

# Surface-consistent matching filters: theory and application

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## 1. SUMMARY

- This paper presents a new idea for designing a matching filter for processing time-lapse seismic data in a surface-consistent manner.
- We extend the surface-consistent data model to the case of designing matching filters to equalize two seismic surveys in the least-squares sense.
- The frequency-domain surface-consistent design equations are similar to those for surface-consistent deconvolution except that the data term is the spectral ratio of two surveys.
- Since taking spectral ratios poses a challenge, we design the matching filters in a least-squares sense in the time domain and Fourier transform the result.
- We decompose the result into four surface-consistent components: source, receiver, offset, and midpoint.
- Two examples are presented to support this innovation.

## 2. THEORY

### 2.1: SURFACE-CONSISTENT MODEL

- The seismic trace can be modeled as:

$$d_{ij}(t) = s_i(t) * r_j(t) * h_k(t) * y_l(t) \quad (1)$$

$d_{ij}$  : the seismic trace;  $t$  is time; and  $*$  for convolution  
 $s_i$  : represent source consistent effect,  $i$  source index  
 $r_j$  : represent receiver consistent effect,  $j$  = receiver index  
 $h_k$  : offset response,  $k = |i - j|$   
 $y_l$  : subsurface response,  $l = (i + j)/2$

This hypothesis is commonly used to solve: statics problem, deconvolution, amplitude balancing and phase-rotation.

### 2.2: MATCHING FILTERS

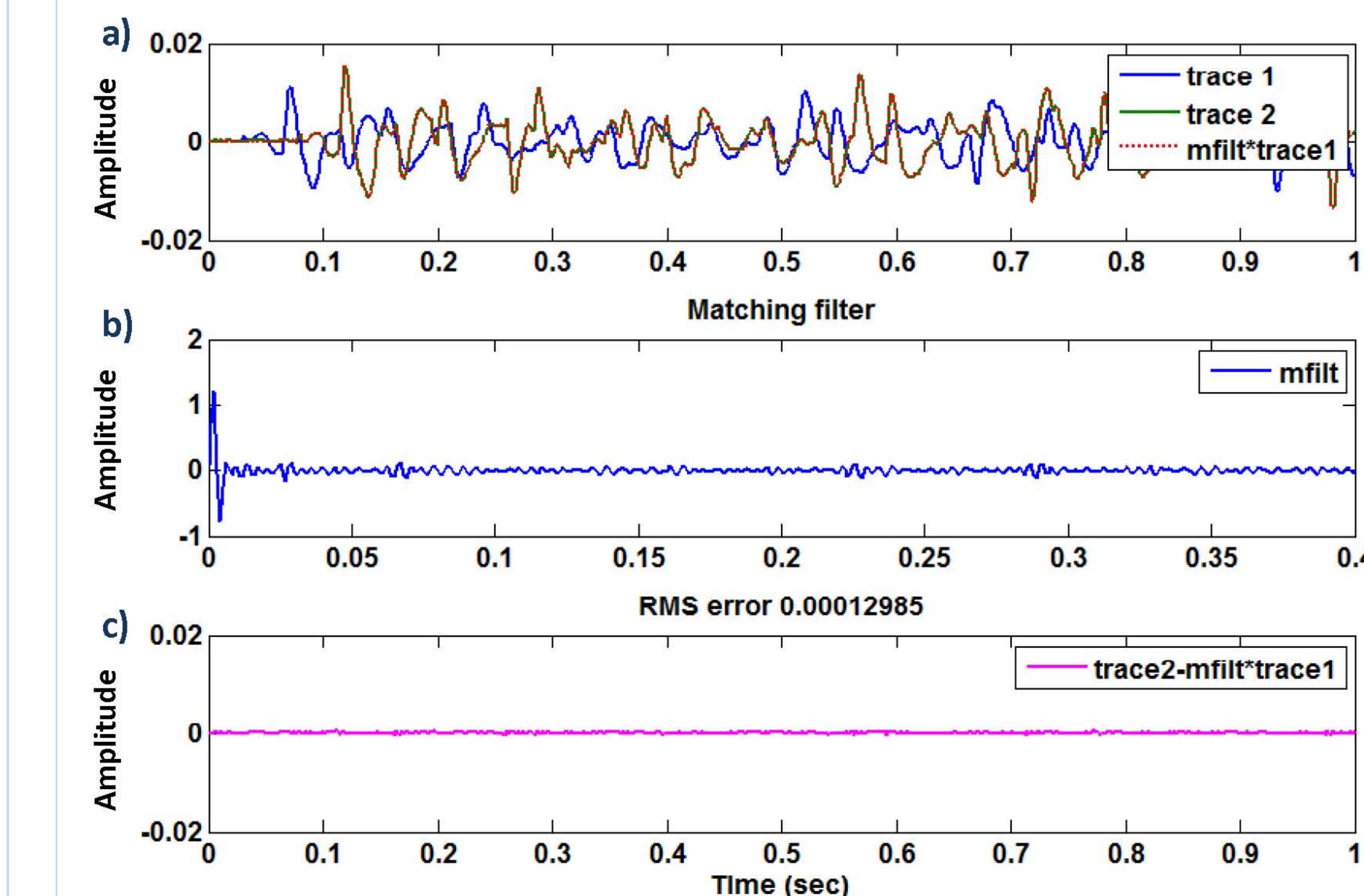


Fig. 1: Two traces (a), their matching filter (b), and residual between trace2 and the matched trace (c).

To match  $s_1$  to  $s_2$ :

$$m * s_1 = s_2 \quad (2)$$

In Fourier domain:

$$M(\omega) = \frac{S_2(\omega)}{S_1(\omega)} \quad (3)$$

Important remarks:

- I. A perfect matching filter is a spectral ratio, however,
- II. eqn. 3 is unstable in presence of noise; and
- III. its LSQ solution is approximate.

