



# Nonstationary Predictive Deconvolution

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# Outline

- Motivation
- Partitions of Unity (POU)
- Nonstationary operators
- Nonstationary prediction filtering
- Testing on nonstationary  $Q$  synthetic
- Testing on synthetic with multiples
- Conclusions

# Motivation

- Predictive deconvolution has a historical basis in multiple attenuation. While not entirely successful, the technique has been useful.
- Nonstationary effects are a limiting factor.
- Gabor deconvolution generalizes spiking deconvolution, can we generalize gapped predictive deconvolution?

# Partitions of Unity

$$\sum_{k=1}^N \Omega_k(x) = 1, \forall x \in [a, b]$$

Definition of a POU

$$g_k(x) = \Omega_k^p(x), \quad p \in [0, 1]$$

Analysis window (applied before the operator)

$$\gamma_k(x) = \Omega_k^{1-p}(x), \quad p \in [0, 1]$$

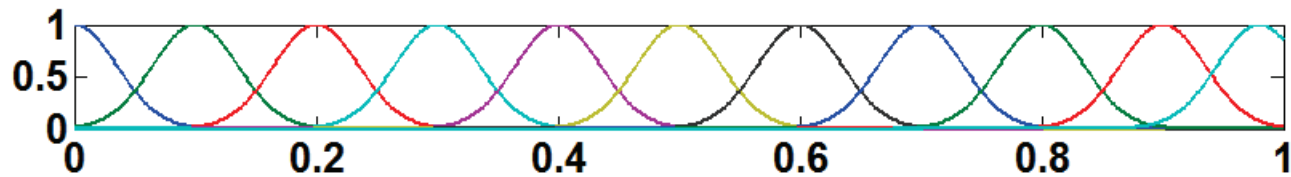
Synthesis window (applied after the operator)

$$\sum_{k=1}^N g_k(x) \gamma_k(x) = \sum_{k=1}^N \Omega_k^p(x) \Omega_k^{1-p}(x) = \sum_{k=1}^N \Omega_k(x) = 1$$

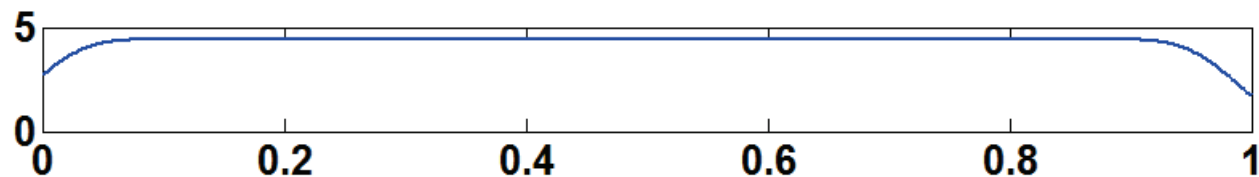
Analysis and synthesis windows together form a POU

