

Time-lapse attenuation variations during CO₂ injection using DAS VSP data from the CaMI.FRS

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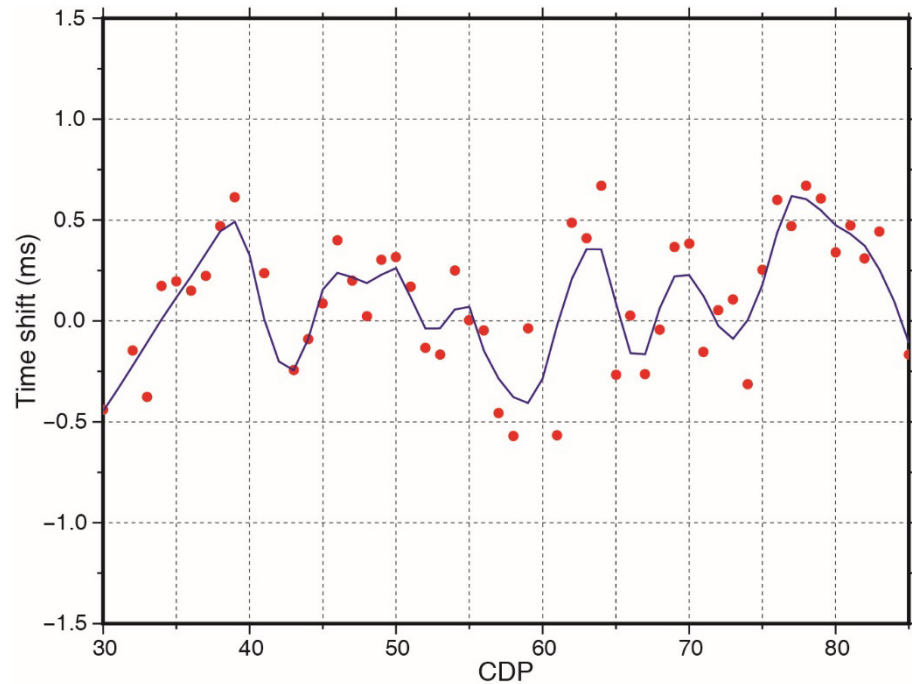
Carbon
Management
Canada



- DAS VSP survey and data processing
- Time-lapse attenuation measurements
- Accuracy and resolution of estimated attenuation
- Discussion
- Conclusions