## 3. CONSTRUCTION OF MATCHING FILTERS

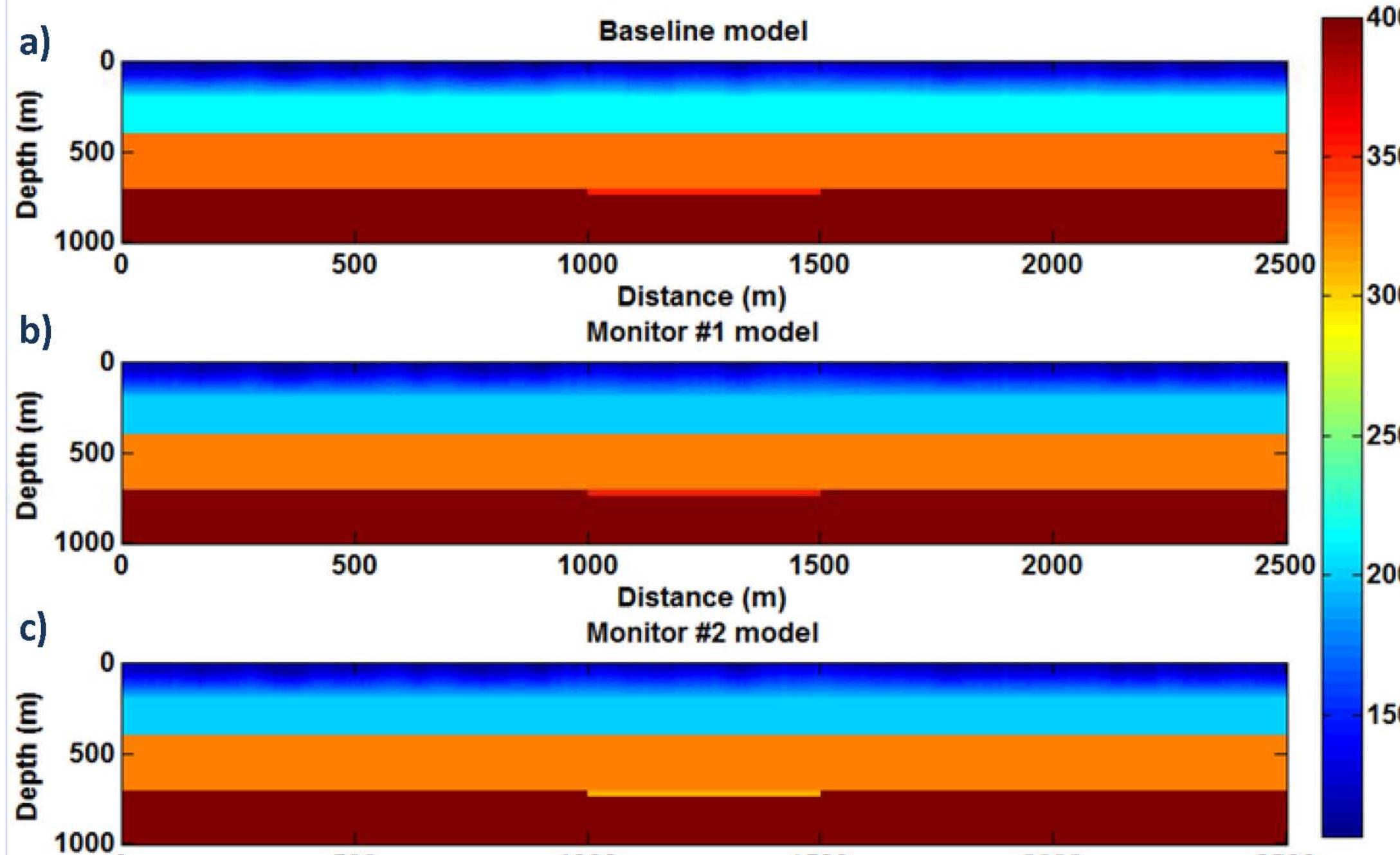


FIG. 2: Baseline model (a) and monitor # 1 model (b) have similar subsurface but differ in near-surface velocity. Monitor # 2 model (c) is similar to (b) except the subsurface (reservoir) is different.