# Uniform POU

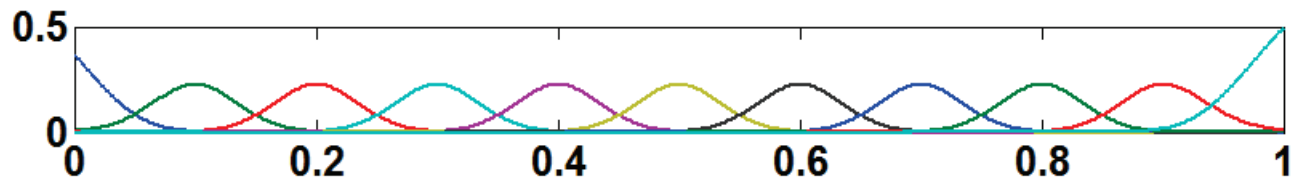
normalized for finite interval



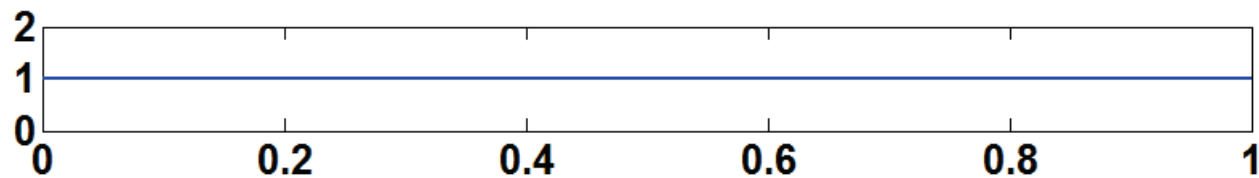
a) Selected Gaussians



b) Normalization factor



c) Gaussians after normalization



d) Sum of the normalized windows

# Making Approximate POU's Exact

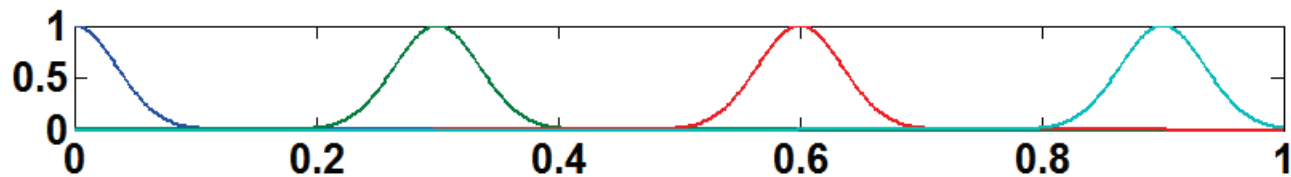
$$\sum_{k=1}^N \tilde{\Omega}_k(x) \approx \text{Constant}, \quad \text{Approximate POU}$$

$$\Omega_k(x) = \frac{\tilde{\Omega}_k(x)}{\sum_{j=1}^N \tilde{\Omega}_j(x)}$$

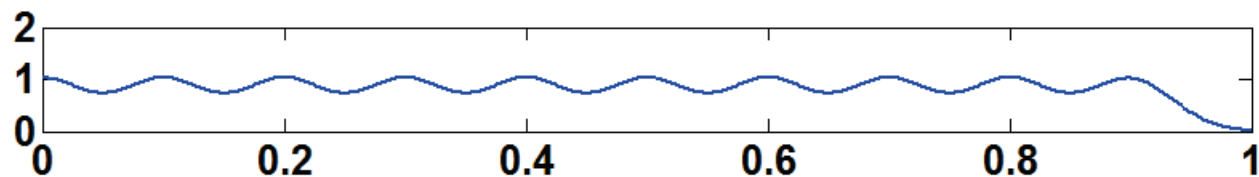
Exact POU formed from approximate one.