Motivation

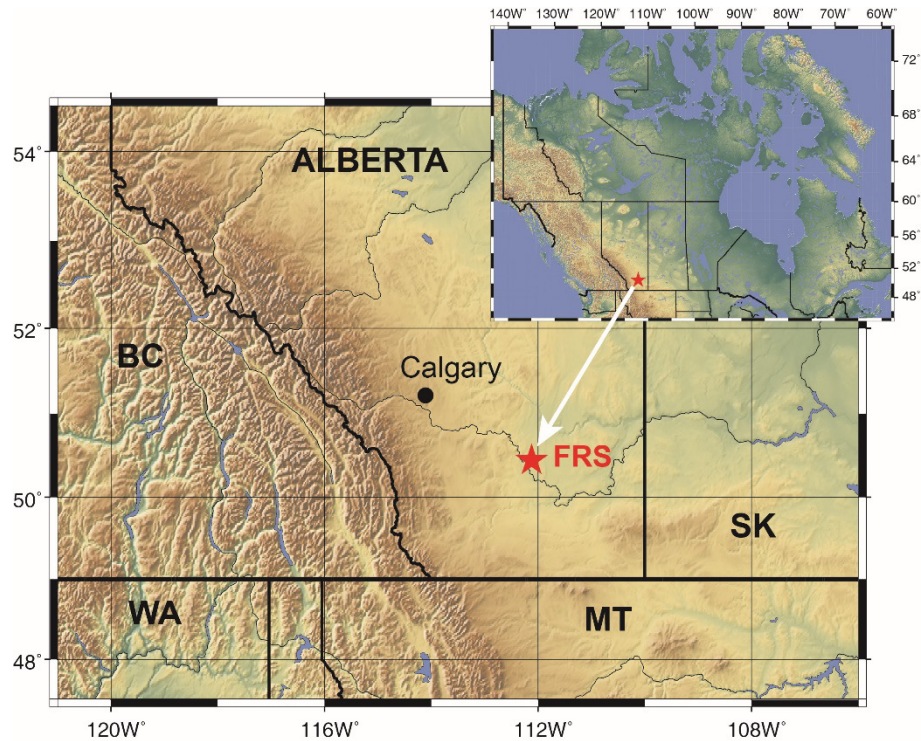


Time shifts along the first reflection horizon below CO₂ injection zone

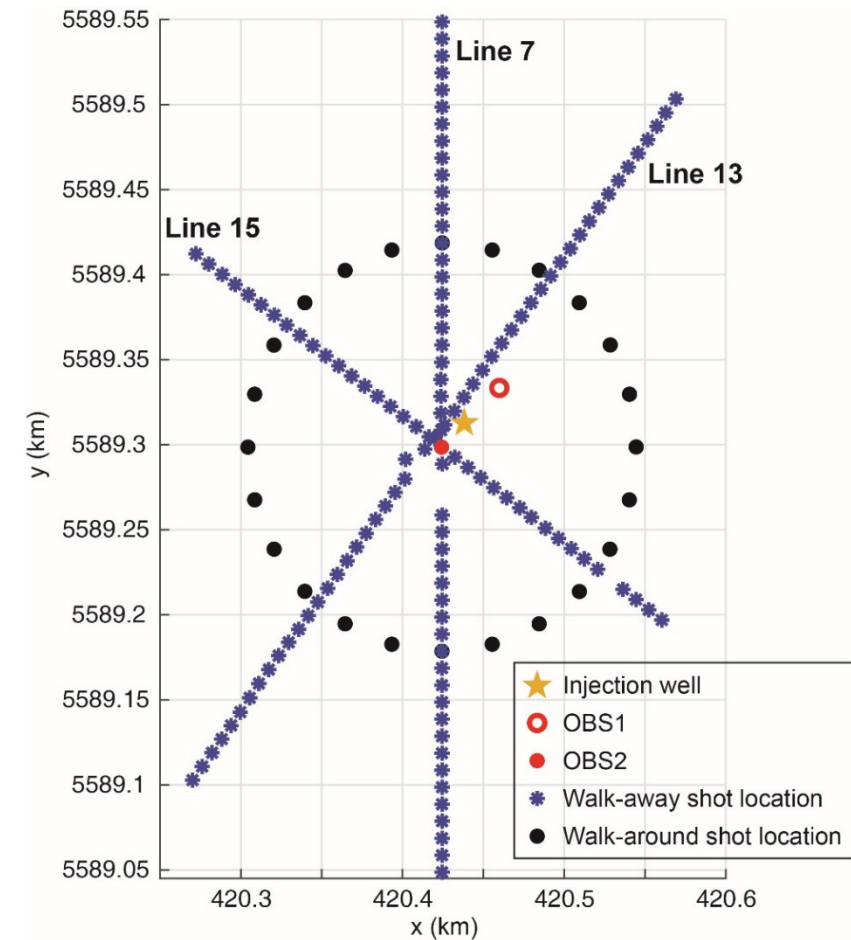
- Injection zone at the FRS is thin (~7 m)
- Injected CO₂ may cause a decrease in P-wave velocity of only a few percent
- Such a decrease is near the seismic noise level for detection
- S/N of VSP data obtained through DAS fiber cable is generally lower than that from geophone
- Compared with velocity or density variations, attenuation is more sensitive to changes in saturation, permeability, and pore fluid



DAS VSP layout



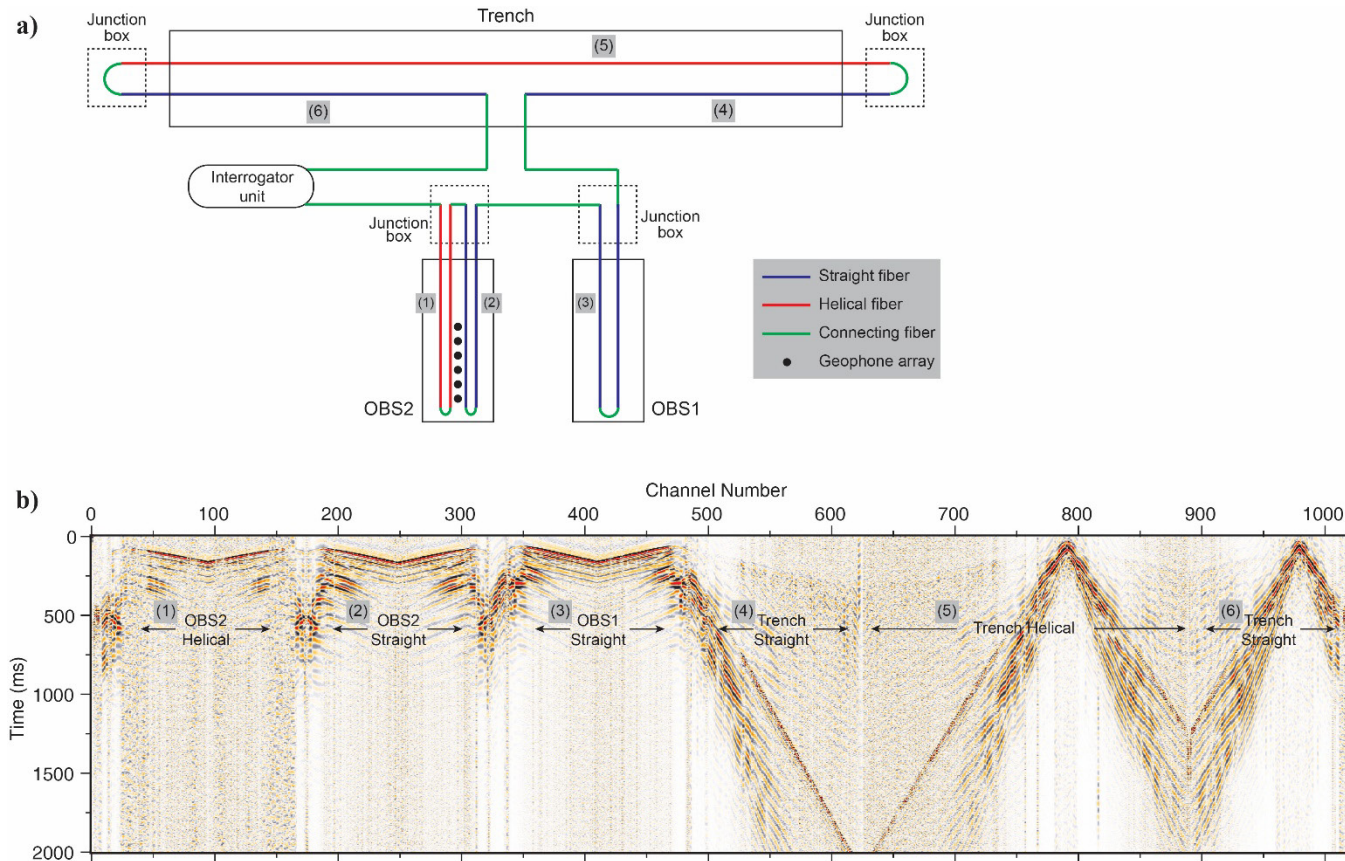
Location map of CaMI FRS in southern Alberta, Canada