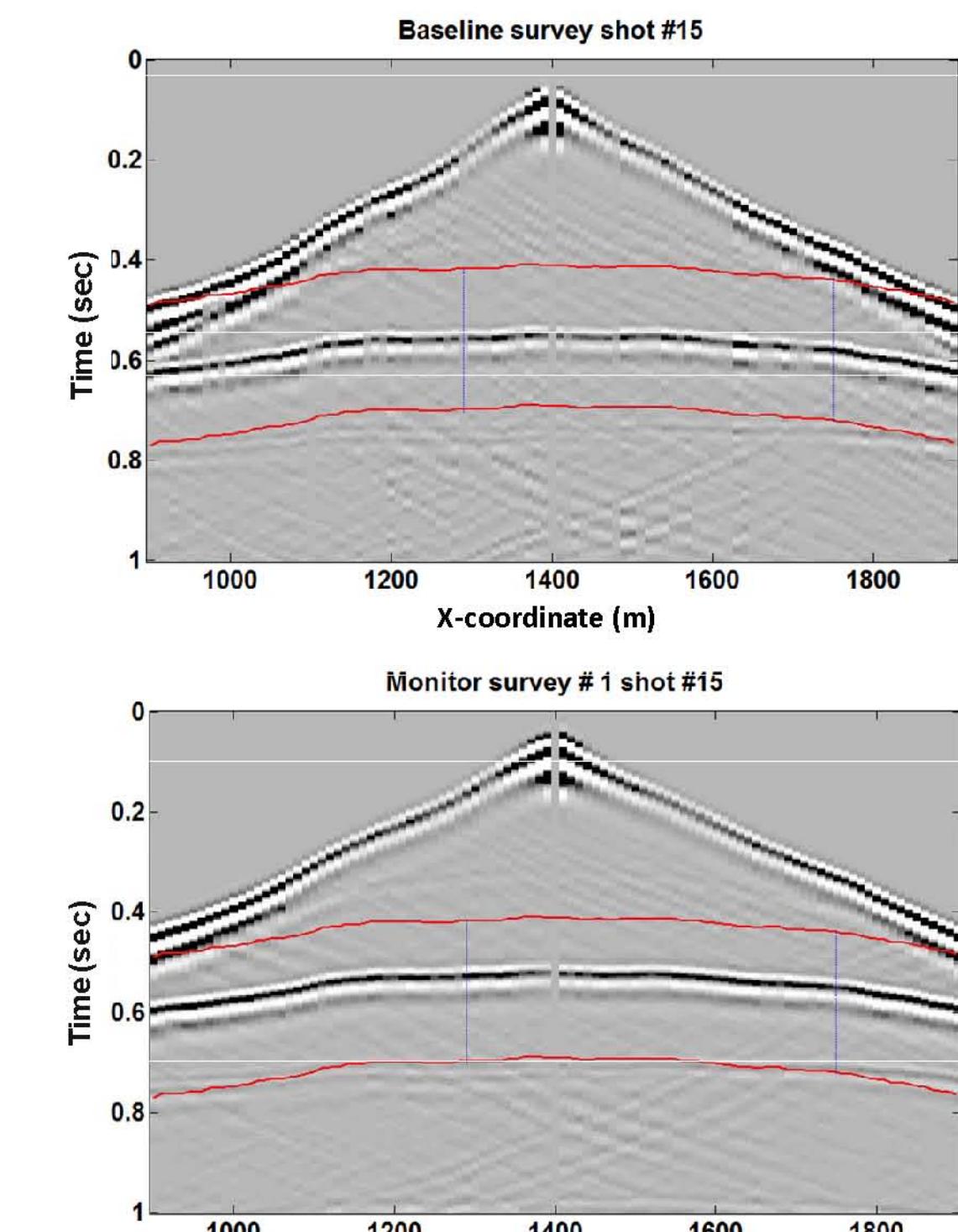


FIG. 3: Input seismic data.

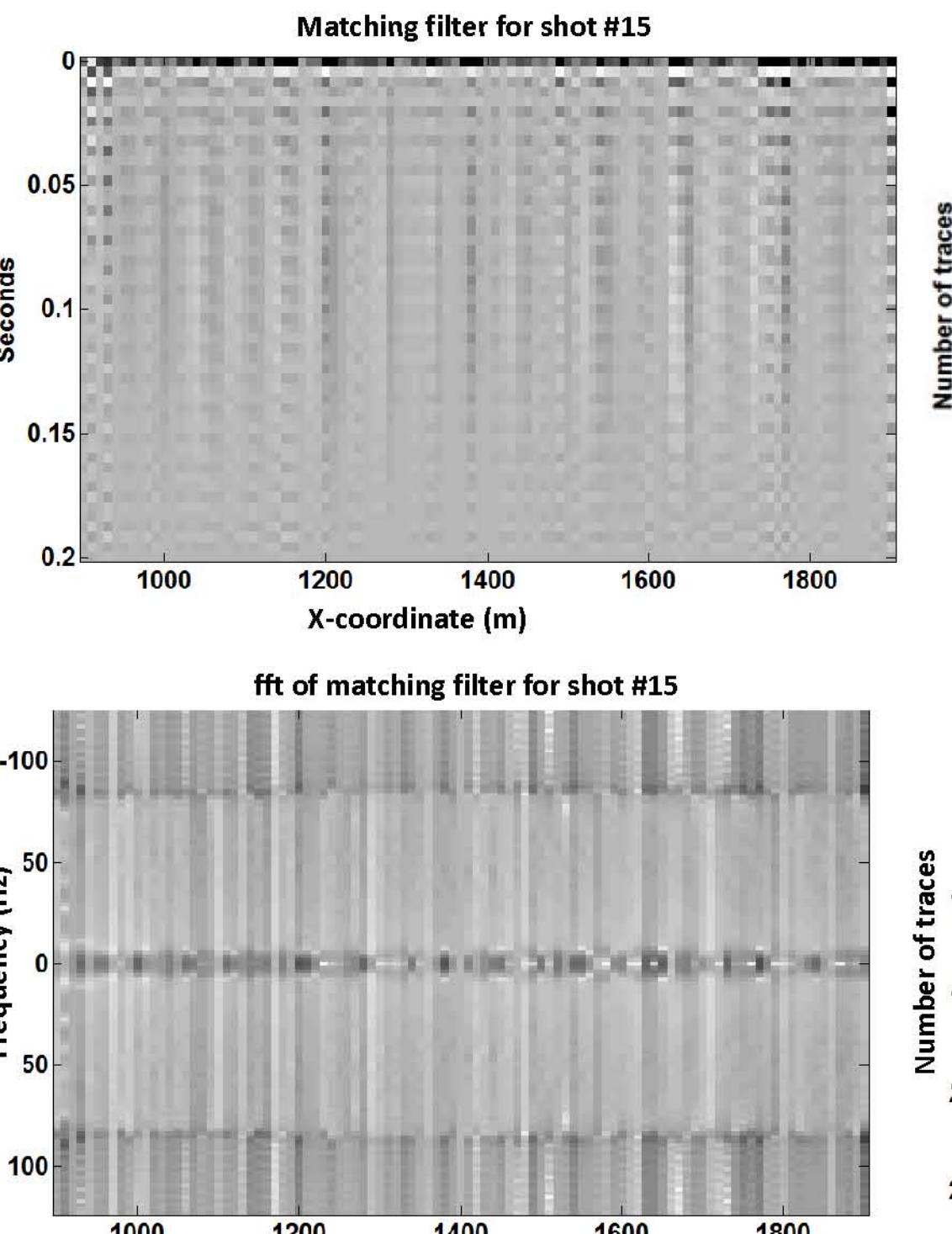


FIG. 4: Matching filters.

