Predicting Heavy Oil Viscosity from Well Logs

September 25th CREWES Tech Talk
By: Eric Rops
Presentation Outline

1. Introduction to Heavy Oil and Viscosity
2. Theory of Multi-attribute Analysis
3. Overview of the study wells
4. Viscosity Prediction Results
5. Conclusions
6. Future Work
Introduction – Heavy Oil
Conventional Heavy
Extra Heavy
Molasses
Maple Syrup
Olive Oil
Cream
Water

Image Credit: ConocoPhillips Oil Sands website
Why do we Care About Viscosity?

• “Viscosity is the key controlling heavy-oil production and, as we shall see, it also has a strong influence on seismic properties.” (Han & Liu & Batzle, 2008)
• It is used as a main criterion in determining the optimum recovery method.
Shear Properties of Heavy Oil (Lab Measurements)

- Because of its high viscosity, heavy oil has a non-negligible shear modulus.
- Figure shows sharp shear arrival in a very heavy oil sample (API -5).

Batzle & Hofmann & Han (2006)
Lab Measurements of Heavy Oil - Rock

- **Gassmann Equation not valid below a certain temperature once the viscosity starts getting high**

  [Graph showing velocity versus temperature for different properties (Vp, Vs, Gassmann Vp, Gassmann Vs) with a core plug sample]

  *Kato & Onozuka & Nakayama (2008)*
Shear Modulus and Attenuation Lab Measurements

- Dynamic behavior of shear modulus and attenuation with temperature. (Measured at 12.6 Hz)

Behura et al. (2007)
Estimating Viscosity from Crosswell Seismic Data

• Attenuation tomography used to extract Q, then related Q to viscosity using Biot Squirt Theory

Vasheghani & Lines (2012)
Goal of this Study

• 13 wells acquired from the Athabasca region of northern Alberta
• Each well had viscosity measurements, and dipole sonic logs

• Can we train a relationship between viscosity and the well log data in only some of the wells, and then successfully predict the viscosity in the remaining wells?
Theory of Multi-Attribute Analysis
Multi-Attribute Analysis

- At each time sample, the target log is modeled as a linear combination of several attributes.
- “Attribute” and “Well log curve” mean the same thing.
Example: Predicting P-wave velocity with 3 Attributes

\[ V_p(z) = w_0 + w_1 D(z) + w_2 G(z) + w_3 R(z) \]

where:
- \( V_p(z) \) = P-wave velocity (m/s)
- \( D(z) \) = Bulk density (kg/m\(^3\))
- \( G(z) \) = Gamma ray (API units)
- \( R(z) \) = Resistivity (Ohm\(\cdot\)m)

Or in matrix form:

\[
\begin{bmatrix}
V_{p1} \\
V_{p2} \\
\vdots \\
V_{pN}
\end{bmatrix} =
\begin{bmatrix}
1 & D_1 & G_1 & R_1 \\
1 & D_2 & G_2 & R_2 \\
\vdots & \vdots & \vdots & \vdots \\
1 & D_N & G_N & R_N
\end{bmatrix}
\begin{bmatrix}
w_0 \\
w_1 \\
w_2 \\
w_3
\end{bmatrix}
\]

Or more compactly as:

\[ V_p = A W \]

The regression coefficients can be solved for using least-squares:

\[ W = (A^T A)^{-1} A^T V_p \]
What are the best Attributes to use?

Goal is to minimize the prediction error:

\[ PE = \sqrt{\frac{\sum_{i=1}^{N} (V_{pTrue,i} - V_{pPredicted,i})^2}{N}} \]

Step-wise regression:

1. Find the **single** best attribute
2. Find the best **pair** of attributes
3. Find the best **triplet** of attributes
4. Carry on as long as desired
When do we Stop Adding Attributes? (why would we want to stop?)

- Adding attributes is similar to fitting a curve through a set of points, using a polynomial of increasing order.
- A higher order polynomial can "overfit" the data.
- Emerge™ uses Cross Validation to determine when to stop adding attributes.
1. Leave out a test well, and solve the regression coefficients using only the remaining wells
2. Use these coefficients to predict the target attribute in the test well
3. The prediction error is the validation error for that test well
4. Repeat for each training well, and compute the average validation error
Data and Results
Location of the 13 Study Wells

- Located within the Athabasca oil sands

Well Locations

Image from Google Earth®
Summary of the 13 Study Wells

Each well has:

- Lab Viscosity Measurements from AccuMap®
- Dipole sonic logs
- Full suite of standard well log curves

- Viscosity ranges from 6,685 cP to 18,374 cP (measured at 20°C)

* Well 13 not included in the analysis until the very end
Type Well for the Study Area (Well 2)
- Wells 1 to 5 were used to train the multi-attribute relation
- Viscosity is then *blindly predicted* in the remaining wells

**Initial Training Results**

**Number of Attributes**

21 Wells 1 to 5 were used to train the multi-attribute relation
Viscosity is then *blindly predicted* in the remaining wells