# Uniform POU

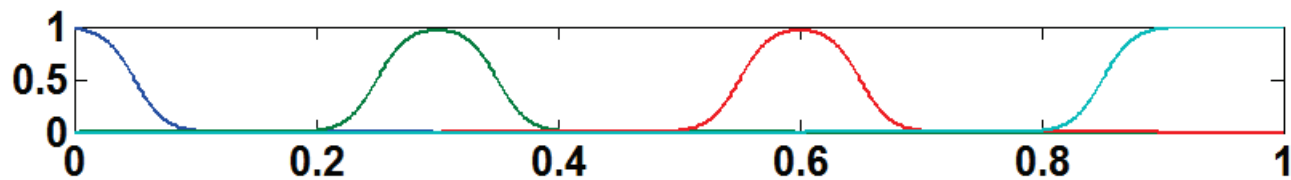
normalized for wide spacing



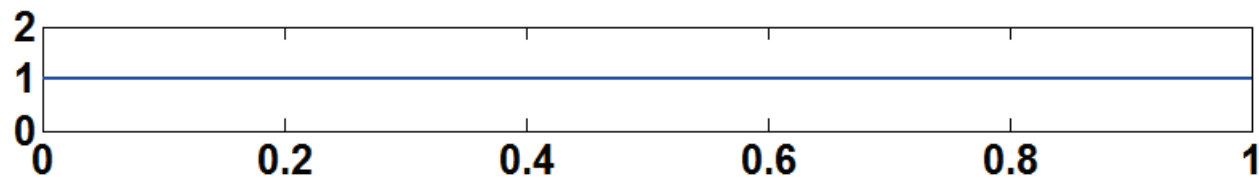
a) Selected Gaussians



b) Normalization factor



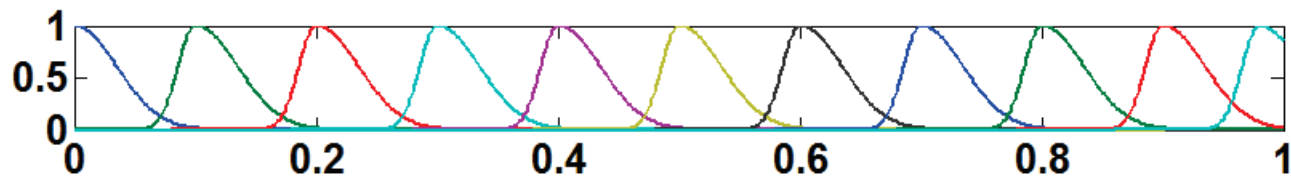
c) Gaussians after normalization



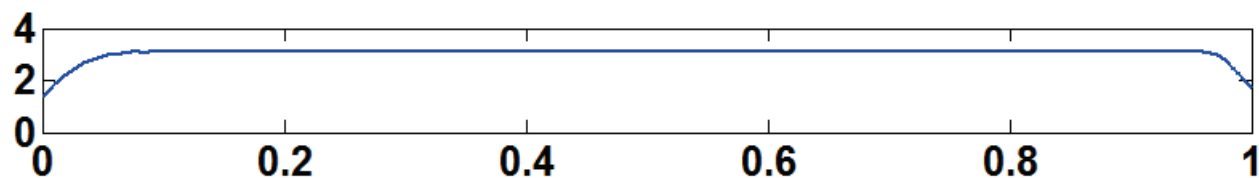
d) Sum of the normalized windows

# Uniform POU

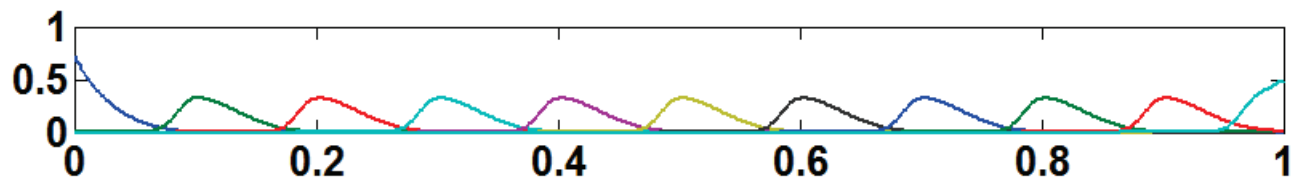
normalized for asymmetry



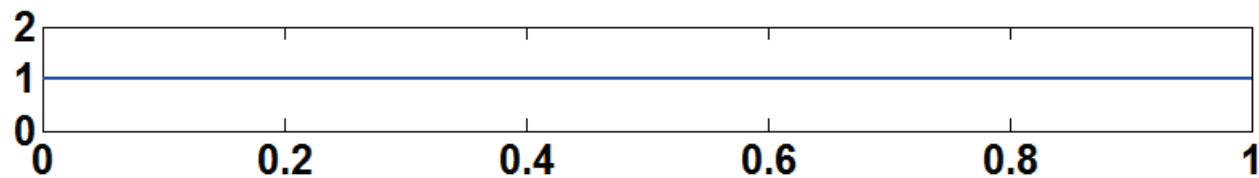
a) Selected Gaussians



b) Normalization factor



c) Gaussians after normalization



d) Sum of the normalized windows



# Nonstationary Operators

$s_k(t) = g_k s(t)$  A Gabor slice of the signal

$s(t) = \sum_{k=1}^N \gamma_k s_k = \sum_{k=1}^N \gamma_k g_k s$  A signal is the sum of a complete set of slices

$(\mathbf{T}s)(t) = \sum_{k=1}^N \gamma_k T_k s_k = \sum_{k=1}^N \gamma_k T_k g_k s$  Inserting a linear operator between the analysis and synthesis windows gives a nonstationary operator

# Nonstationary Predictive Deconvolution

## “slicedecon”

$d_k^{m_k}(t)$ ... A conventional PEF (prediction error filter) of lag  $m_k$  designed on the  $k^{\text{th}}$  Gabor slice.

Then we define nonstationary predictive deconvolution as

$$s_d = \sum_{k=1}^N \gamma_k d_k^{m_k} \cdot s_k = \sum_{k=1}^N \gamma_k d_k^{m_k} \cdot (g_k s)$$

This is the simplest possible definition with the PEF's independently designed for each slice. A more sophisticated method would require that the PEF's be related by physics.