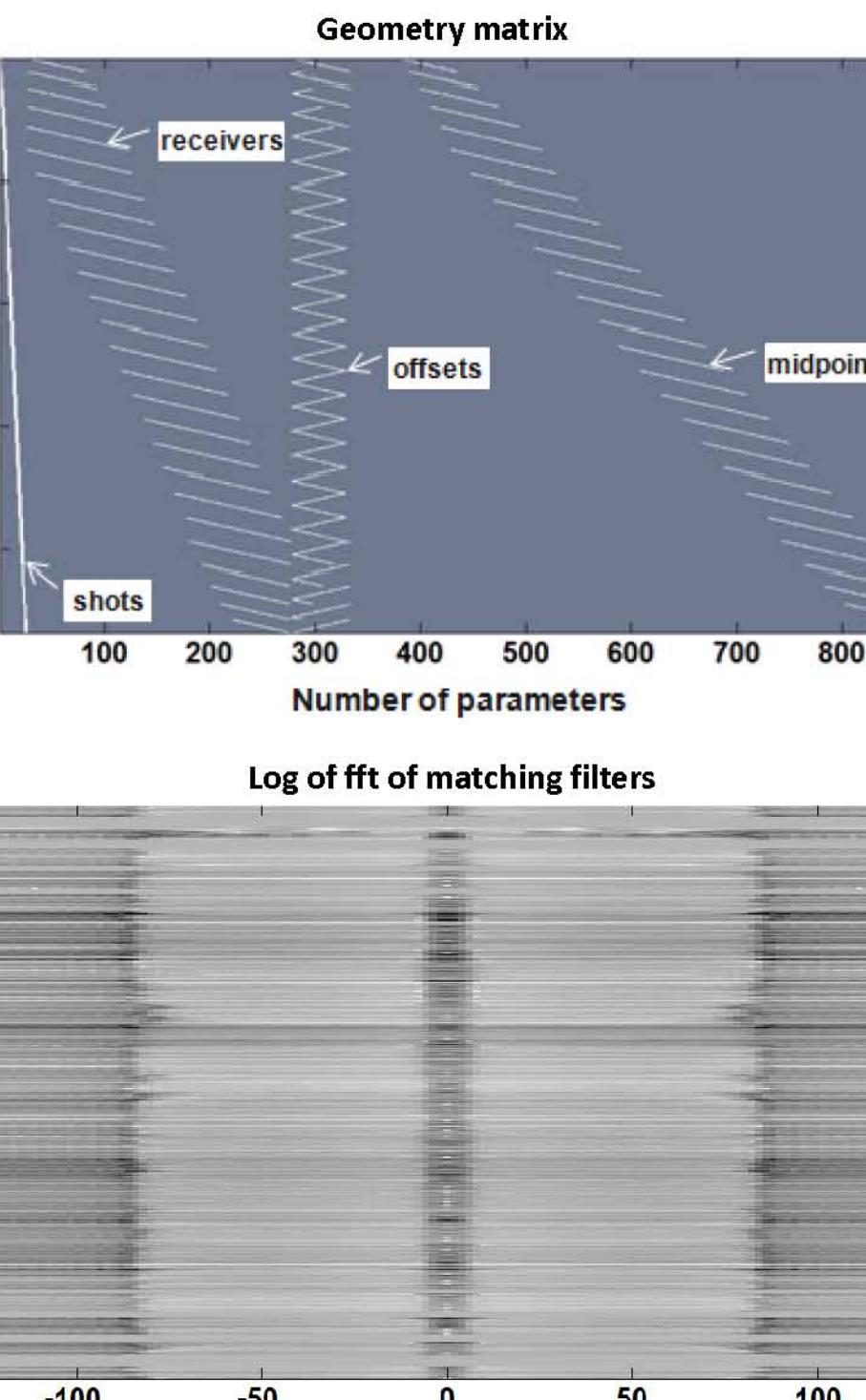


FIG. 5: The log of fft of the matching filters.