**Most important attributes:**

1. \((1 / S\text{-wave})\)
2. \((1 / SP) \reflectbox{!!!}\)
3. \((1 / \text{Gamma Ray})\)
4. \((1 / \text{Res Shallow})\)
5. \((\text{Res Deep})^{1/2}\)
6. \((\text{Res Medium})^{1/2}\)
7. \((1 / \text{Neutron Porosity})\)
8. \((1 / P\text{-wave})\)

**Average Error (cP)**

**Validation Error**

**All Well Error**

**Number of Attributes**
Modified Training Results (No SP)

- Validation error curve is much smoother
- Optimum fit between viscosity and our 5 training wells is found using **7 attributes**

Most important attributes:

1. \(\frac{1}{S\text{-wave}}\)
2. Res Deep
3. Res Medium
4. \(\frac{1}{\text{Res Shallow}}\)
5. \(\frac{1}{\text{Neutron Porosity}}\)
6. \(\frac{1}{\text{Photoelectric}}\)
7. \(\frac{1}{\text{Density Porosity}}\)
Cross Validation Results for the 5 Training Wells

(Log scale from 5,000 cP to 50,000 cP)

Well 1
Avg RMSE: 1830 cP

Well 2
Avg RMSE: 1205 cP

Well 3
Avg RMSE: 2199 cP

Well 4
Avg RMSE: 2190 cP

Well 5
Avg RMSE: 1716 cP
Blind Viscosity Predictions of the Remaining Wells

Well 6
Avg Error: 2011 cP

Well 7
Avg Error: 4584 cP

Well 8
Avg Error: 1060 cP

Well 9
Avg Error: 8390 cP

Well 10
Avg Error: 5162 cP

Well 11
Avg Error: 384 cP

Well 12
Avg Error: 2901 cP

Well 13
Avg Error: 55697 cP

(Log scale from 5,000 cP to 50,000 cP)
Which Wells Did Good? Which Wells did not?

- Using a cutoff error of 25% of the total viscosity range (2922 cP)

<table>
<thead>
<tr>
<th>Well</th>
<th>Avg Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Well 6</td>
<td>2011 cP</td>
</tr>
<tr>
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</tbody>
</table>

82 km South
Why Would Some Wells Predict Viscosity Better than Others?

Well 11
Best Visosity Predictor

Well 9
Worst Visosity Predictor
Conclusions

• Predicting viscosity using multi-attribute regression of well logs was done successfully, within 25% error in 4 out of the 7 blind test wells.

• It is important to use the entire range of desired viscosities when training the regression.

• The shear sonic log was found to be the most important viscosity predictor.

• The next most important attributes were: the 3 resistivity logs, neutron porosity, photoelectric factor, and density porosity.

• Observations suggest that viscosity can be predicted most accurately in a well where the reservoir has separation between resistivity curves (ie. is porous and permeable).
Future Work

• **Nexen – CNOOC** has provided viscosity data for ~150 wells with multiple measurements per well

• **Goal:** define an empirical relationship to predict a wide range of viscosities using only standard well log curves

• **If time:** develop a Matlab code to do this analysis, but test more non-linear transformations of the attributes
Acknowledgements

• Larry Lines (supervisor)
• Nexen / David Gray (expanded viscosity dataset)
• Scott Keating & Bobby Gunning (discussions / dry runs)
Questions?
Viscosity Regression Equation

\[
\eta = 2331.90 + 8751259.00 \left( \frac{1}{S_{wave}} \right) + 49.33(\text{ResDeep}) - 72.02(\text{ResMedium}) \\
+ 566728.13 \left( \frac{1}{\text{ResShallow}} \right) - 2788.40 \left( \frac{1}{N\phi} \right) + 16271.04 \left( \frac{1}{P_E F} \right) \\
- 1551.46 \left( \frac{1}{D\phi} \right)
\]
Viscosity Measurement

- Cone and Plate Viscometer is typically used for heavy oil
- The resistance to the rotation of the cone produces a torque that is proportional to the shear stress in the fluid

\[ \text{Viscosity} = \frac{\text{Shear Stress}}{\text{Shear Rate}} \]

\[ \eta = \frac{3G}{2\pi R^3} \left/ \frac{\Omega}{\psi} \right. \]

McKennell (1956)
Viscosity Concept

1 cP = 1 mPa · s = 0.001 Pa · s = 0.001 \( \frac{N}{m^2} \cdot s = 0.001 \frac{kg}{m \cdot s} 

• If a fluid is placed between two plates with distance 1 m, and one plate is pushed sideways with a shear stress of 1 Pa, and it moves at “u” m/s, then it has viscosity of “u” Pa·s
Uncertainty of the Viscosity Measurement

• Miller et al (2006): *Should you Trust your Heavy Oil Viscosity Measurement?*
Velocity Dispersion

- Velocities tend to increase with measurement frequency
- Laboratory measurements give higher velocities than sonic logs or seismic data
- Example from a heavy oil field 50km SW of Fort McMurray

Kato & Onozuka & Nakayama (2008)
Wait ... S-waves travel through heavy oil?