# Fact

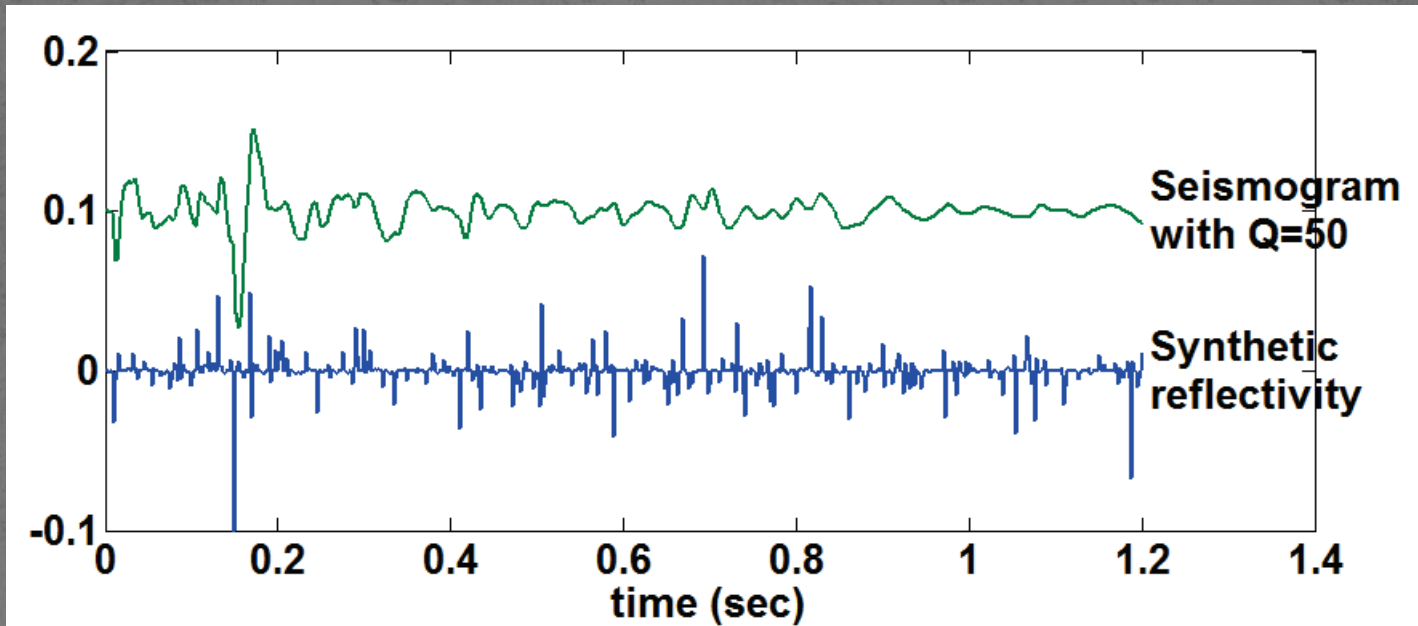
Stationary, unit-lag, predictive deconvolution is identical to minimum-phase Weiner spiking deconvolution.

# Question:

Will something similar be true for *slicedecon*?  
Specifically, will unit-lag *slicedecon* perform similarly to *gabordecon*?