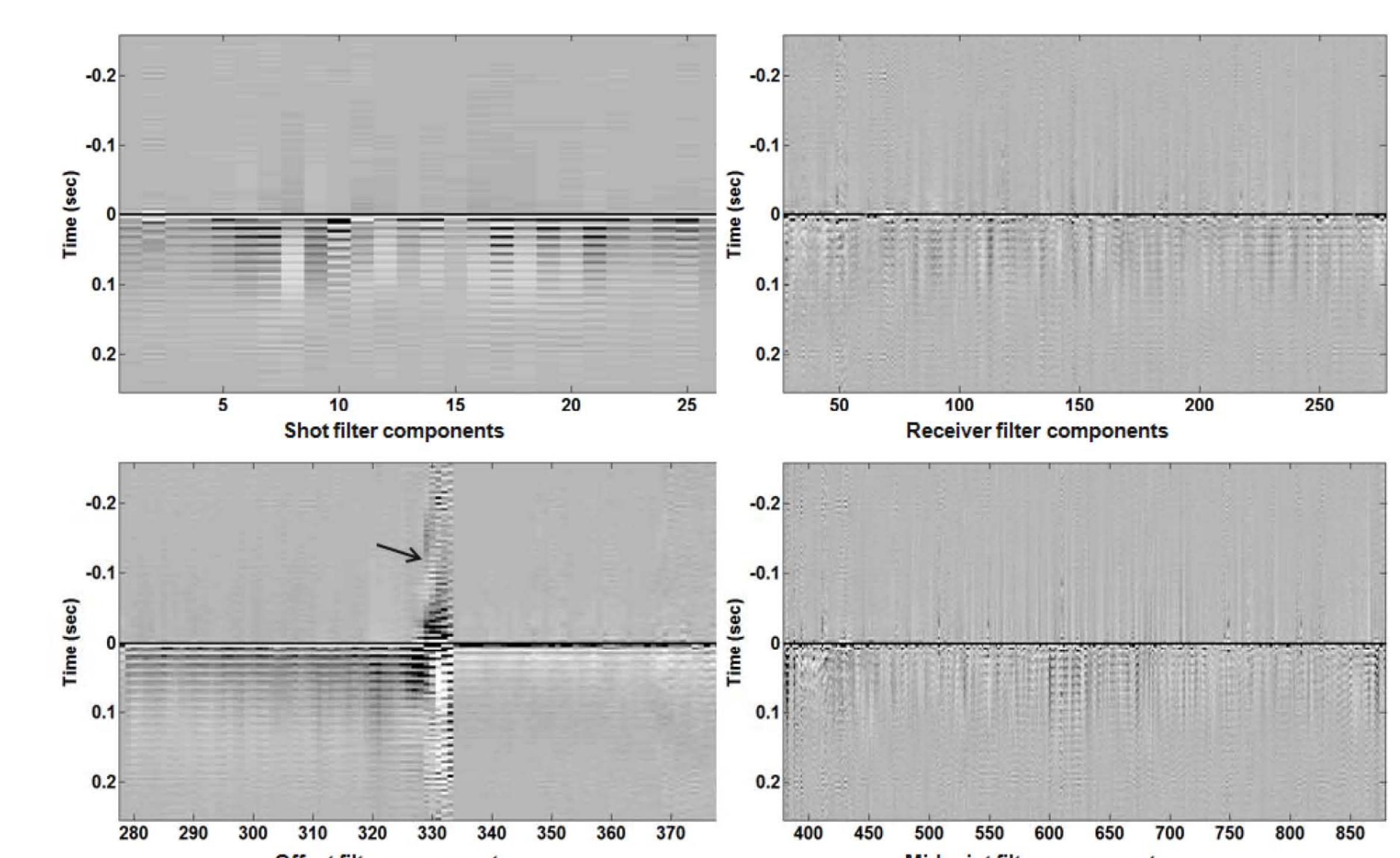


FIG. 6: The four-components filters.

## 4. EXAMPLES

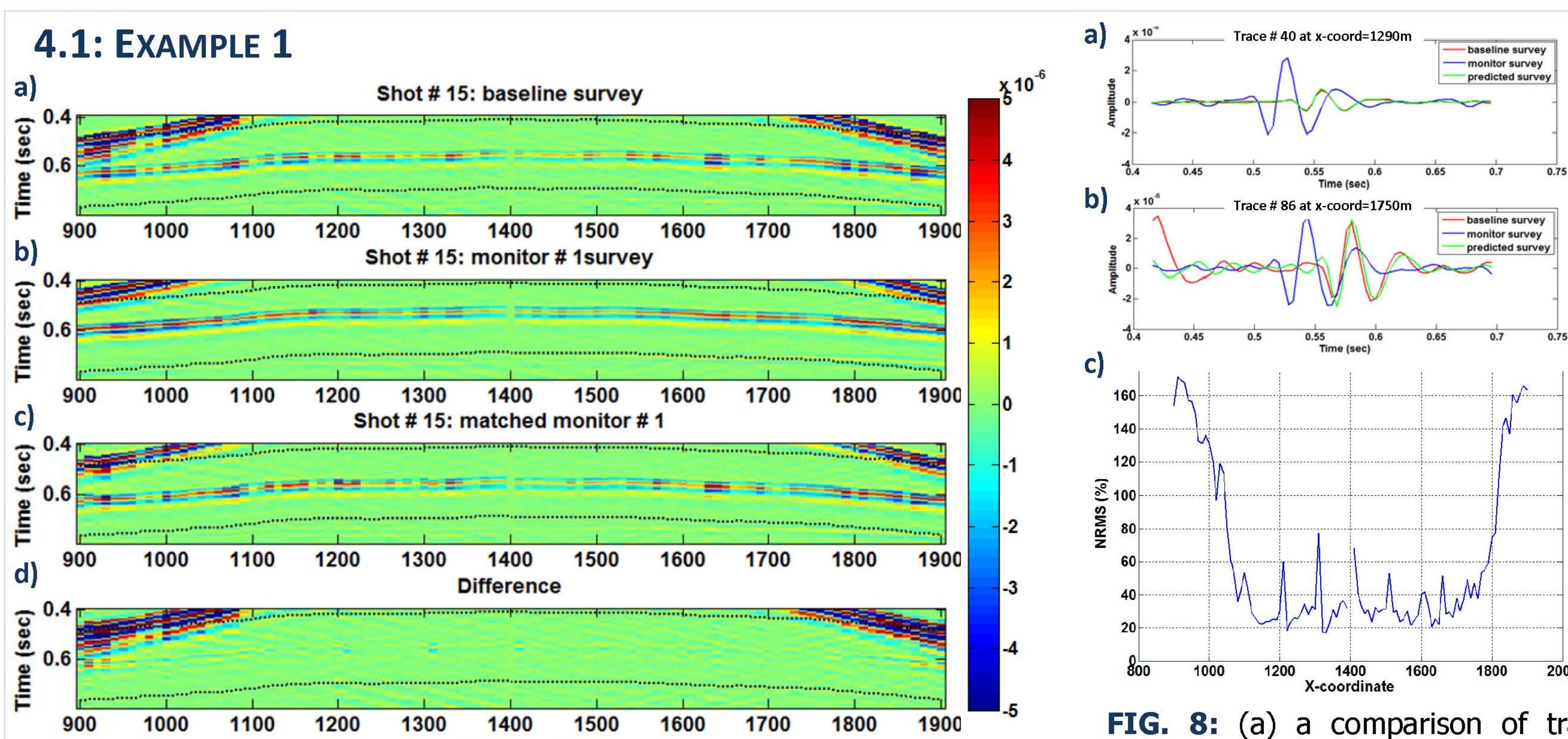


FIG. 7: (a) baseline, (b) monitor # 1, (c) matched monitor # 1, and (d) the difference between baseline and matched monitor.

