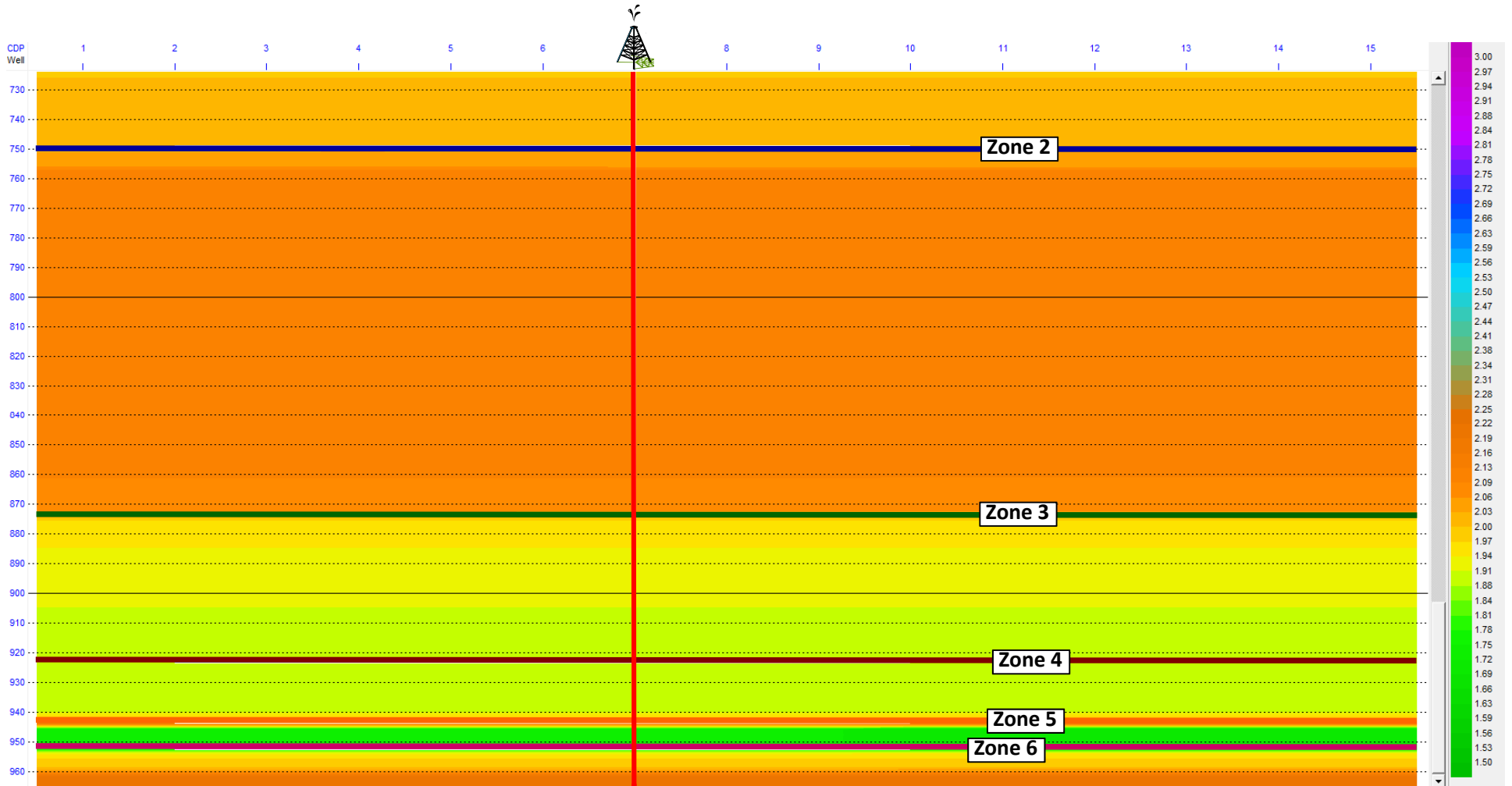


## PS Seismic



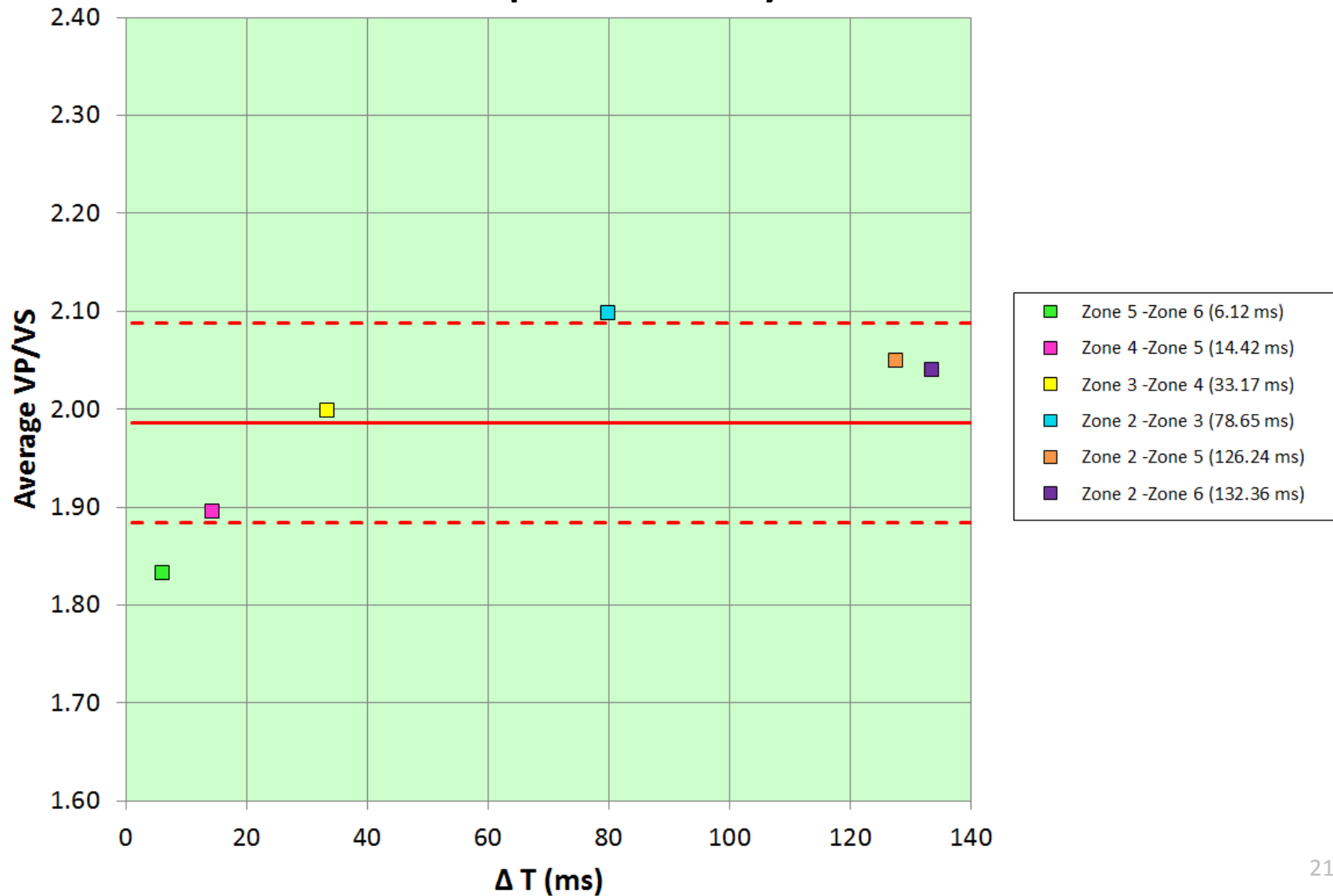
# Synthetic Model

## Vp/Vs analysis



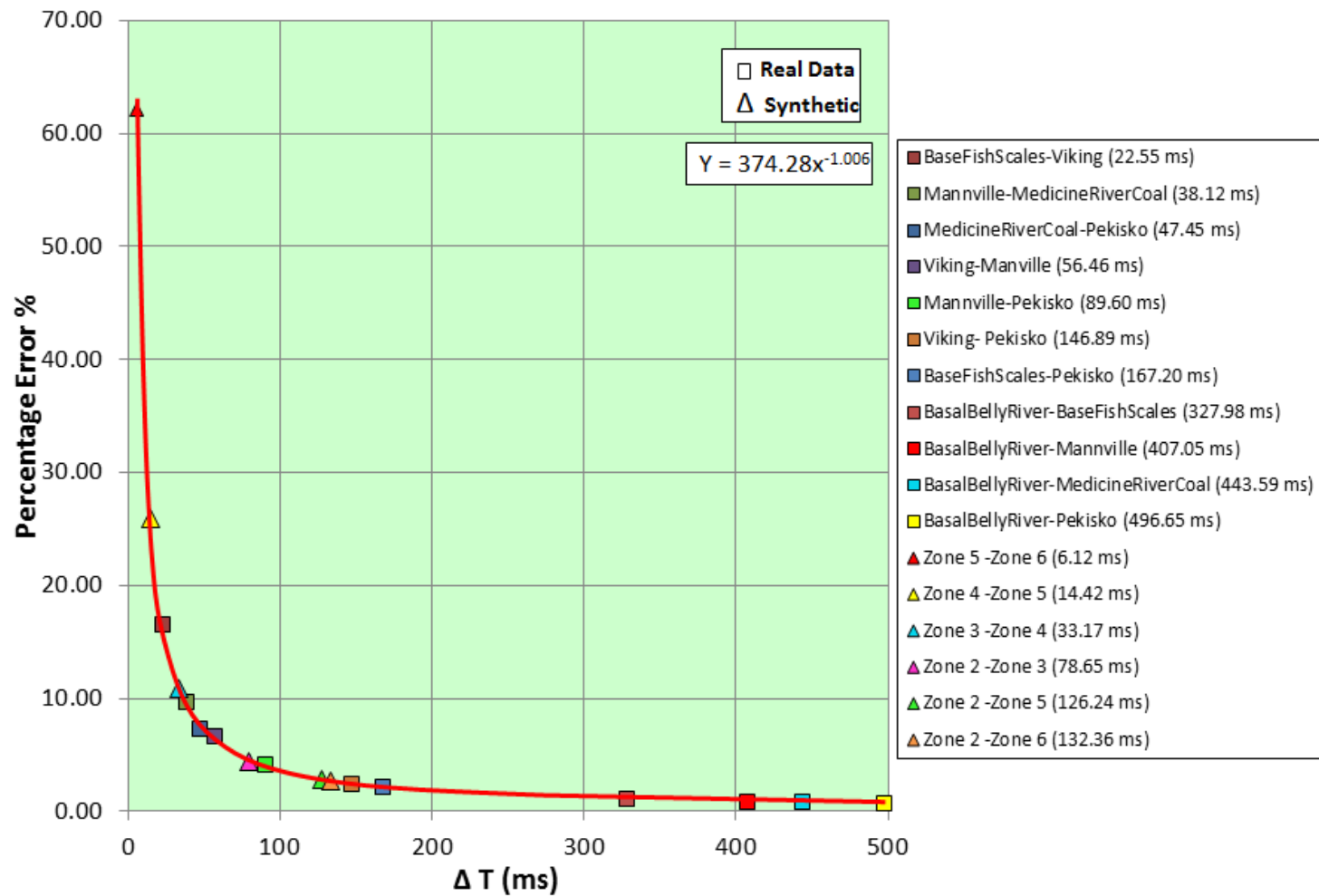
# Synthetic Model

## Vp/Vs analysis



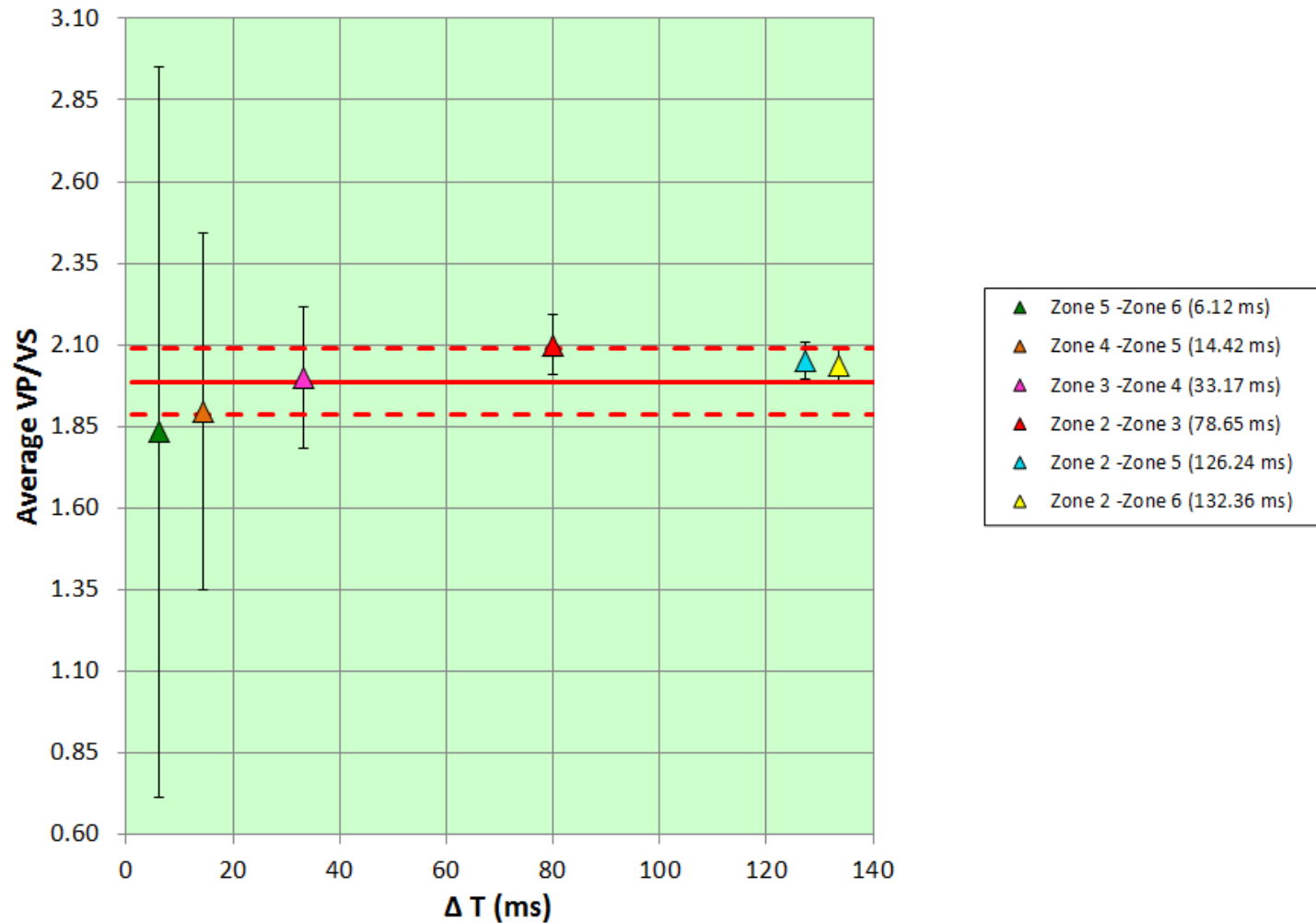
# Synthetic Model

Vp/Vs analysis assuming  $\pm 2$ ms uncertainty



# Synthetic Model

Vp/Vs analysis assuming  $\pm 2$ ms uncertainty



# Conclusions

- Analysis performed on the Hussar data indicates that the uncertainty in  $V_p/V_s$  values will increase as time interval becomes smaller.
- Based on the increasing behavior of error with respect to decrease in the time interval, it is suggested to use isochron intervals greater than 150 ms.
- Precise Horizon interpretation helps reduce uncertainty for  $V_p/V_s$  calculations.
- Results shows standard deviation to be affected by the interval time chosen.
- $V_p/V_s$  values in large isochrons are affected mostly by heterogeneity in the geology.



# Acknowledgements

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