- Monitor survey acquired in March 2021
- ~34 tonnes of CO₂ injected prior to this date



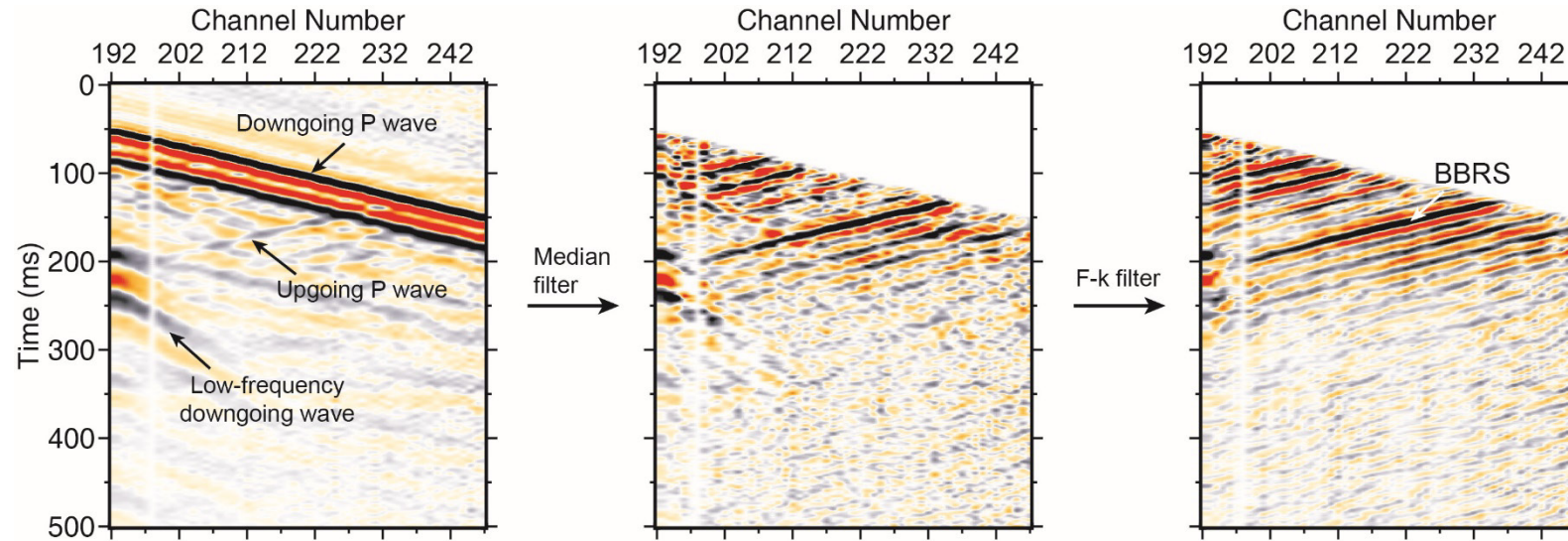
Fiber layout and data



- Continuous fiber loop (5km) and raw DAS shot gather
- Tag numbers indicate the corresponding data from different portions of fiber loop
- DAS data from the straight fiber in OBS2
- Identical data processing for different vintages of DAS data



Wavefield separation



- Construct attenuation-attribute images from reflection signal for monitoring injected CO₂
- Separate downgoing and upgoing wavefields through a median filter followed by a f-k filter
- Upgoing P-wave reflections are clearly isolated and evident over the entire depth coverage

1) Non-stationary convolutional model for reflection signal:

$$A(t, f) = S(f) R(t, f) F(t, f) G(t)$$

- A : time-frequency variant amplitude of reflection signal
- S : spectrum of seismic source
- R : time-frequency response of reflectivity
- F : seismic attenuation $F(t, f) = \exp\left[-\pi f \int_0^t d\tau / Q(\tau)\right]$ (anelastic)
- G : focusing or defocusing $G(t) = \exp\left[-\int_0^t \gamma(\tau) d\tau\right]$ (elastic)

2) Take logarithm and time derivative:

$$\gamma + \pi f Q^{-1} = \frac{\partial}{\partial t} [\ln R(t, f) - \ln A(t, f)]$$

