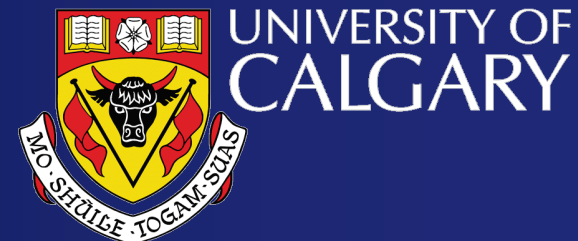


# Delta weights for footprint suppression in 3D prestack migration

Joanna K. Cooper, Gary F. Margrave,  
and Don C. Lawton

November 20, 2009



# Outline

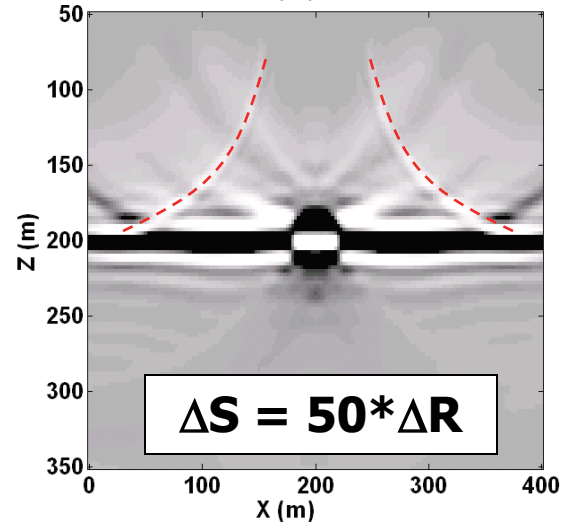
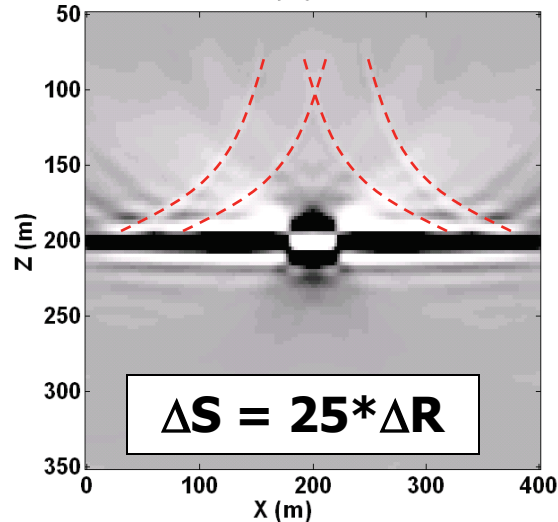
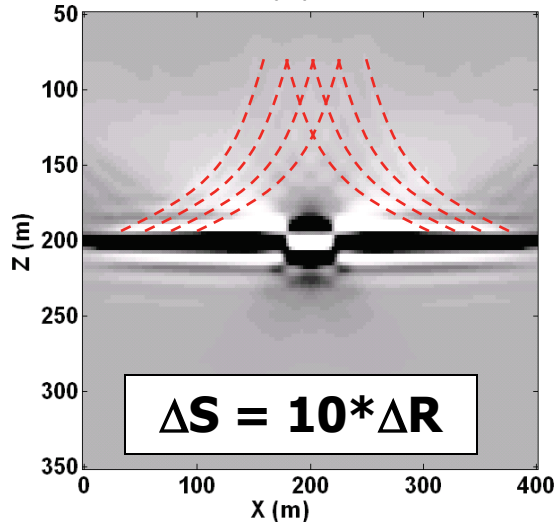
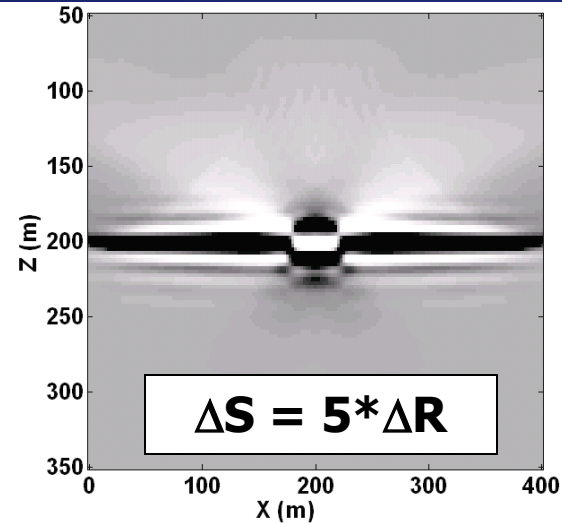
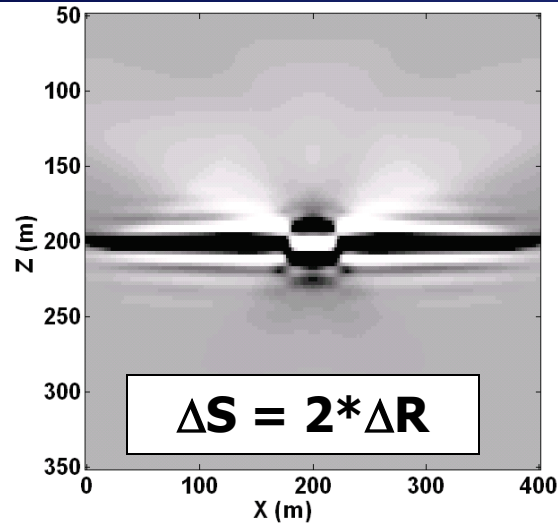
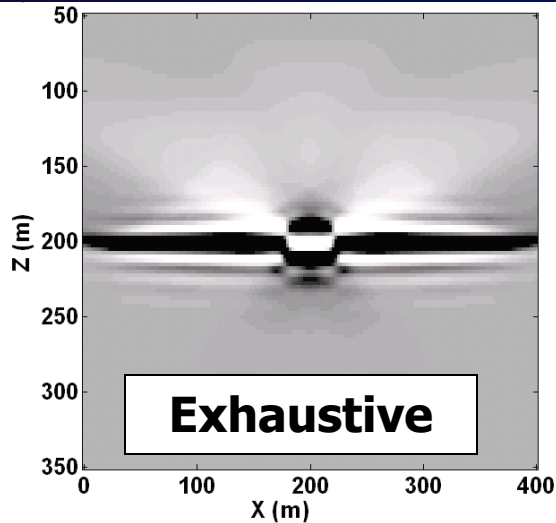
- Review of previous 2D results
- Review of method for angle-weighted stacking
- Application of method in 3D
- Conclusions

# Recap: 2D Footprint Simulations

- Modelled an exhaustive 2D dataset: shots and receivers spaced at 5 m intervals over a 400 m long model
- Created five shot decimations with shot spacings of 10 m, 25 m, 50 m, 100 m, and 200 m
- Applied Kirchhoff prestack migration and stacked migrated shot records