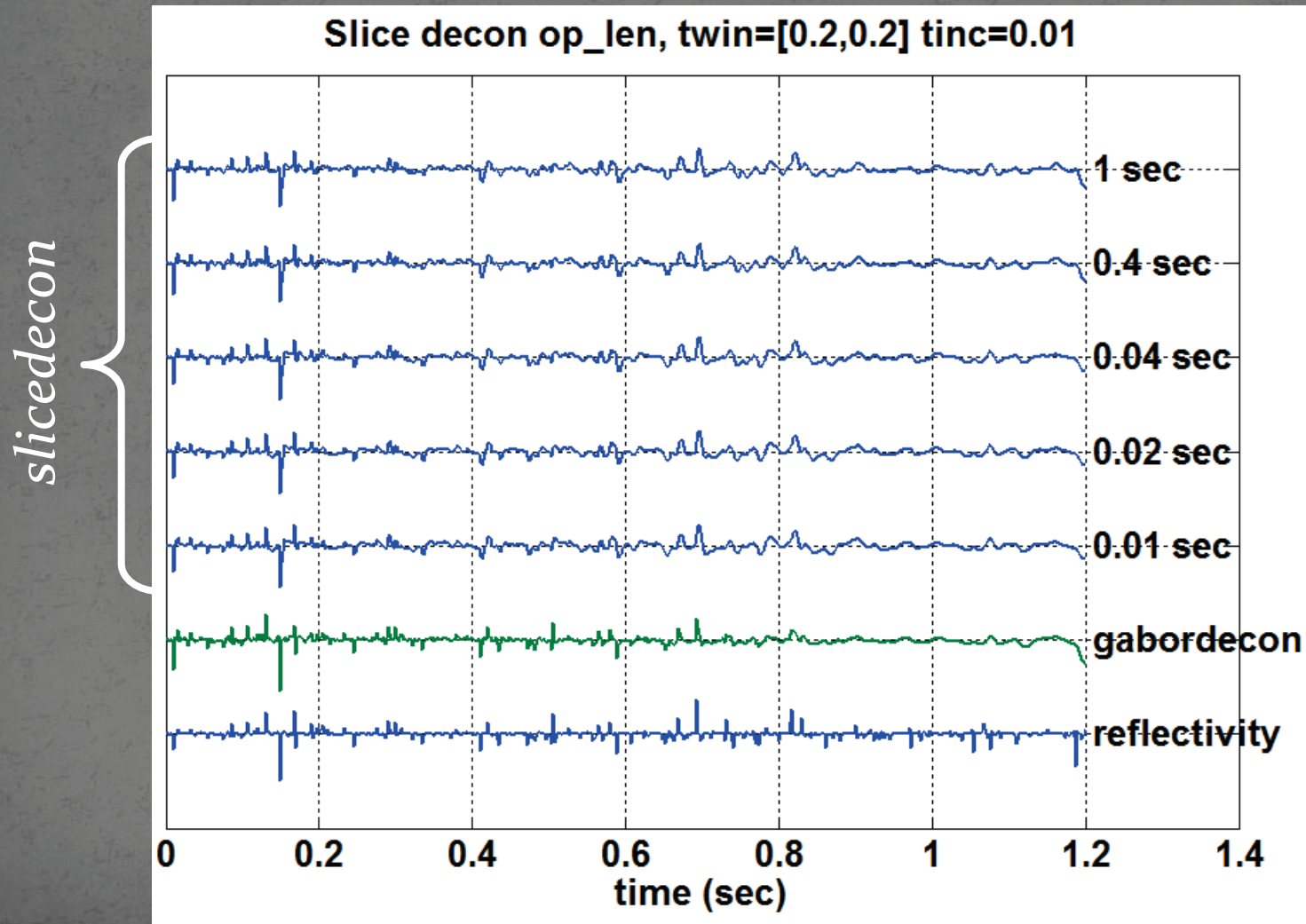
# A Constant Q Synthetic

no multiples



# *slicedecon versus gabordecon*