- γ is a “geometric” counterpart for Q^{-1}

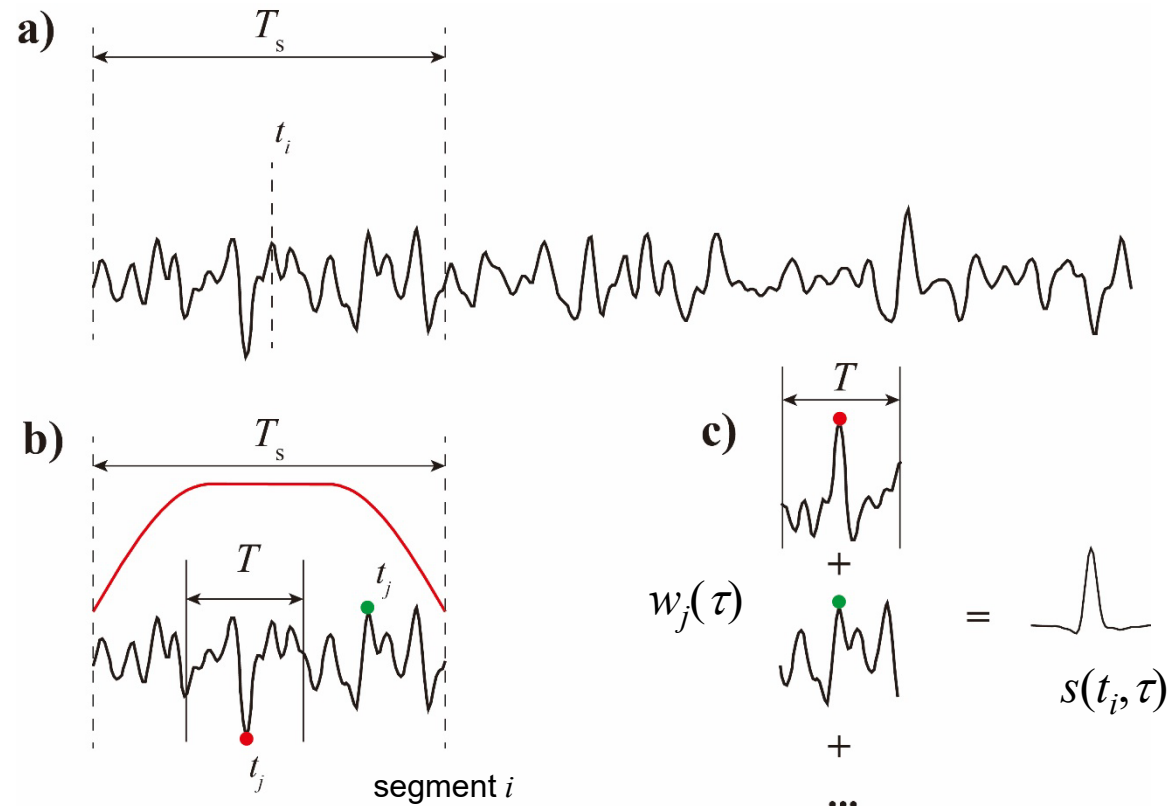
3) Under the assumption $R(t, f) = \text{const}$:

$$\gamma_A + \pi f Q_A^{-1} = -\frac{\partial \ln A(t, f)}{\partial t}$$

- γ_A and Q_A are the “apparent” attenuation
- Require smooth estimates of $A(t, f)$



Time-variant spectra



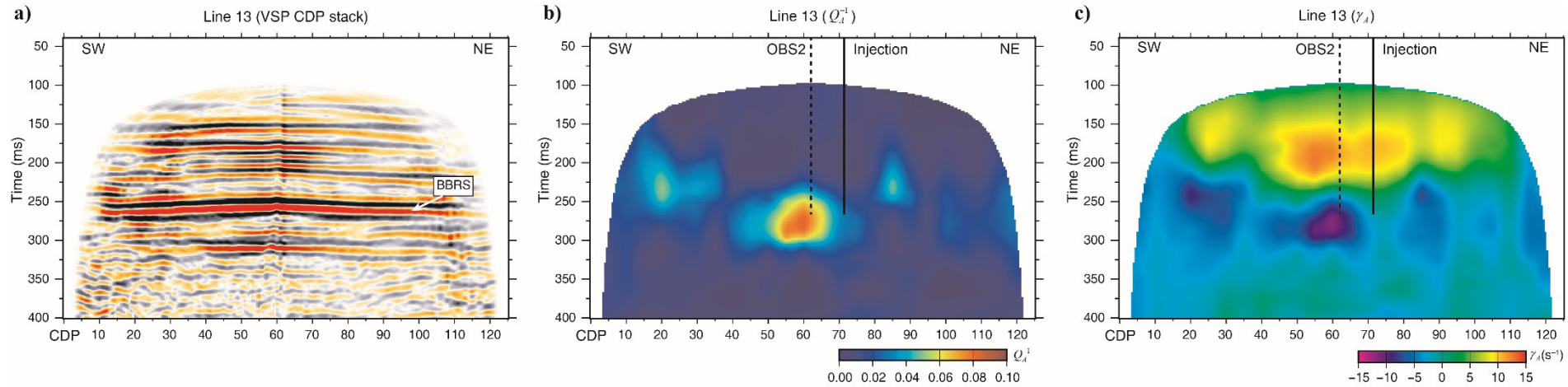
$$s(t_i, \tau) = c_0 \sum_{j \in \text{segment } i} h\left(\frac{t_j - t_i}{T_s}\right) w_j(\tau)$$

- c_0 scales peak amplitude equal to $s(t_i, \tau) = 1$
- Hann window h of the same length T_s with segment i
 - Apply weights to $w_j(\tau)$ located within different parts centered on t_j of each peak
 - Located at the middle of segment has the maximum weight and at the edge has a zero weight
- Temporal resolution of the resulting spectra can be estimated as the half segment length $T_s/2$