# Recap: 2D Simulations

## ■ Prestack migrated sections:



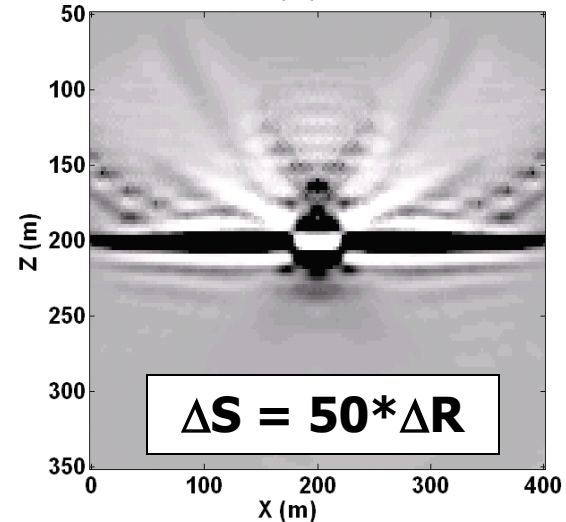
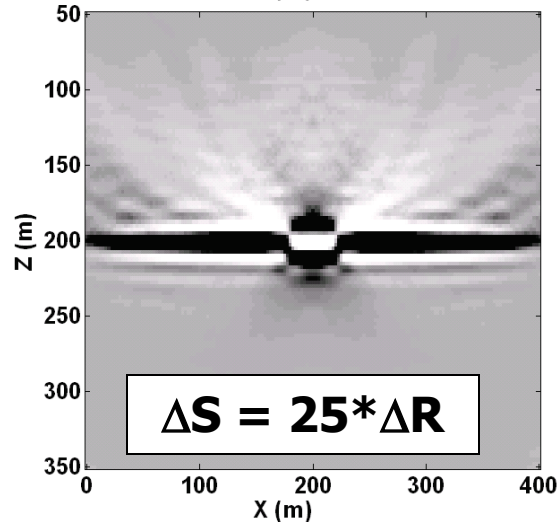
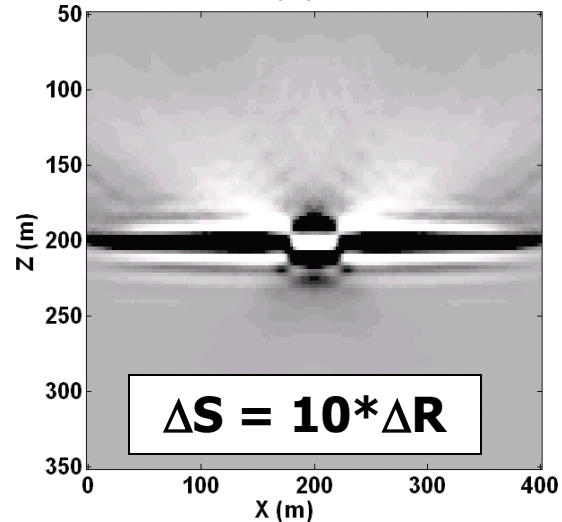
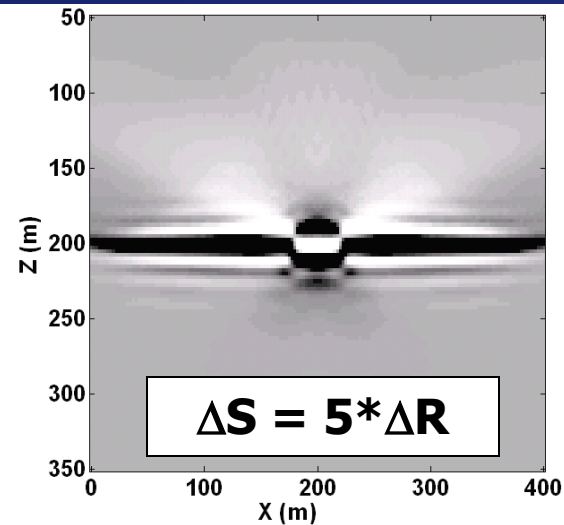
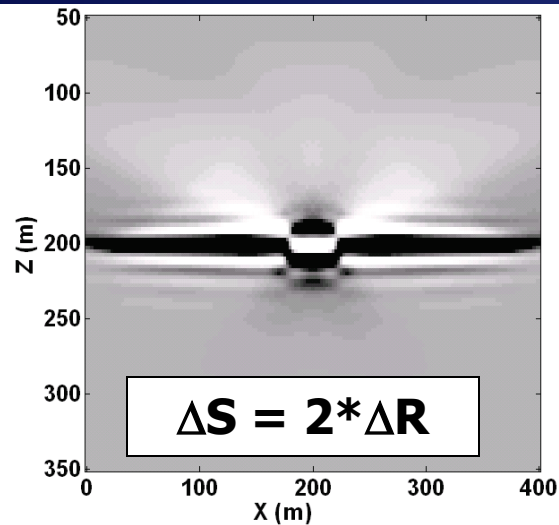
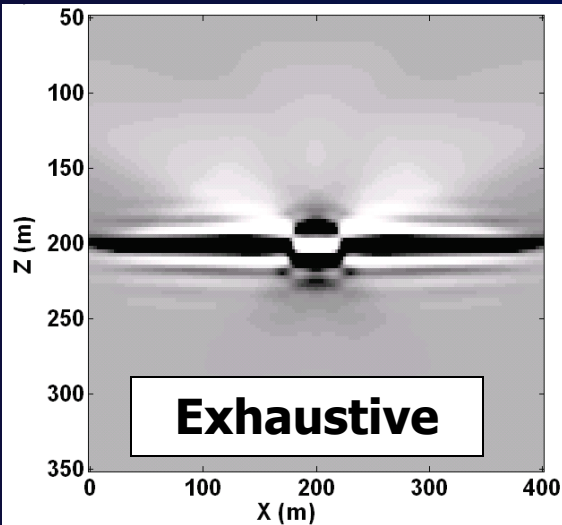


# Recap: 2D Footprint Simulations

- Footprint manifests as residual migration wavefronts
- Hypothesis: prestack migration weights may allow for proper interference of wavefronts, thereby reducing these artefacts
- Applied Kirchhoff prestack migration with delta-ratio weighting

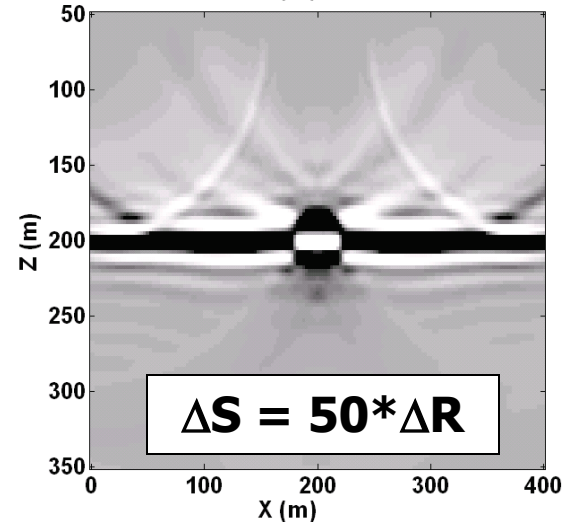
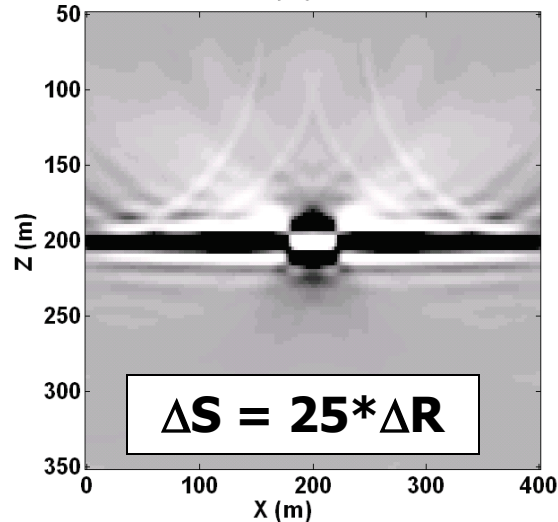
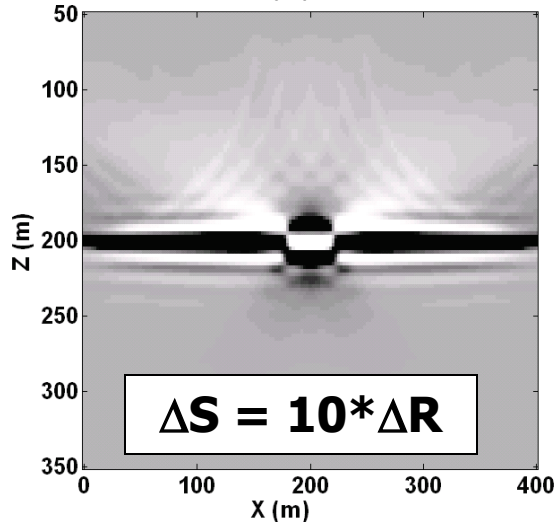
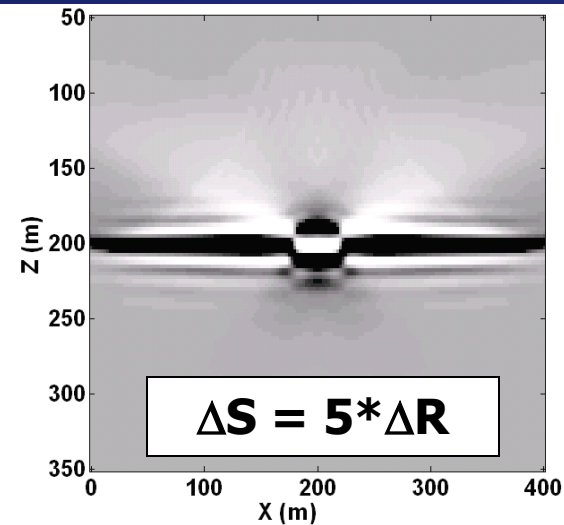
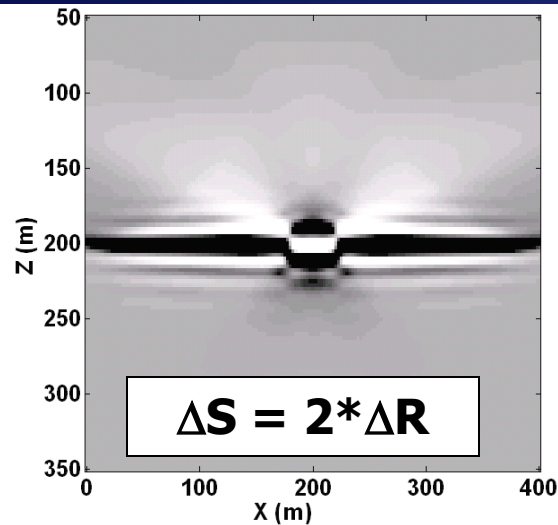
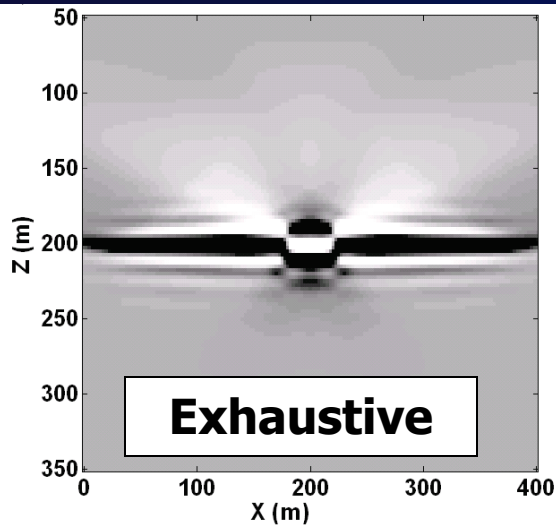
# Recap: 2D Simulations