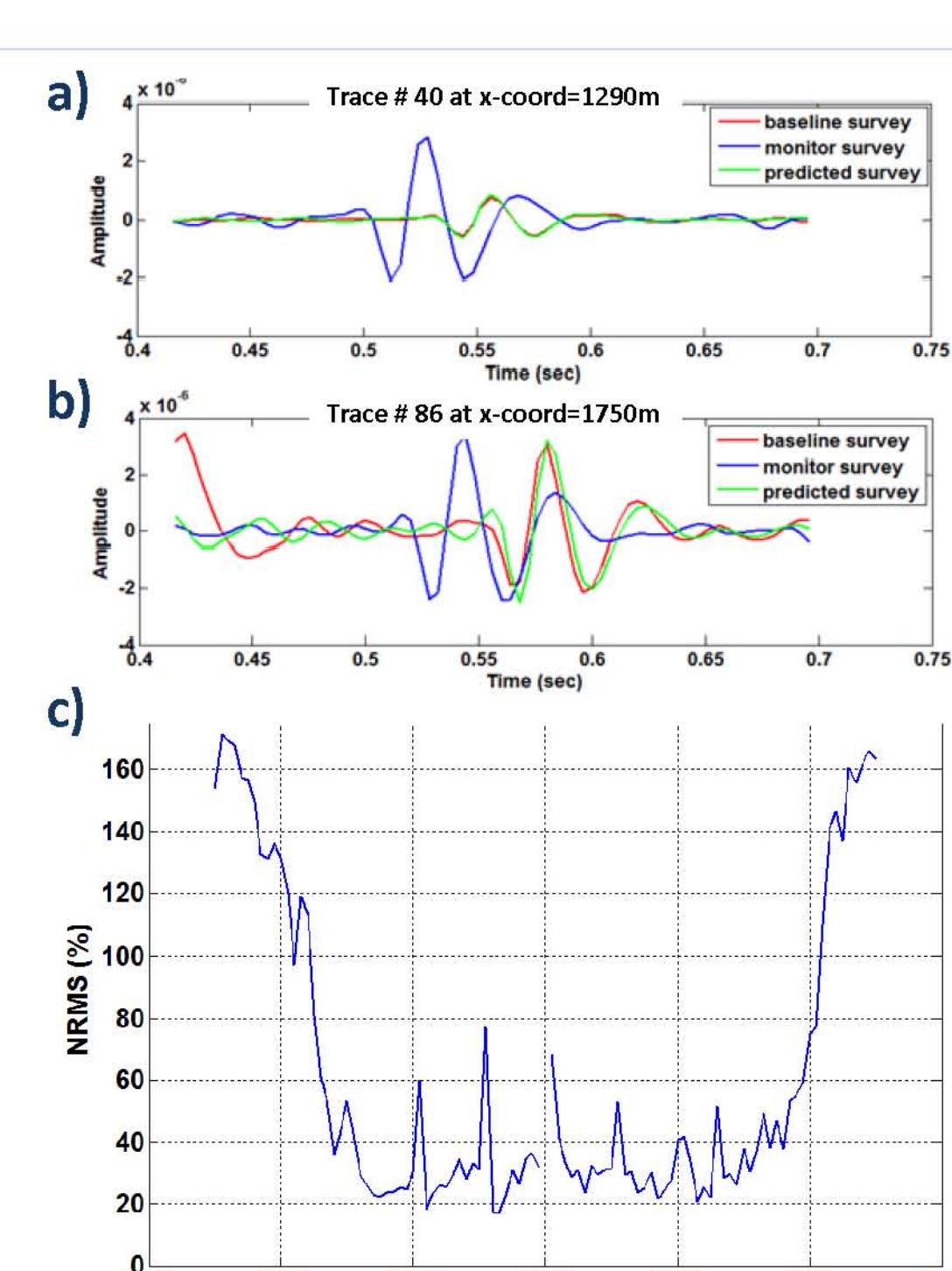


FIG. 8: (a) a comparison of trace #40 from top three shots in Figure 7, and similarly (b) shows trace #86. Nrms values are shown in (c).