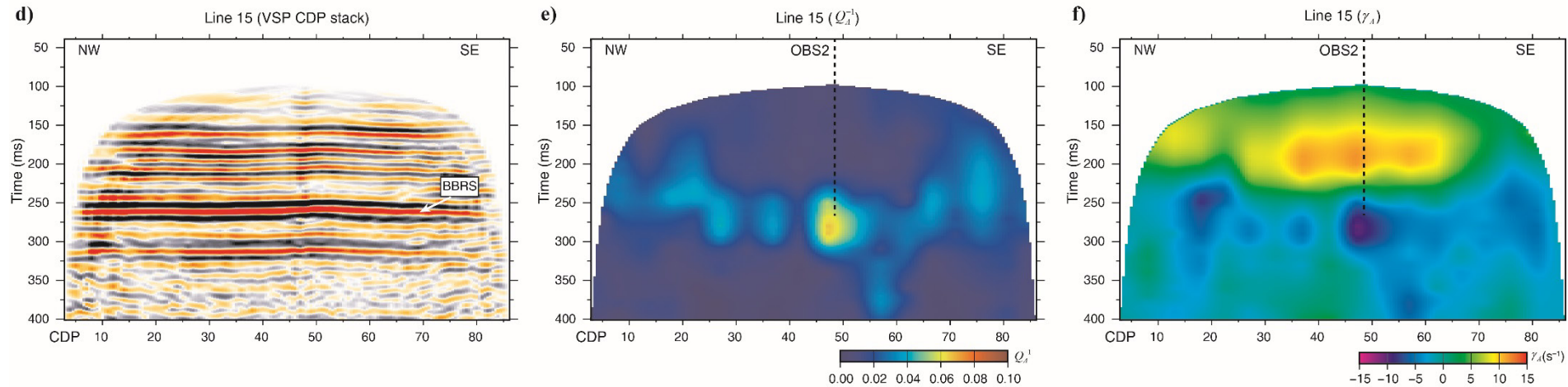


Attenuation measurements from monitor data

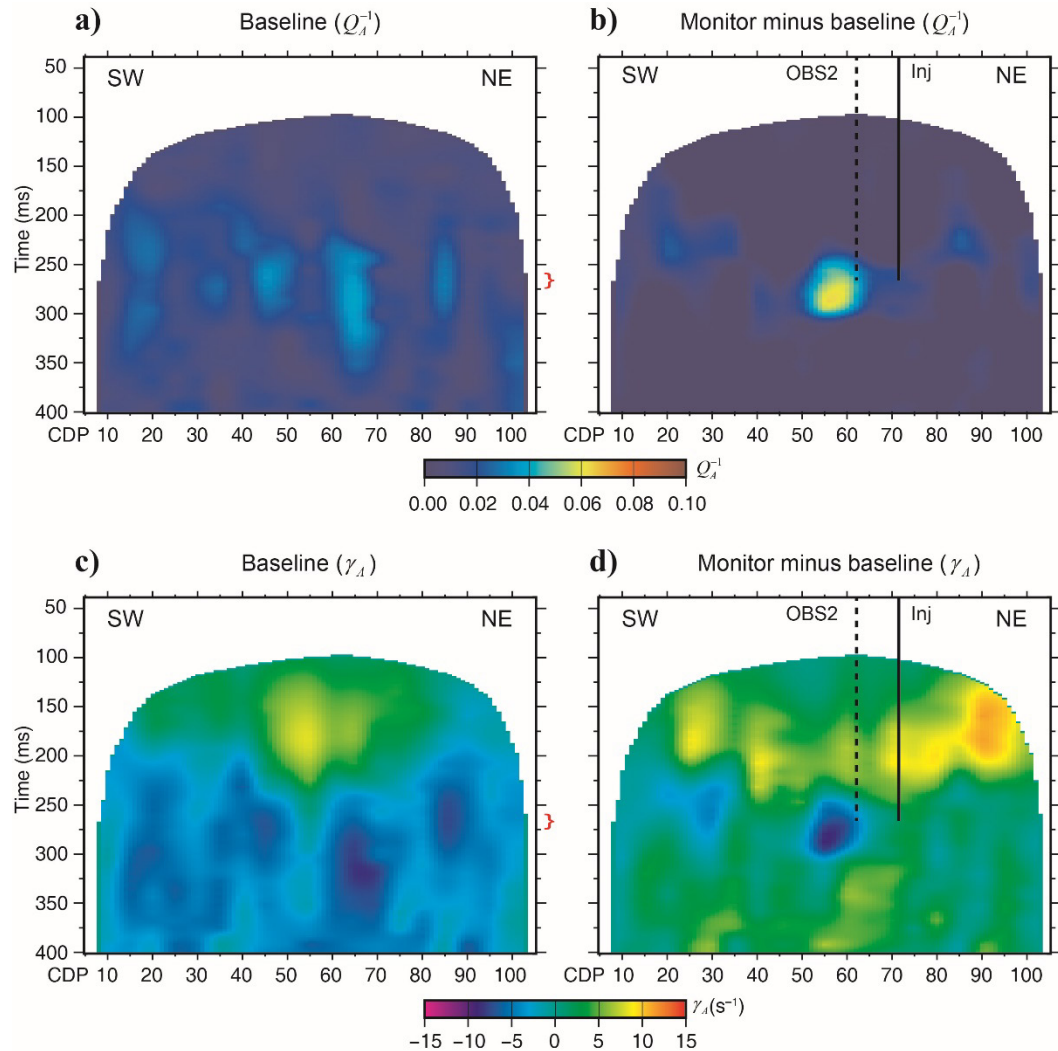
Line 13



Line 15



- Large γ_A and Q_A^{-1} around OBS2 at the BBRs injection zone
- Increased CO_2 saturation and/or pore pressure
- Consistent γ_A and Q_A^{-1} around OBS2 from two different lines



- Measurements from baseline data show there is no anomaly prior to CO_2 injection
- Time-lapse responses show a clear increase to the SW of OBS2
- Attenuation increase not around the injection well indicates the migration of injected CO_2
- From liquid phase around the injection well to gas phase at the leading edge of the plume



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$$a_k = \gamma + \pi(f_k - \bar{f})Q^{-1}$$

Empirical error

Errors for regression coefficients (Q^{-1} and γ) are

$$s_{\hat{\gamma}} = \frac{\sigma_{\hat{a}}}{\sqrt{n}} \quad (\text{intercept})$$

$$s_{\hat{Q}^{-1}} = \frac{\sigma_{\hat{a}}}{\pi \sqrt{\sum (f_k - \bar{f})^2}} = \frac{s_{\hat{\gamma}}}{\pi \langle f_k - \bar{f} \rangle_{RMS}} \quad (\text{slope})$$

- $\langle \dots \rangle_{RMS}$: RMS average
- $\sigma_{\hat{a}}^2$: variance of the estimated spectral quantity