## ■ Results: delta-ratio weights



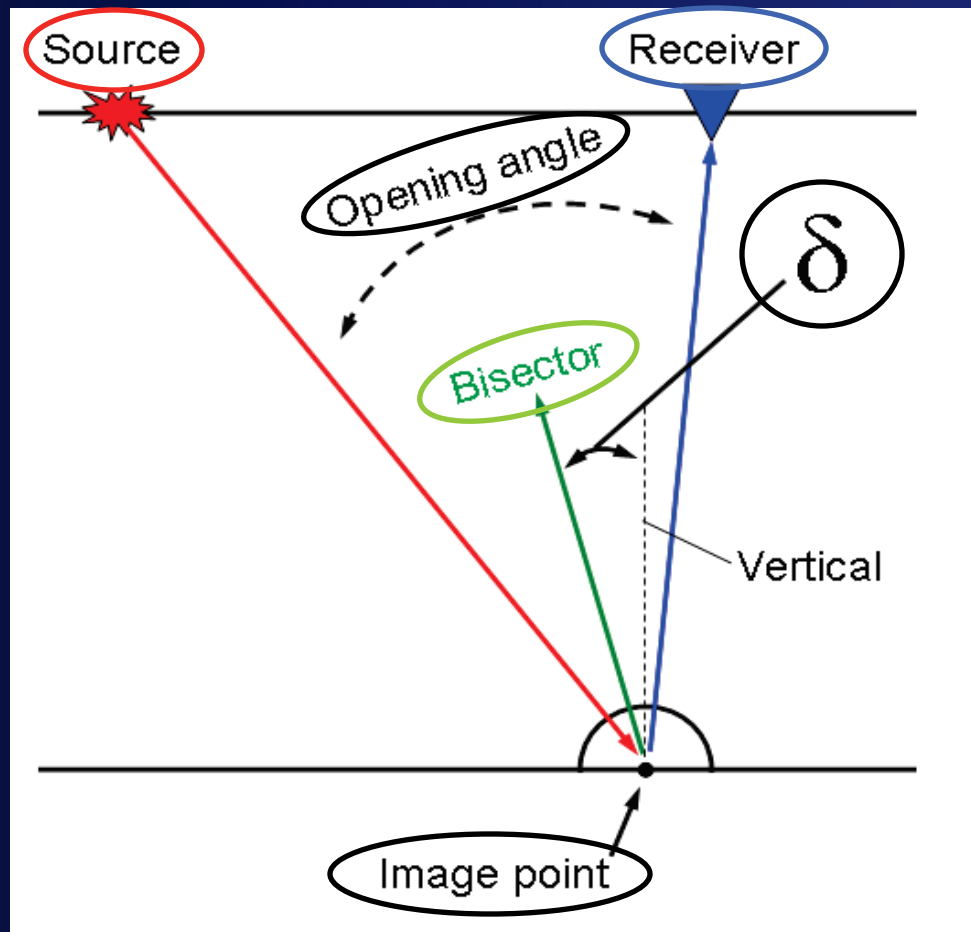
# Recap: 2D Simulations

## ■ Prestack migrated sections:



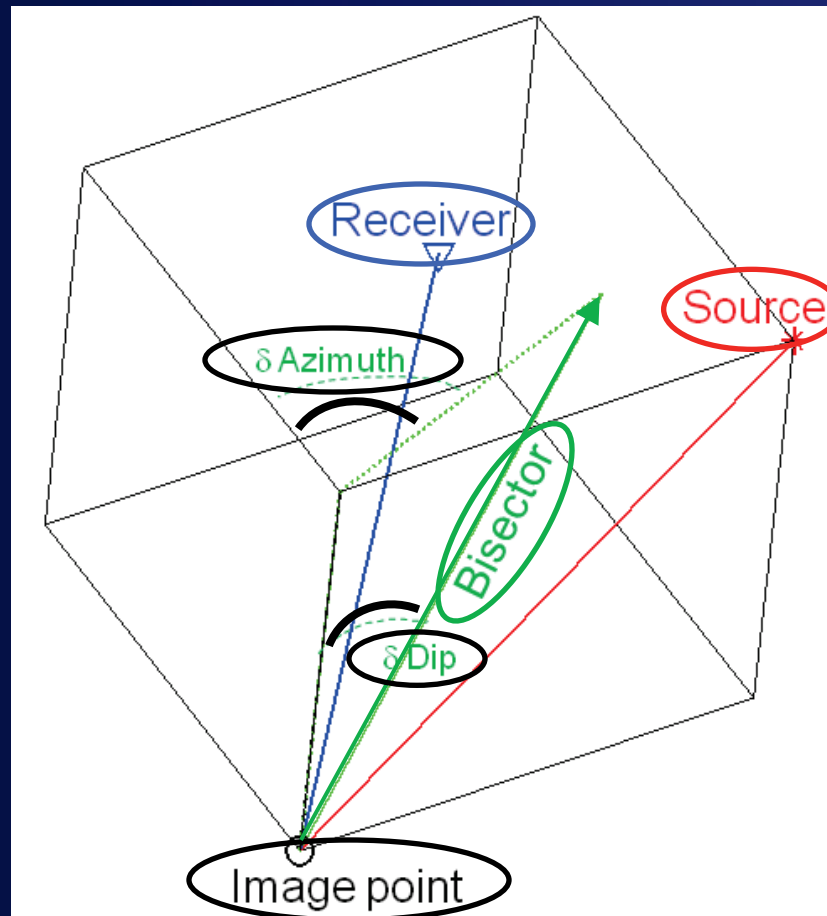
# Recap: Method

- Concept: illumination of image point by delta angles



# Recap: Method

- Concept: illumination of image point by delta angles



# Method

- Measure hit counts in delta bins at each image point
- Want to achieve uniform illumination by normalizing by delta hit counts
  - Method 1: Make hit counts in each bin equal (“delta-fold weights”)
  - Method 2: Make hit counts in each bin equal to what they would be in the exhaustive survey (“delta-ratio weights”)

# Method

- Migrate each shot record into delta-limited volumes and apply weights during stacking:

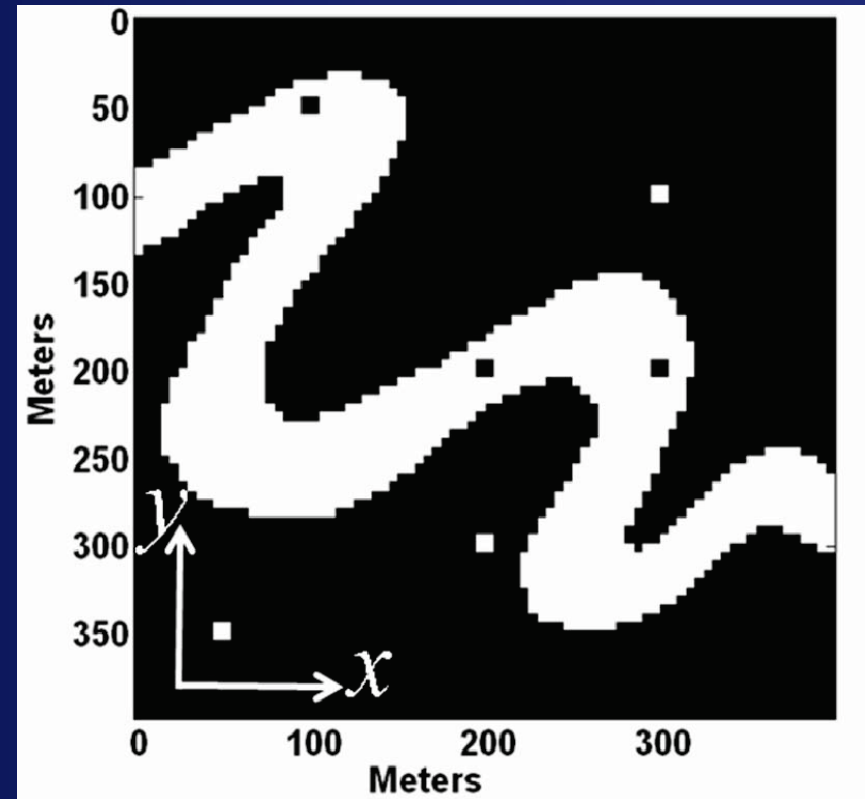
$$\text{Im}(\underline{x}) = \sum_{j \text{ shots}} \left[ \sum_{k \text{ bins}} W_k(\underline{x})^* \phi_j(\underline{x}, \delta_k) \right],$$

where  $W_k(\underline{x}) = 1/n(\underline{x}, \delta_k)$  (delta-fold)

or  $W_k(\underline{x}) = n_{\text{exh}}(\underline{x}, \delta_k) / n(\underline{x}, \delta_k)$  (delta-ratio)

# Recap: 3D Model

- $v(z)$  model with three flat reflectors
- Featureless reflectors at 100m and 180m depth
- Channel reflector at 200m depth