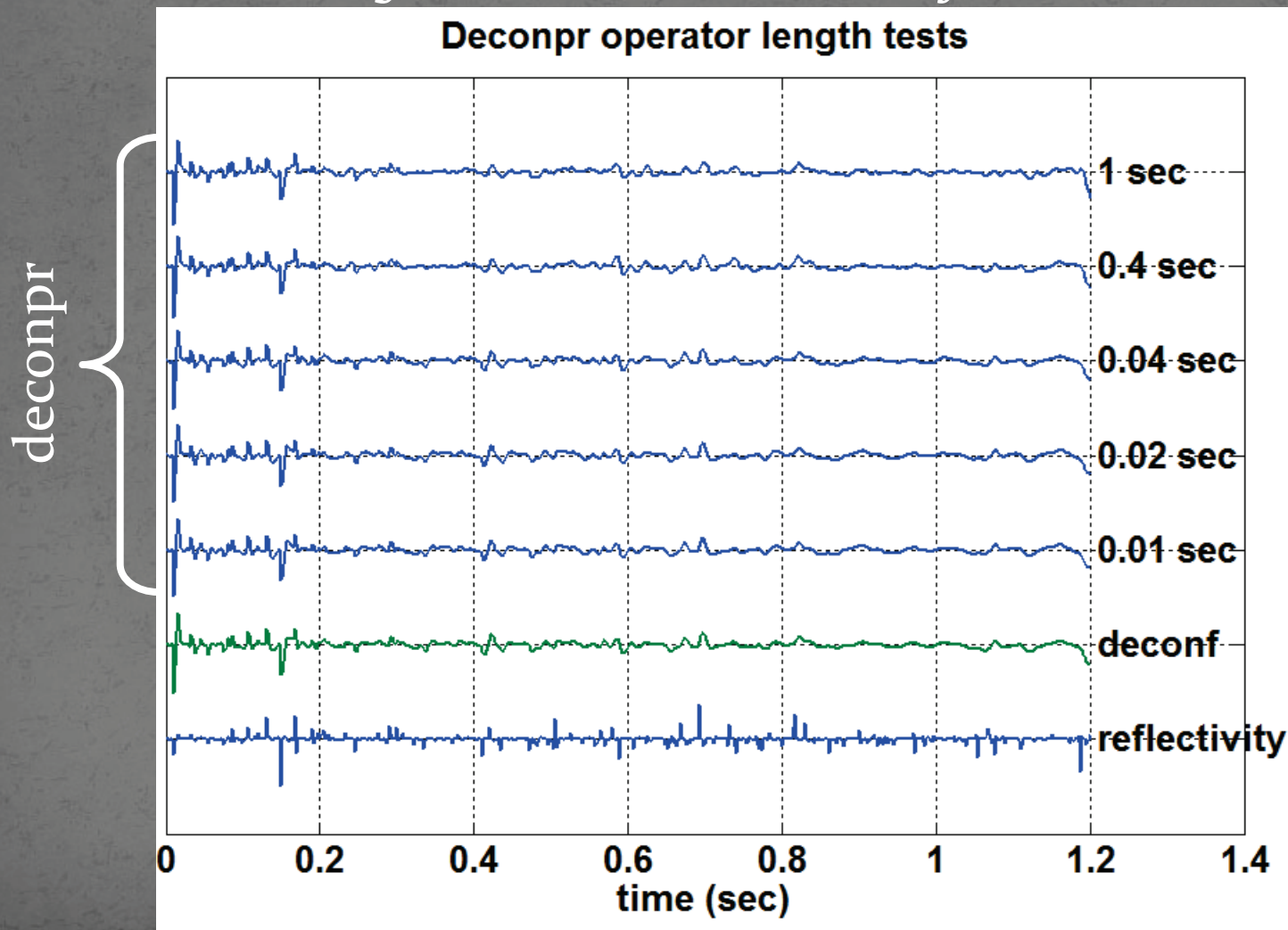
## testing operator length



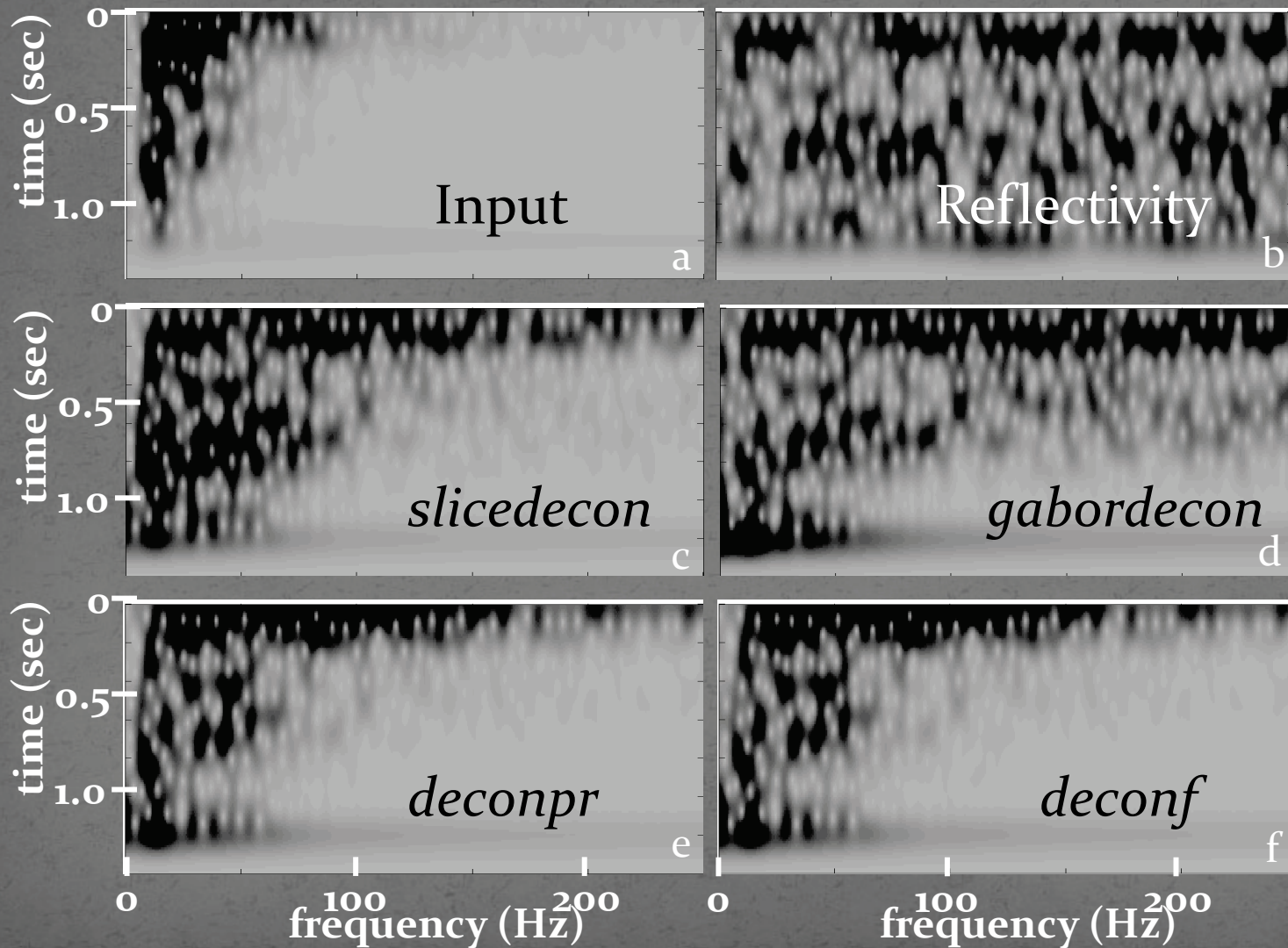
# Stationary algorithm comparison