Theoretical error

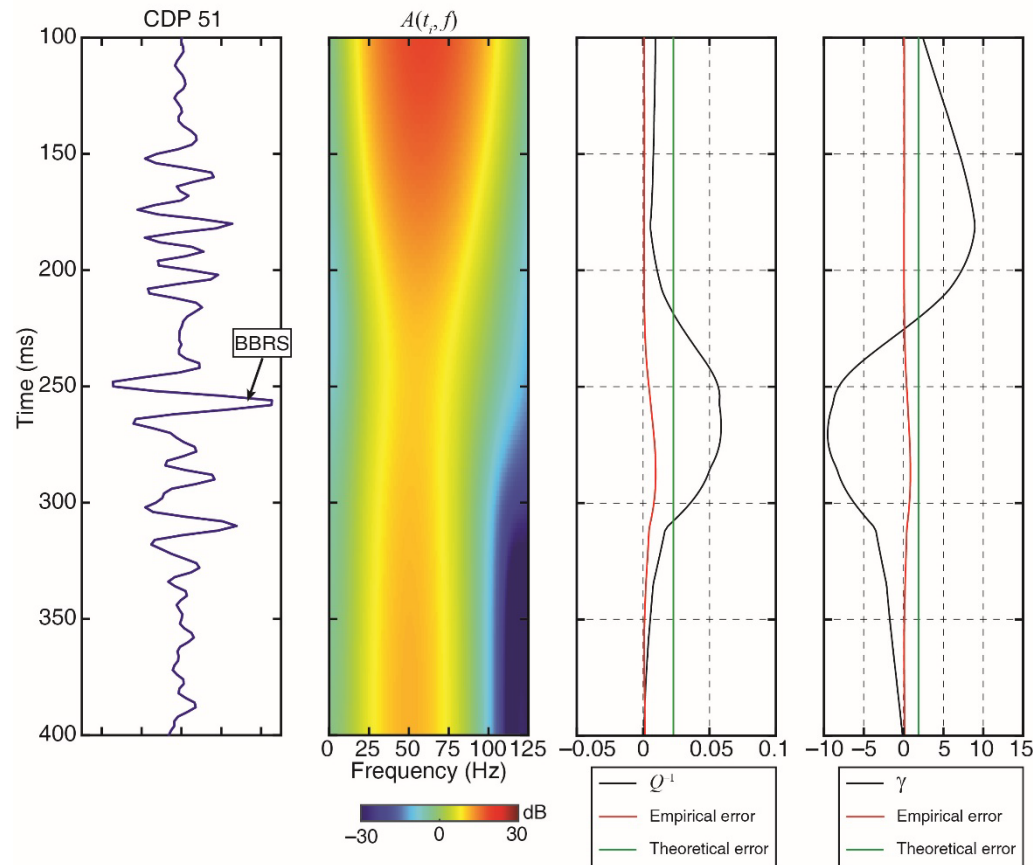
$$s_{\hat{\gamma}} = \frac{1}{\sqrt{2\Delta t}} \frac{1}{\sqrt{BT}}$$

$$s_{\hat{Q}^{-1}} = \frac{s_{\hat{\gamma}}}{\pi c B} = \frac{1}{\pi \sqrt{2c}} \frac{1}{\sqrt{BT}} \frac{1}{B\Delta t}$$

- B : signal frequency bandwidth
- T : waveform length in spectral measurement
- Δt : temporal resolution
- Independent of γ or Q^{-1} value
- Key parameter is the desired temporal resolution Δt