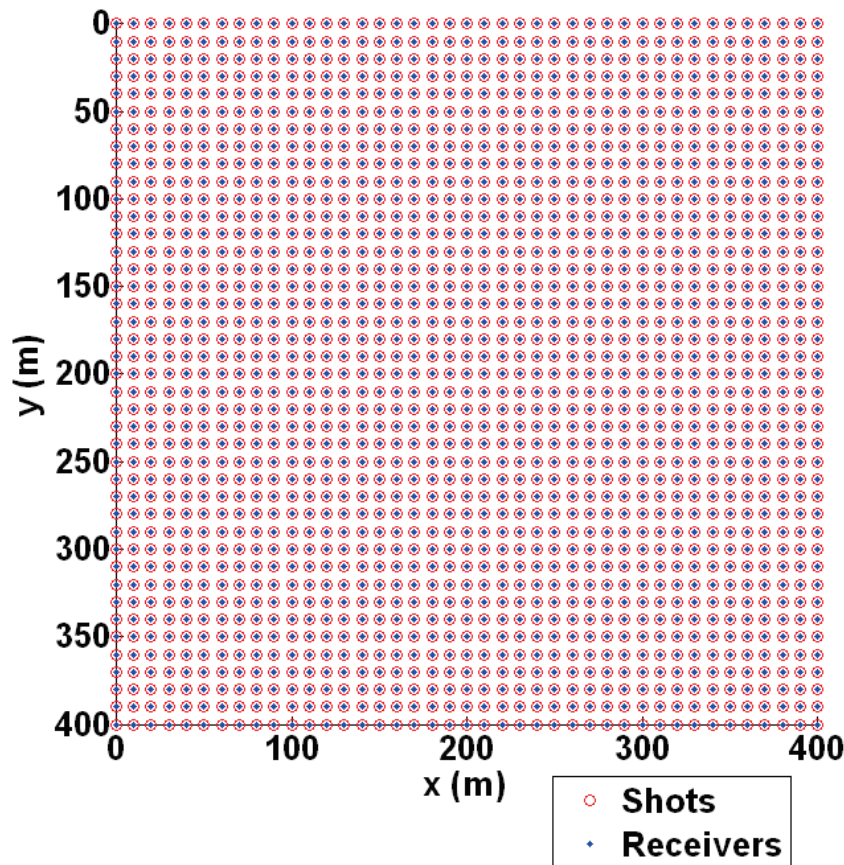




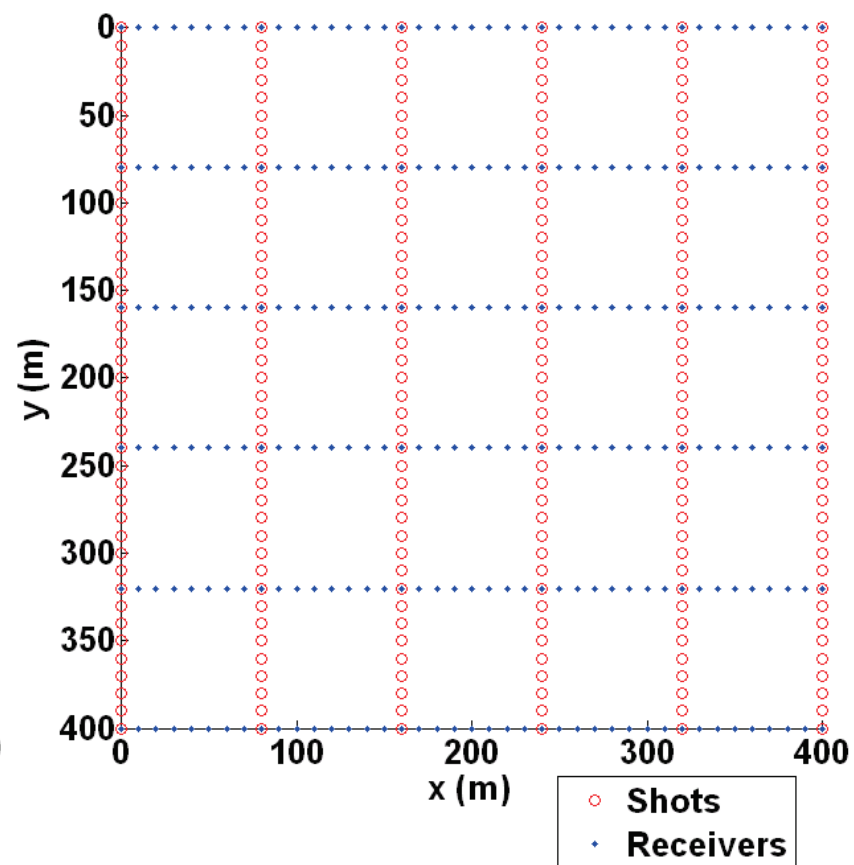
# Recap: 3D Model

## ■ Survey geometries

Exhaustive



Decimated

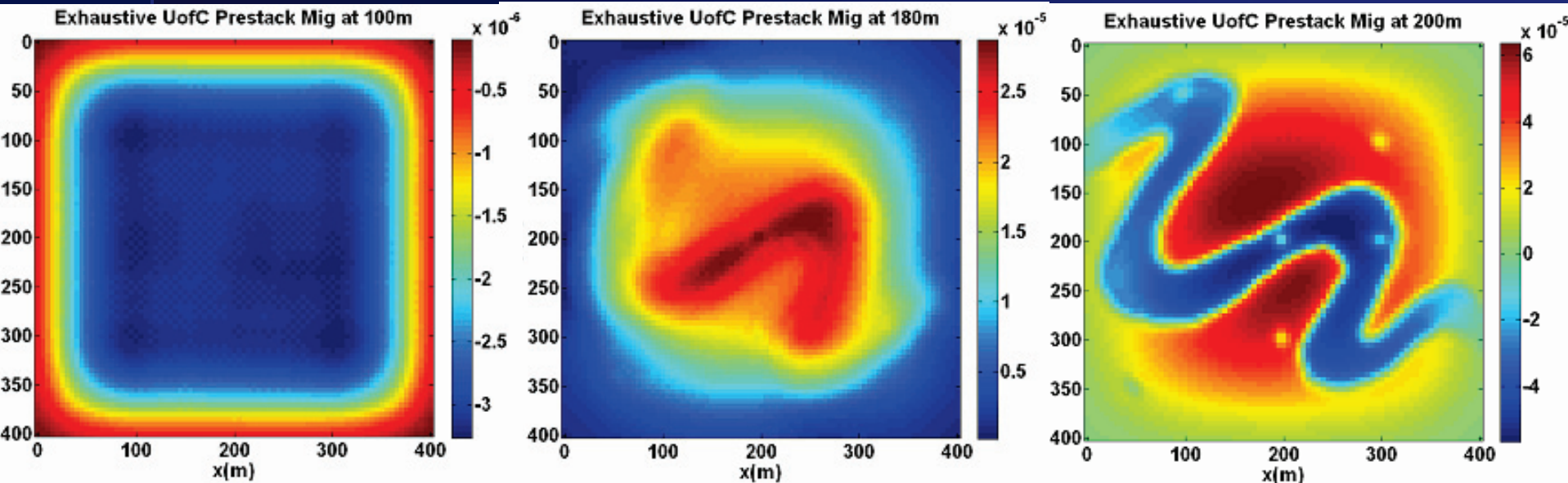


# 3D Results

- Migrations of exhaustive and decimated datasets from previous study (2007)
- Migrations with delta-ratio weights with several choices for azimuth binning
- Migrations with delta-fold weights
- Migrations with common-offset weights
- Comparison of migrations to true reflectivity as percent differences