*slicedecon*  $\longrightarrow$  *deconpr*

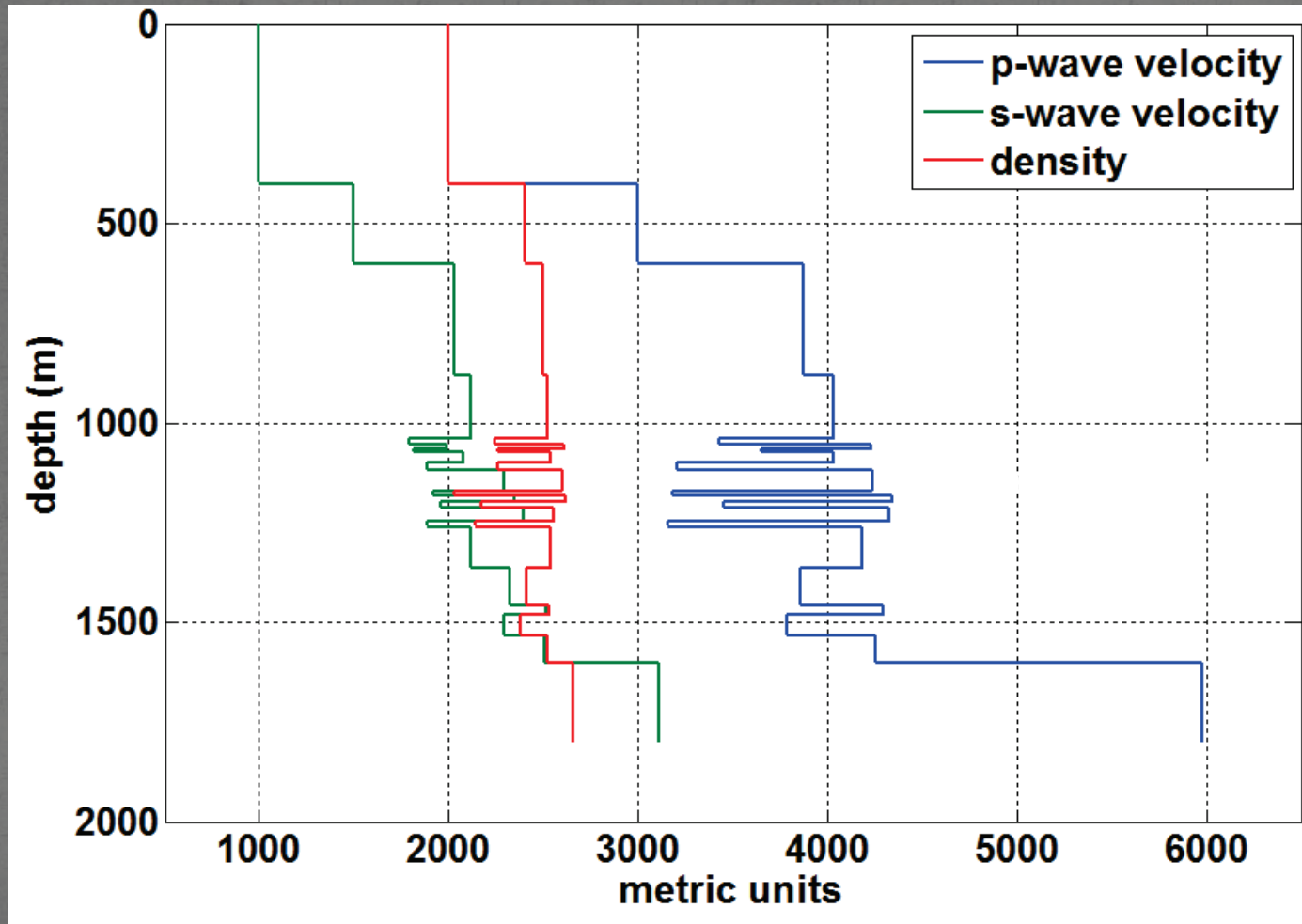
*gabordecon*  $\longrightarrow$  *deconf*