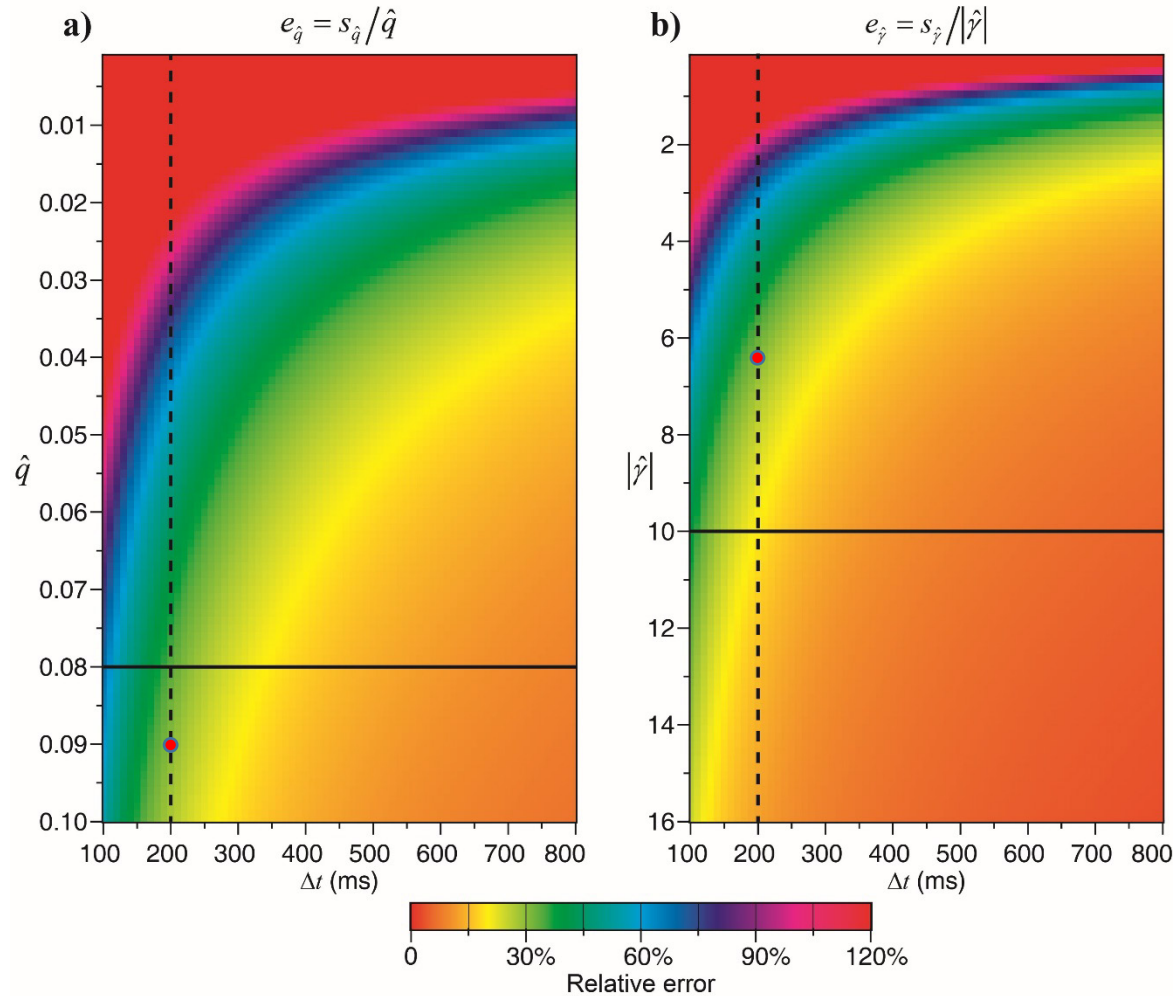
Measurement errors



- Resolution of $\Delta t = 200$ ms
- Q^{-1} is below theoretical error (green line) for most depths above and below the BBRS
- Limited accuracy of Q^{-1} for areas outside of injection zone
- Around the BBRS that is with high attenuation, Q^{-1} is much larger than error
- Accuracy of γ is higher with the theoretical error smaller than γ for all the depths



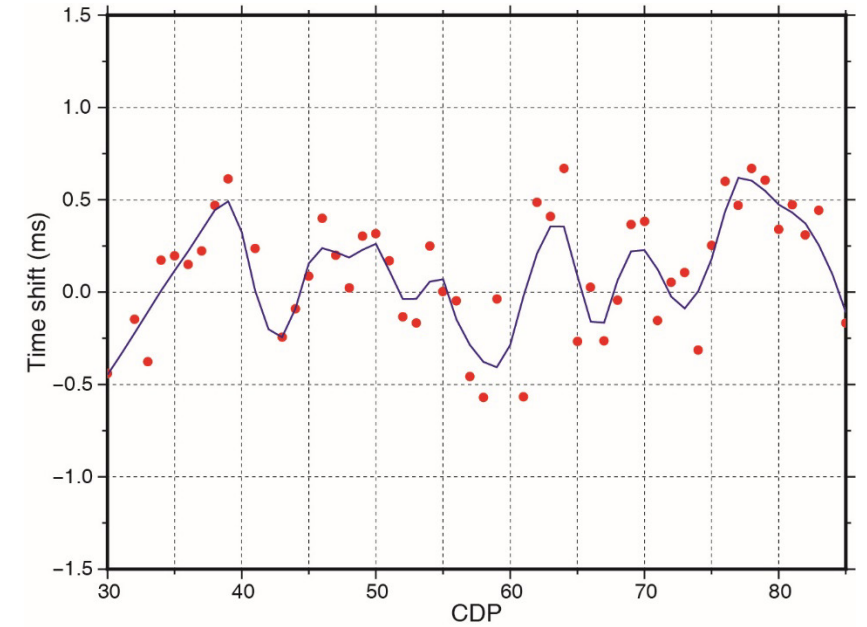
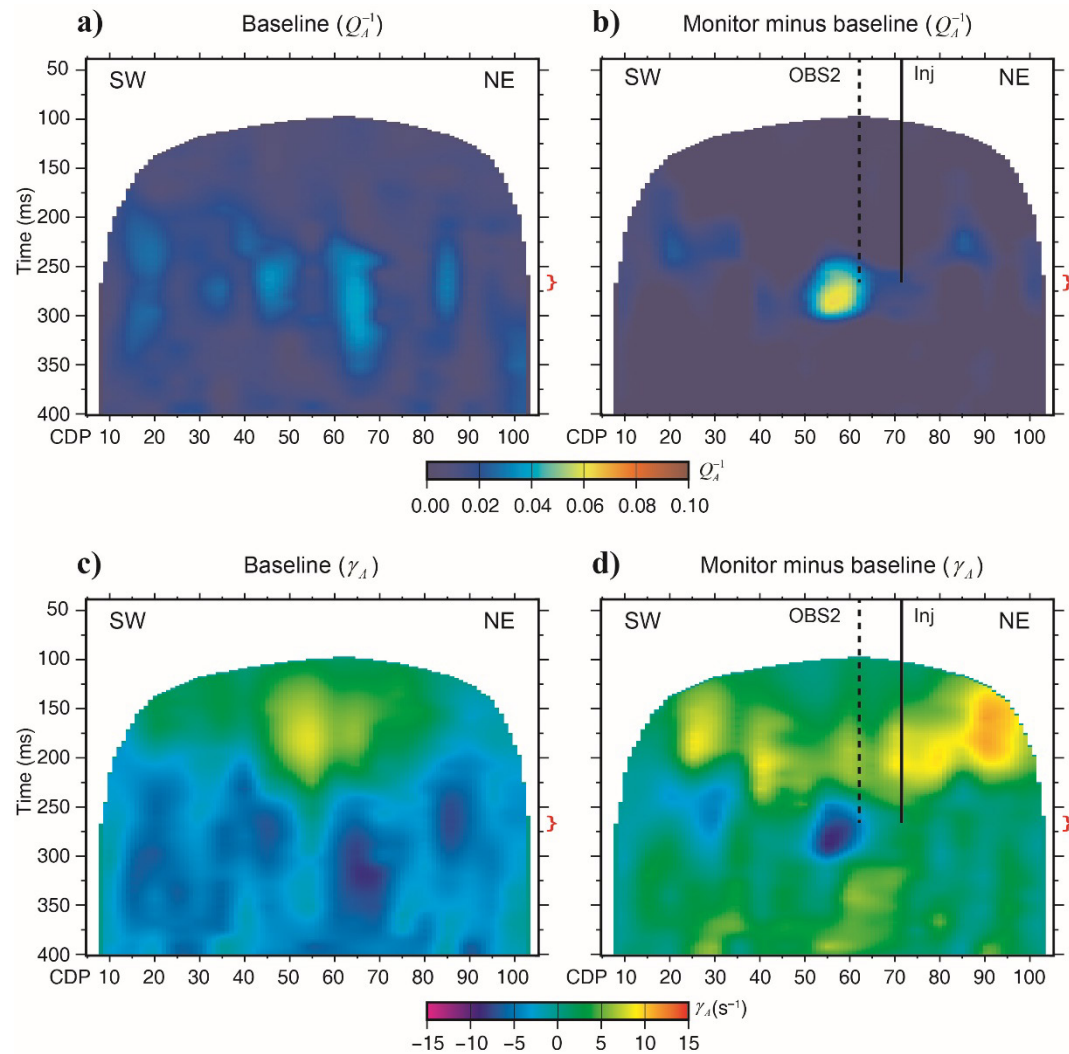
Relative errors