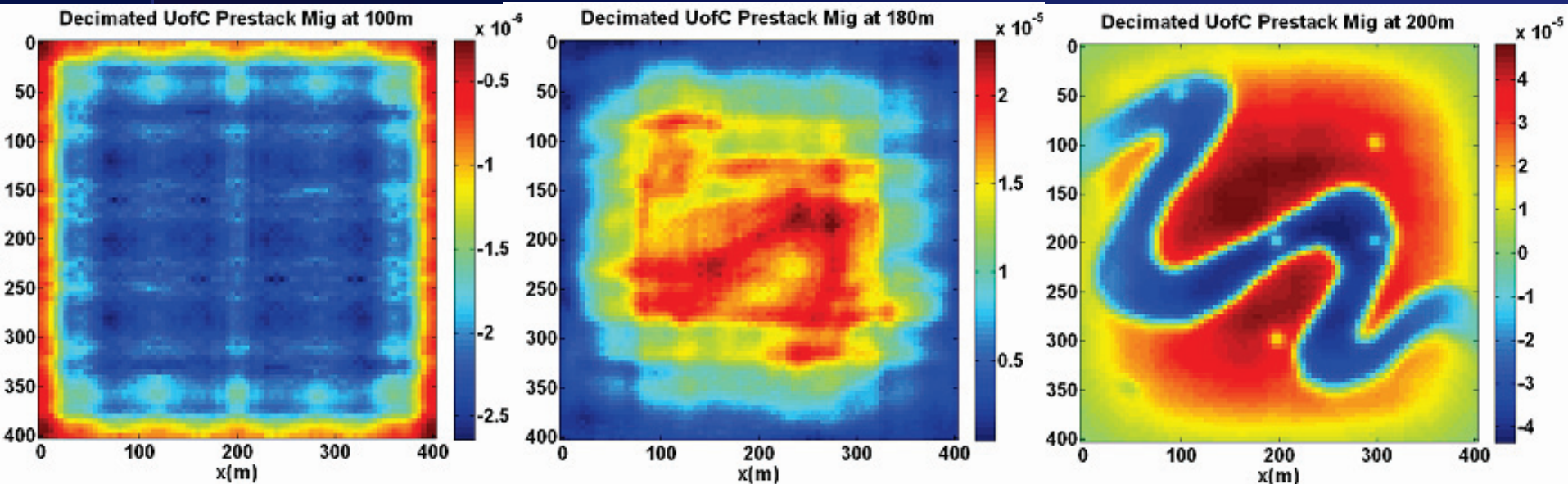
# Recap: 3D Results

- Depth slices from prestack migration of exhaustive dataset



# Recap: 3D Results

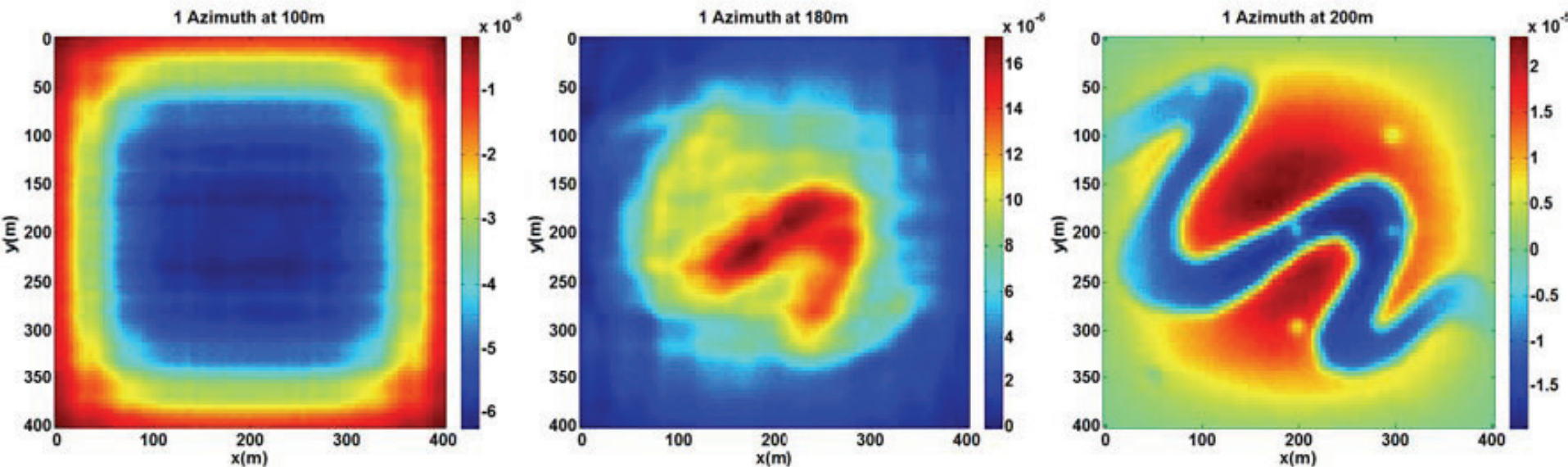
- Depth slices from prestack migration of decimated dataset





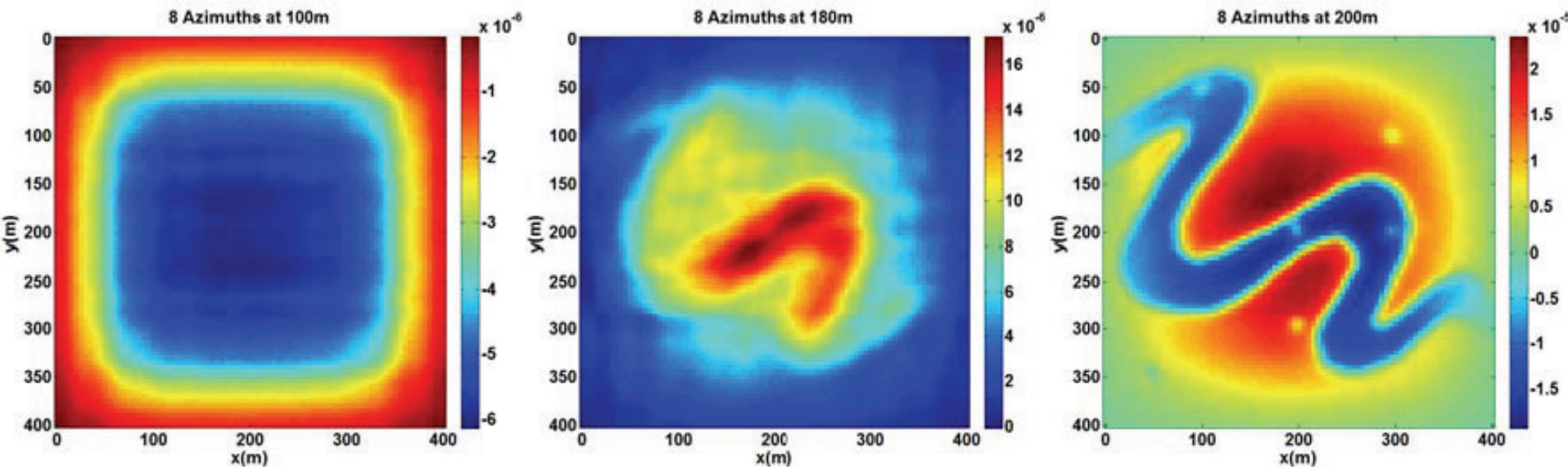
# 3D Results: delta-ratio

- Delta-ratio weights with 5 degree bins in dip and 1 azimuth bin



# 3D Results: delta-ratio

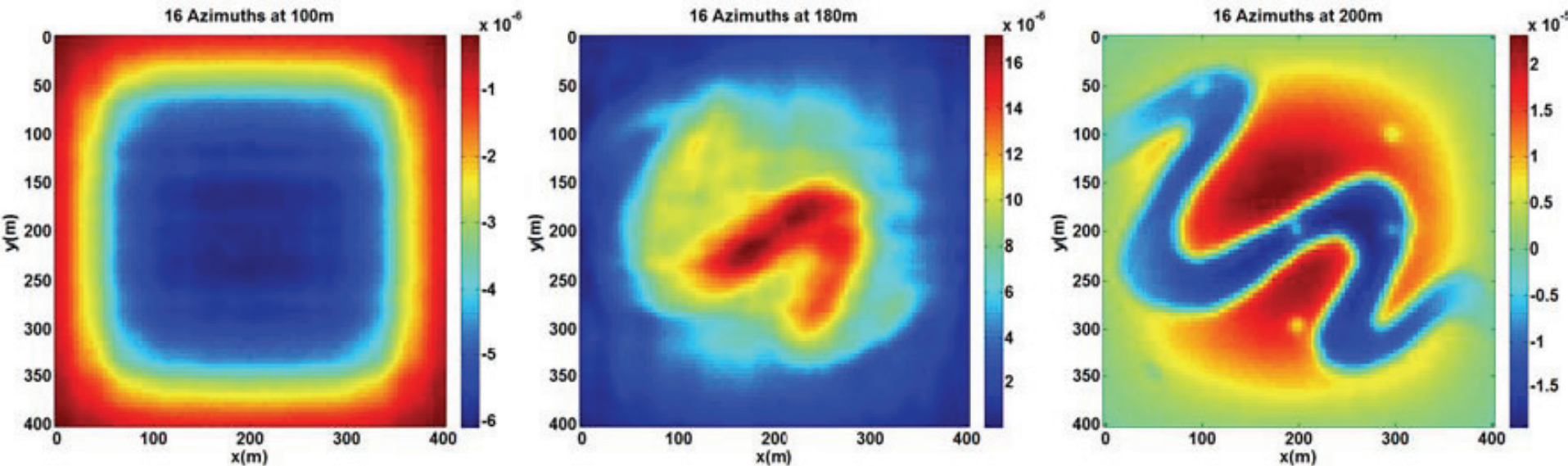
- Delta-ratio weights with 5 degree bins in dip and 8 azimuth bins