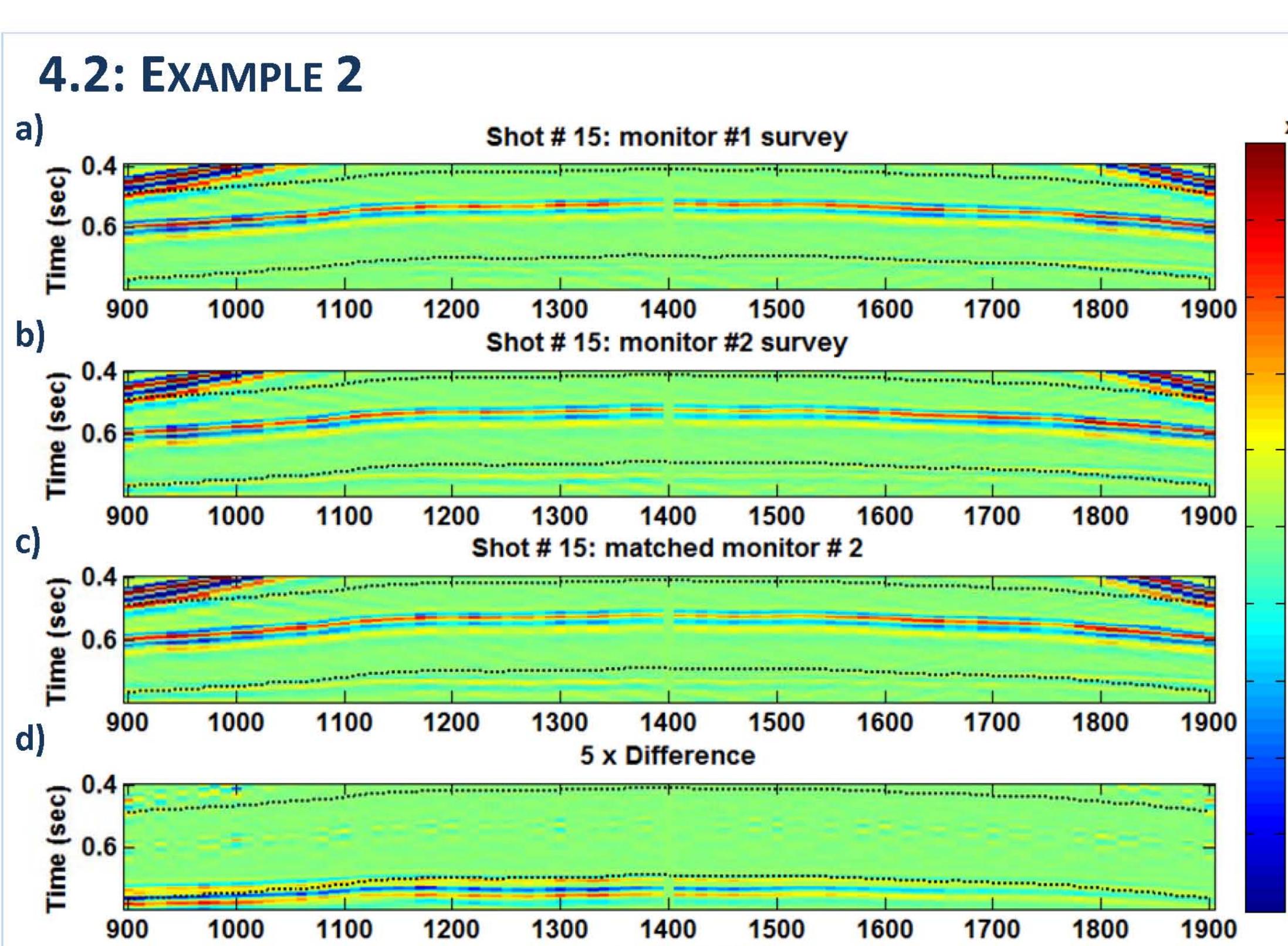


FIG. 9: (a) monitor #1, (b) monitor #2, (c) matched monitor # 2, and (d) the difference between monitor #1 and matched monitor #2