- Black dashed line: resolution of $\Delta t = 200$ ms
- Black solid line: a) estimated Q^{-1} of 0.08; b) estimated γ of 10 s^{-1}
- Significant trade-off between accuracy of estimated Q^{-1} or γ and temporal resolution
- $Q^{-1} > 0.09$ and $|\gamma| > 6.5 \text{ s}^{-1}$ for achieving an error lower than 30%
- Around the BBRS injection zone, relative errors are modest $e_{\hat{Q}^{-1}} \approx 34\%$ and $e_{\hat{\gamma}} \approx 20\%$



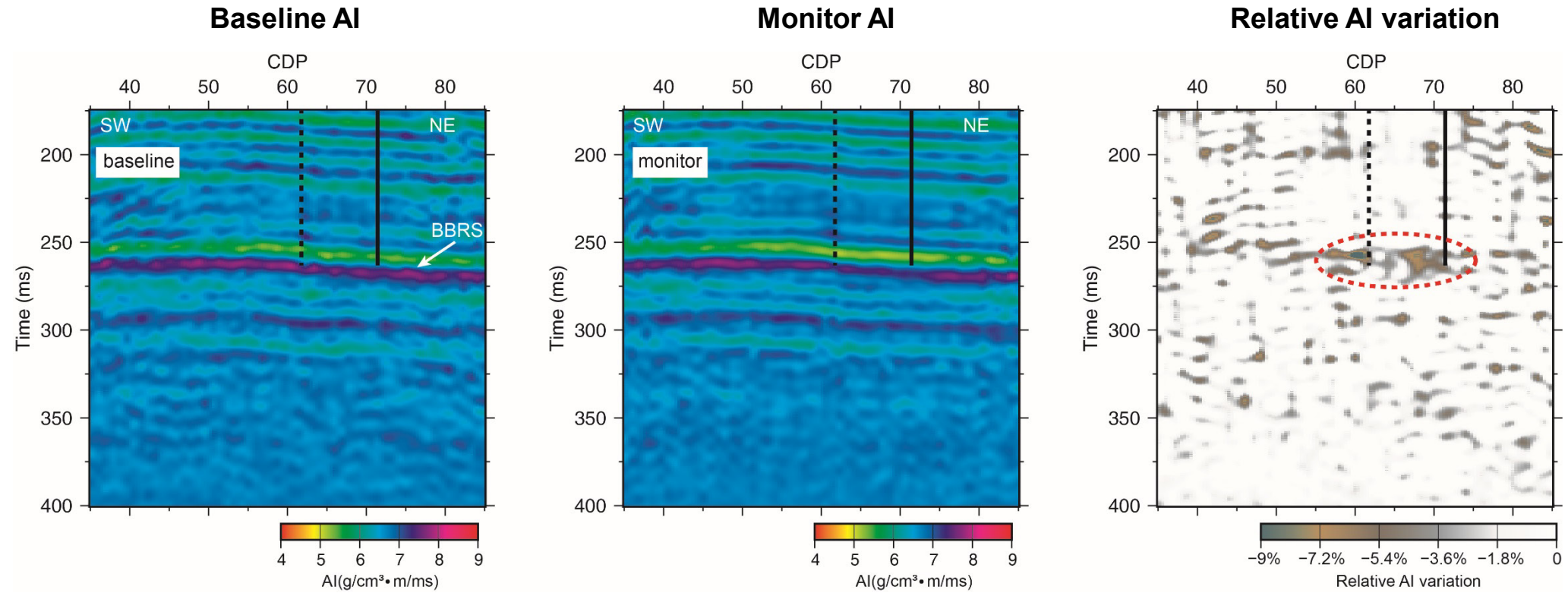
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Time shifts along the first reflection horizon below injection zone



Comparison with impedance variations





- Both Q^{-1} and its geometric counterpart γ are measured from the DAS VSP data for monitoring the CO₂ injection.
- The variations of Q^{-1} or γ are correlated with injection zone and interpreted as being caused by an increase in CO₂ saturation.
- Evaluations of measurement accuracy show the measured Q^{-1} or γ of large values around the injection zone are reliable.
- Attenuation is a sensitive property that can complement velocity change for monitoring injected CO₂ during geologic CO₂ storage.



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