– Binning azimuth is important

# 3D Results: delta-ratio

- Delta-ratio weights with 5 degree bins in dip and 16 azimuth bins

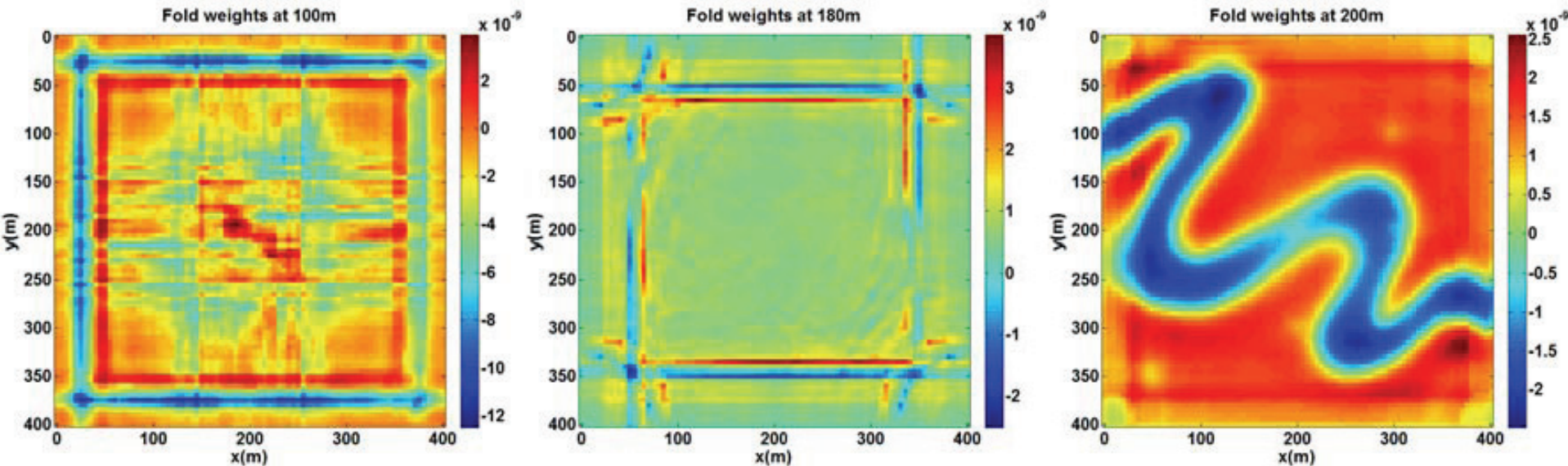


– An optimal bin size/number of bins exists



# 3D Results: delta-fold

- Delta-fold weights with 5 degree bins in dip and 8 azimuth bins



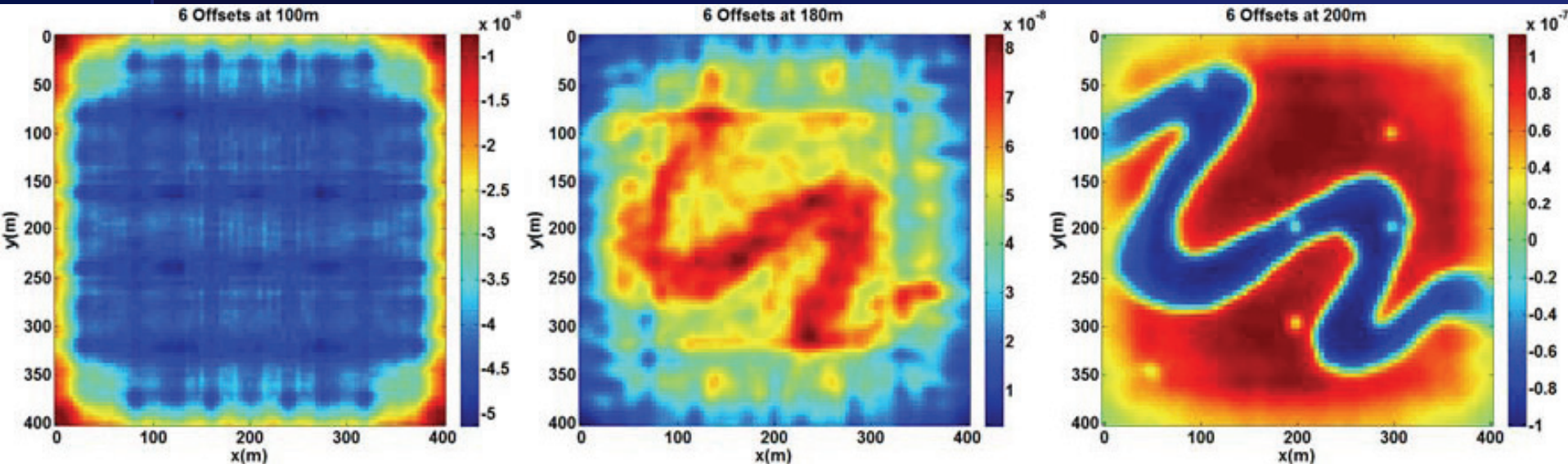


# 3D Results: common-offset

- Recall: common-offset weighting method
- Choose offset bins
- Calculate offset-limited fold
- Pre-weight traces by  $1/\text{fold}$
- Prestack migrate

# 3D Results: common-offset

- Common-offset weights with 100m offset bins

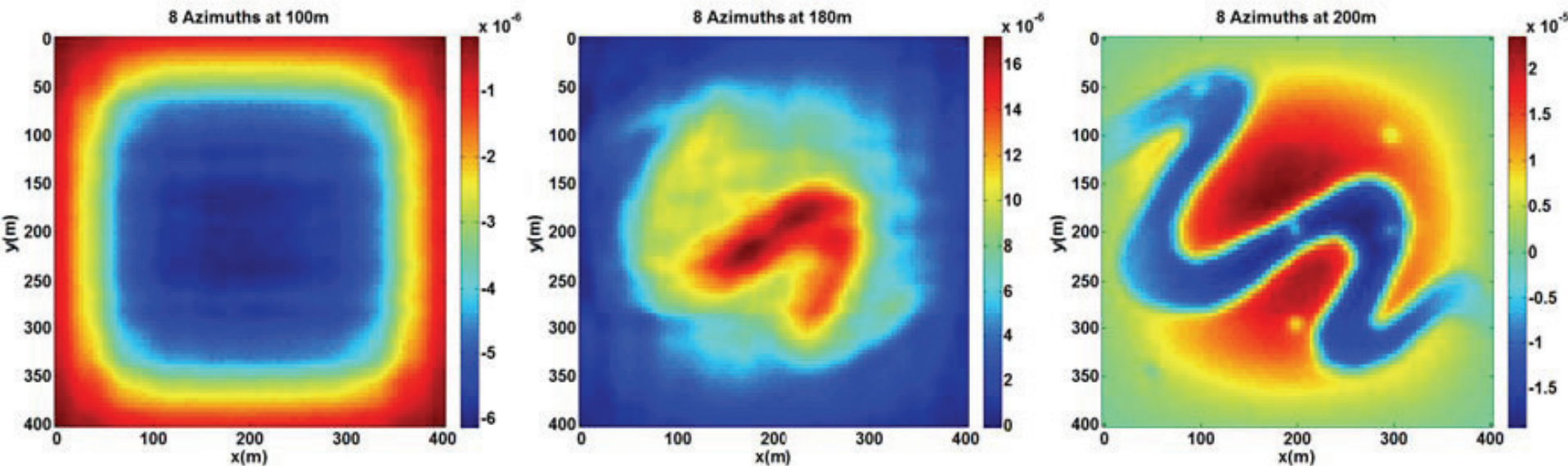


# 3D Results: aperture filter

- Want to quantitatively compare migrated depth slices to the true reflectivity
- Different weighting schemes result in different aperture imprints
- Want to remove these differences to isolate internal footprint artefacts
- Method: smooth slices to estimate aperture, then divide