### 4.2: EXAMPLE 2

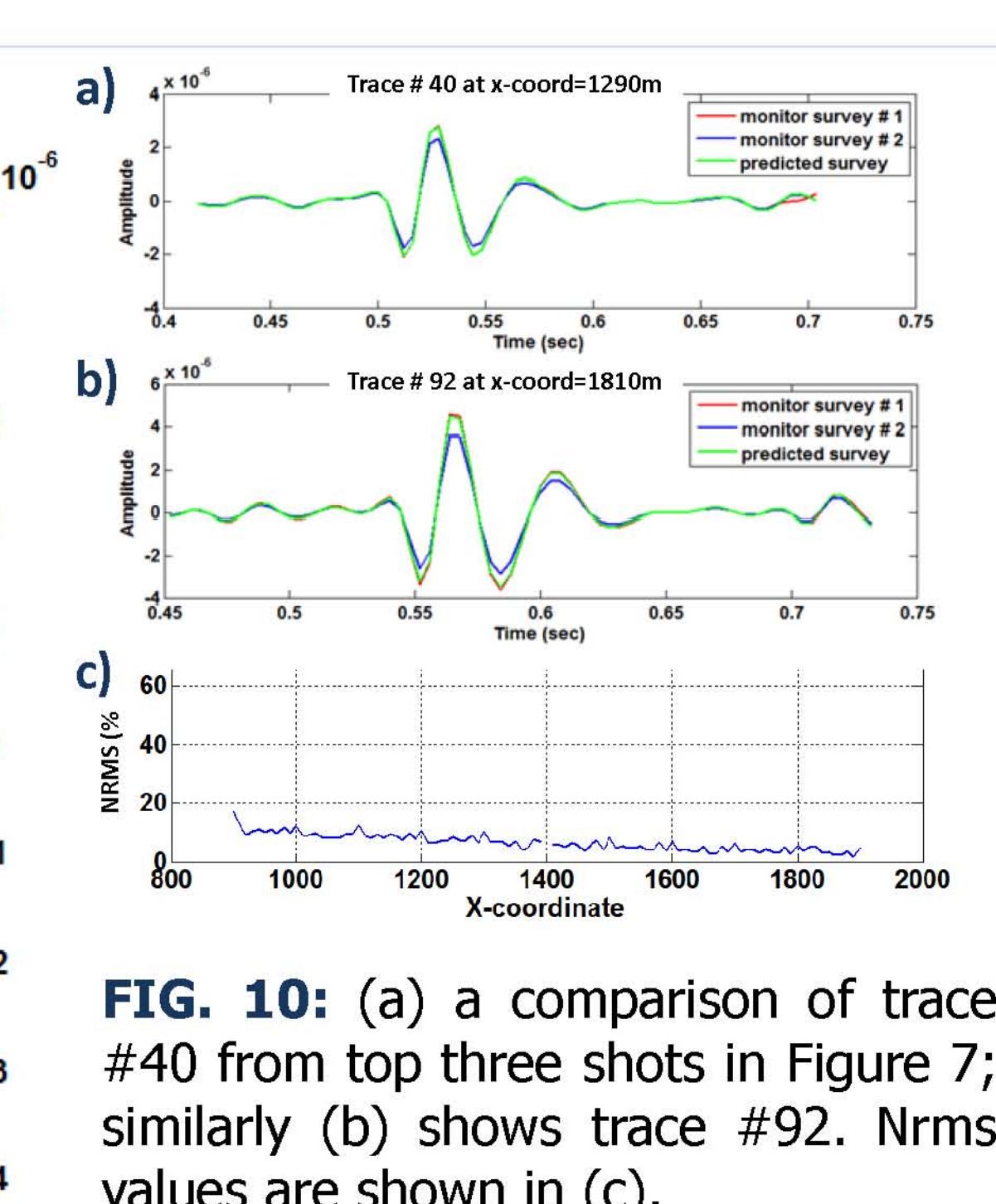
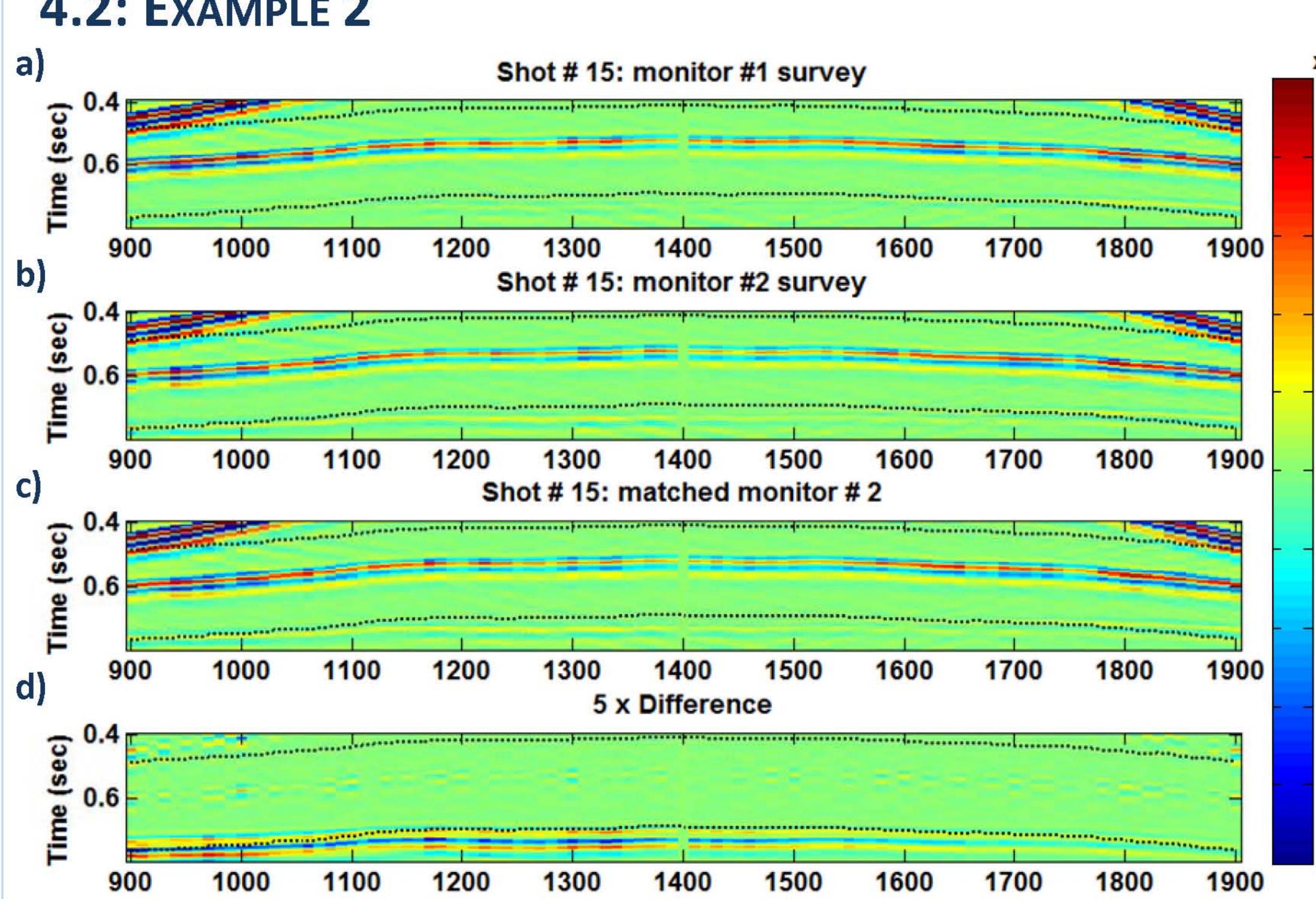


FIG. 10: (a) a comparison of trace #40 from top three shots in Figure 7; similarly (b) shows trace #92. Nrms values are shown in (c).

### WHAT IS NRMS?

NRMS is a metric measure of the differences in time-lapse data sets. Low NRMS values indicate higher similarities between traces

$$NRMS = \sqrt{\frac{RMS(a) - RMS(b)}{RMS(a) + RMS(b)}}$$

## 5. ACKNOWLEDGMENTS

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## REFERENCES:

Please see Almutlaq and Margrave 2011 CREWES report for complete list of references.