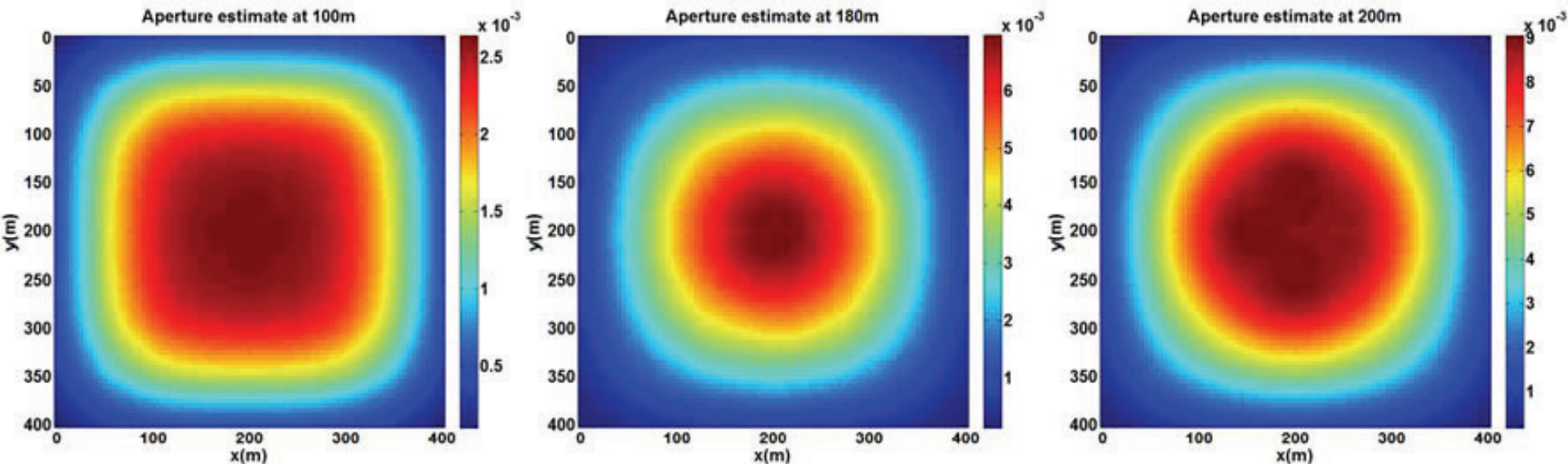
# 3D Results: aperture filter

- Delta-ratio slices with aperture imprint



# 3D Results: aperture filter

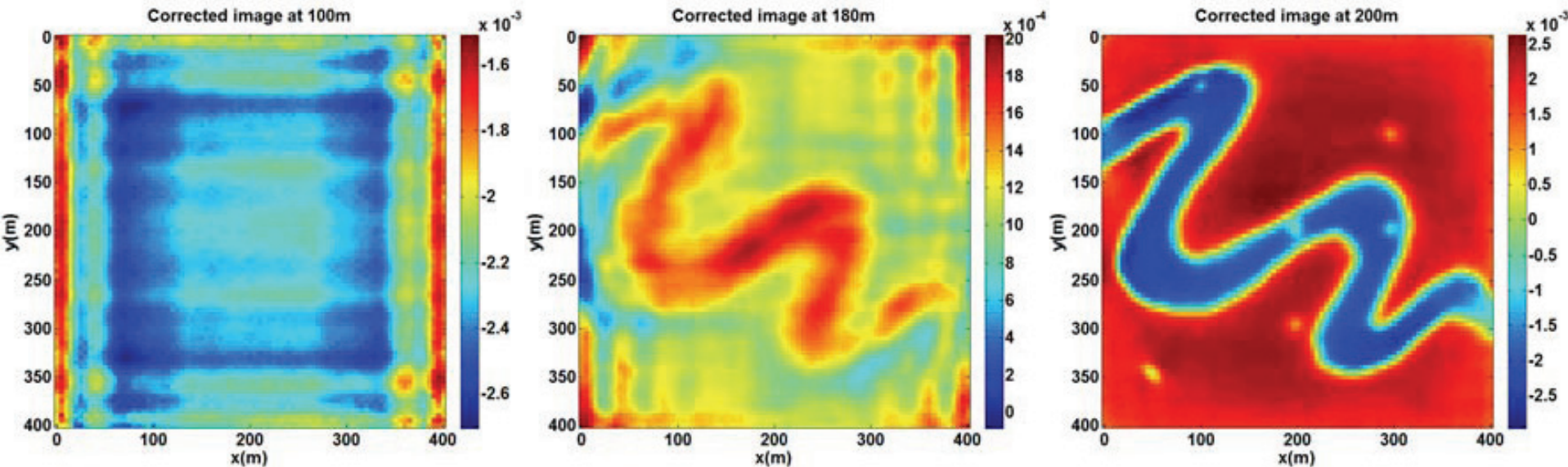
- Aperture estimate





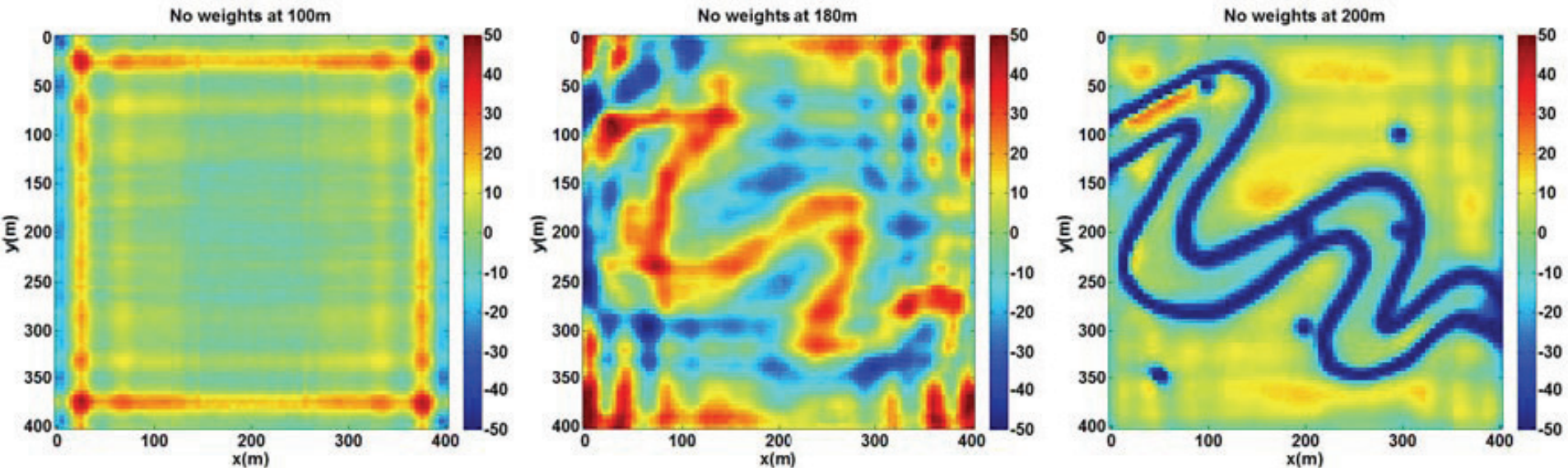
# 3D Results: aperture filter

- Delta-ratio slices after aperture removal



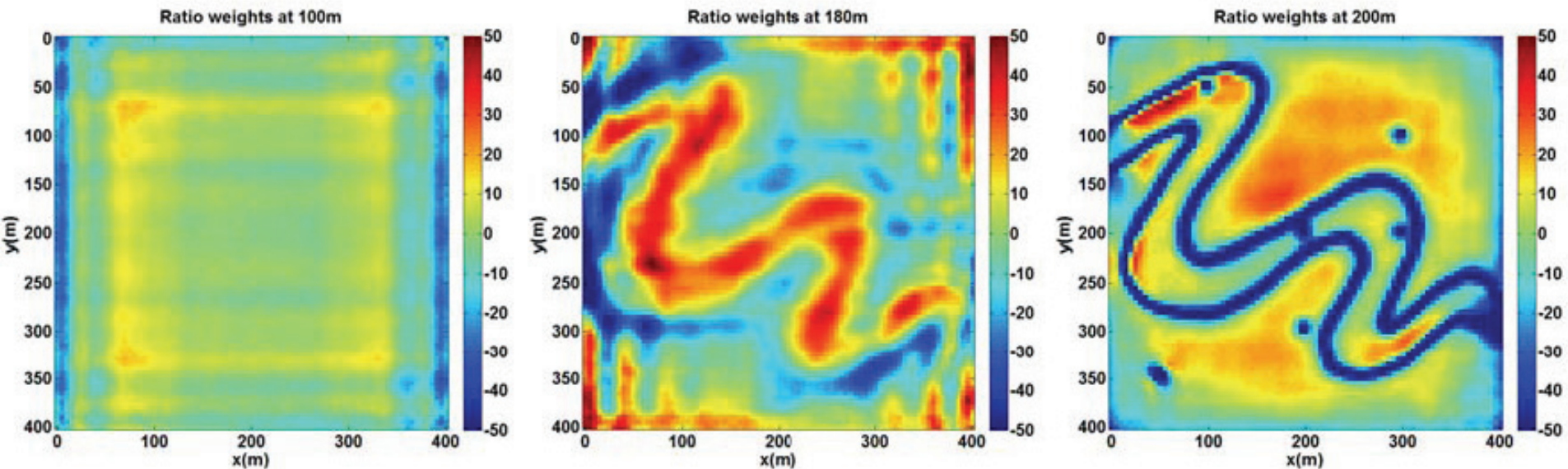
# 3D Results: % difference

- Difference between true reflectivity and unweighted migration



# 3D Results: % difference

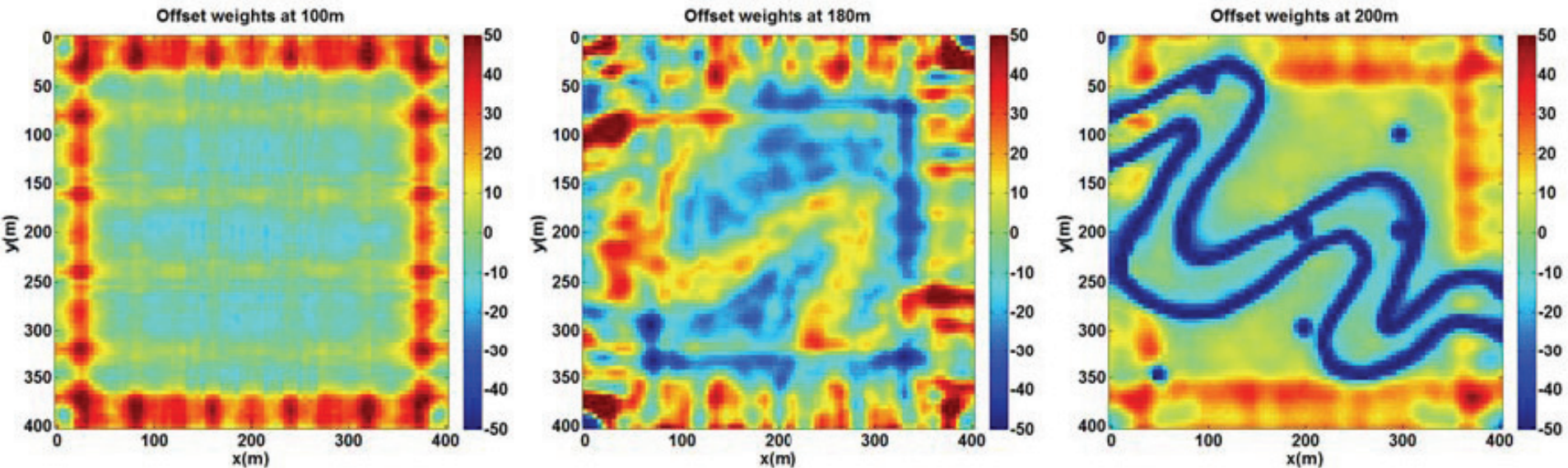
- Difference between true reflectivity and delta-ratio-weighted migration





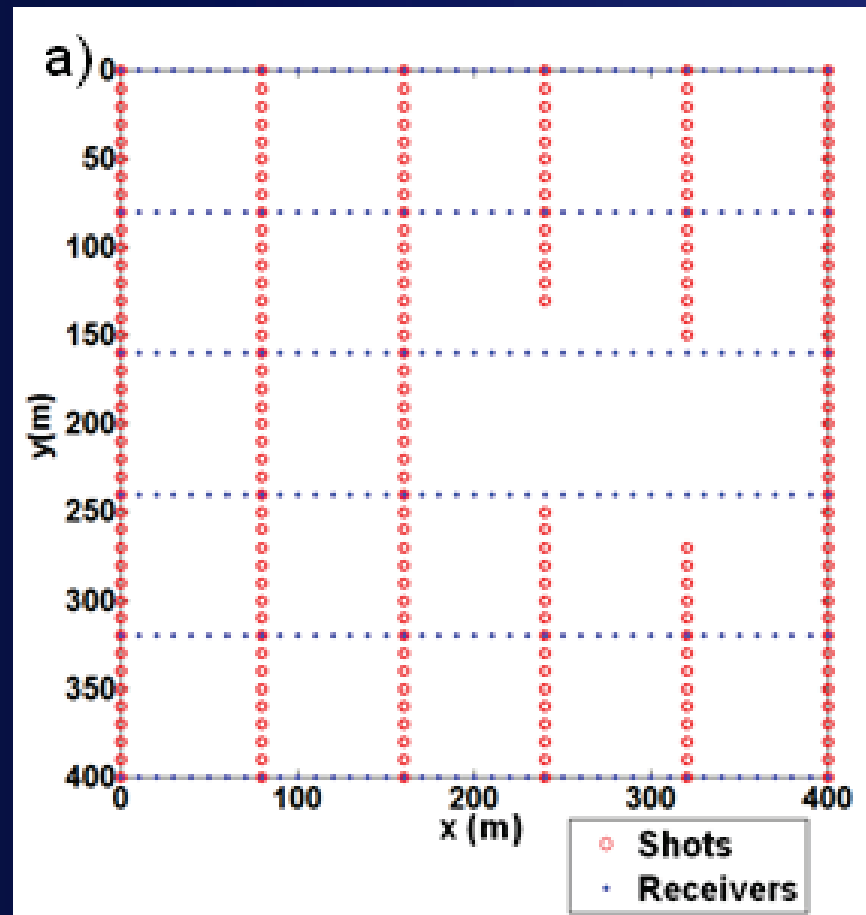
# 3D Results: % difference

- Difference between true reflectivity and common-offset-weighted migration



# 3D Results

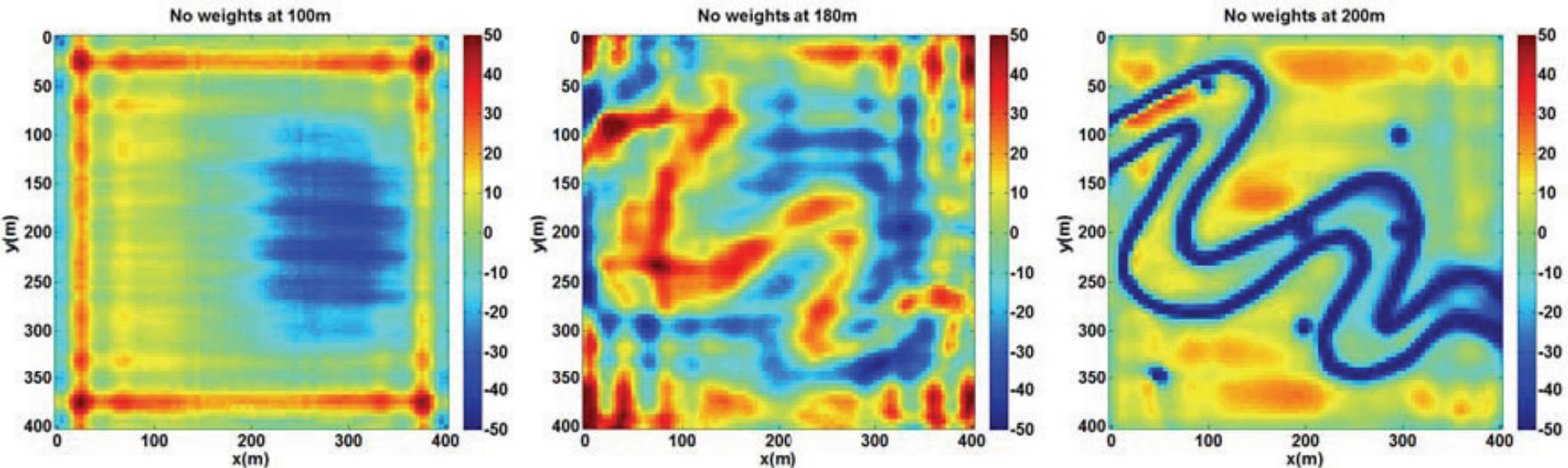
- Additional decimated geometry





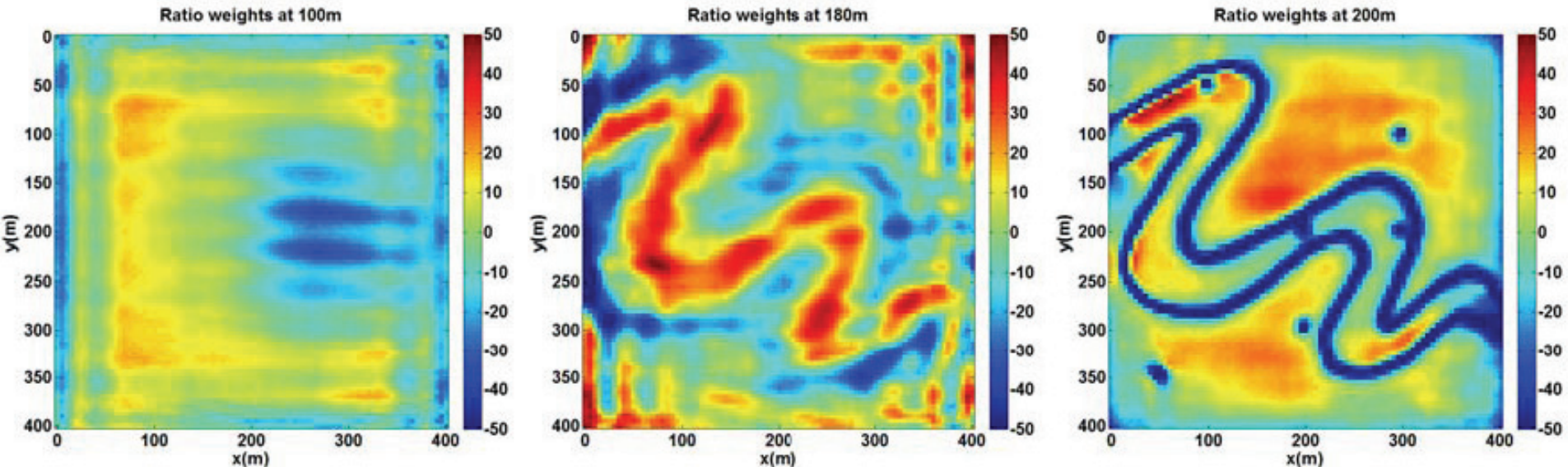
# 3D Results: % difference

- Difference between true reflectivity and unweighted migration with hole



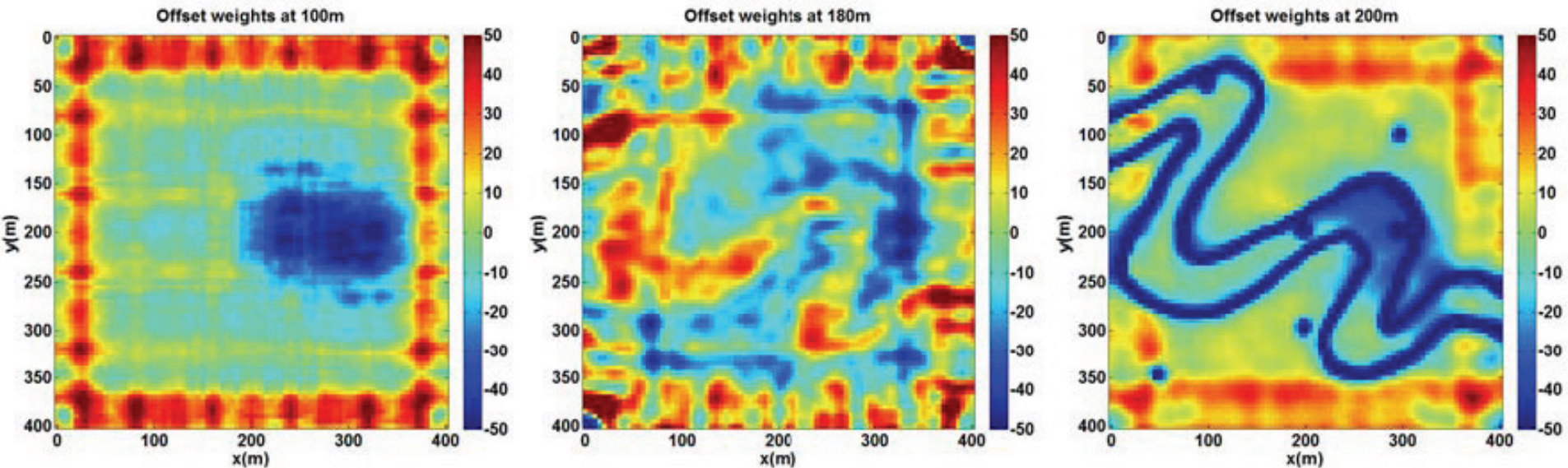
# 3D Results: % difference

- Difference between true reflectivity and delta-ratio migration with hole



# 3D Results: % difference

- Difference between true reflectivity and common-offset migration with hole





# Conclusions

- Though not a replacement for proper sampling, delta-ratio weights appear to reduce footprint in 2D and 3D by compensating for irregular image point illumination
- In a comparison of “bare-bones” algorithms, delta-ratio weights outperformed common-offset weights

# Acknowledgements

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- NSERC
- Alberta Ingenuity