# Gabor domain comparison

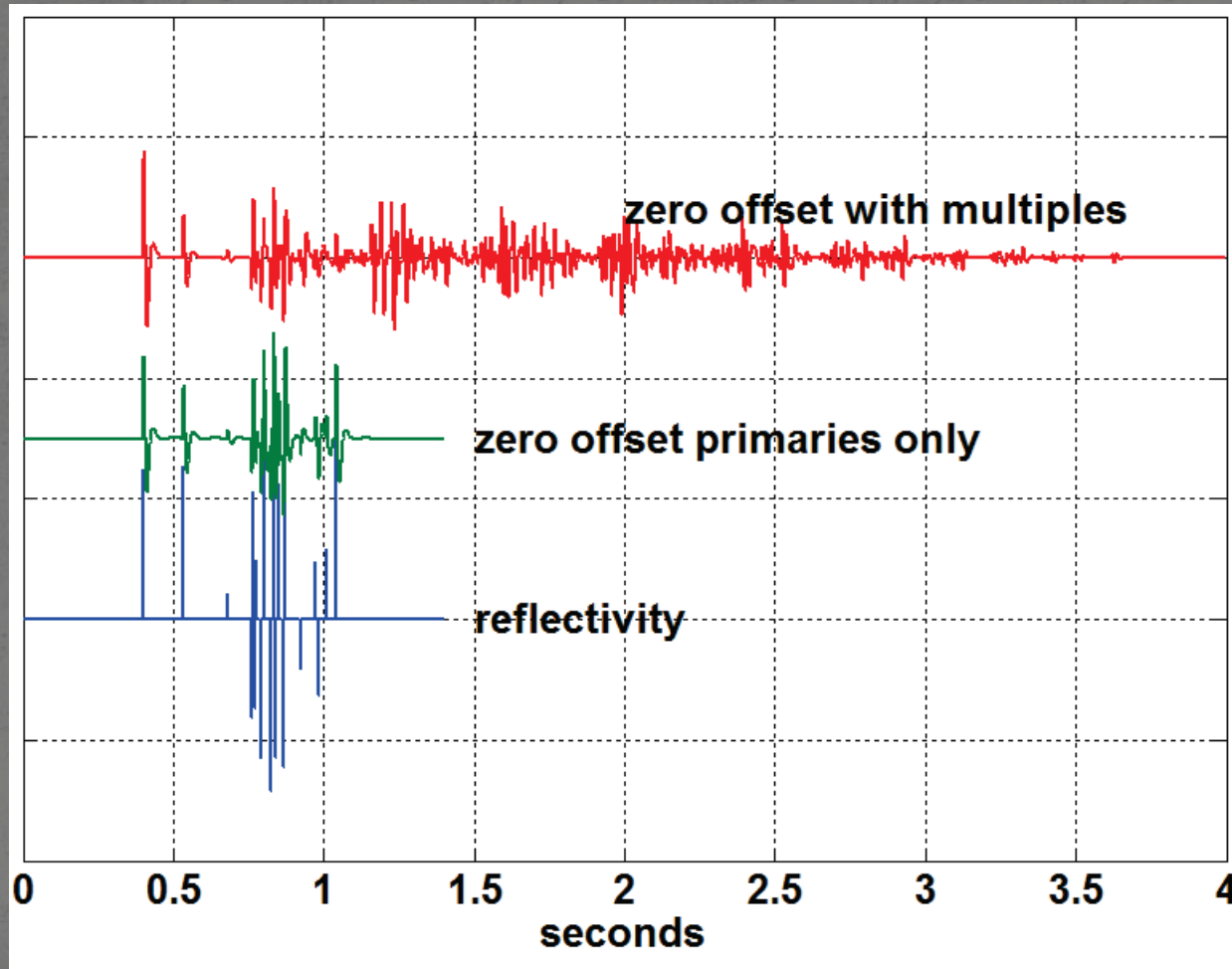


# Well-log based model

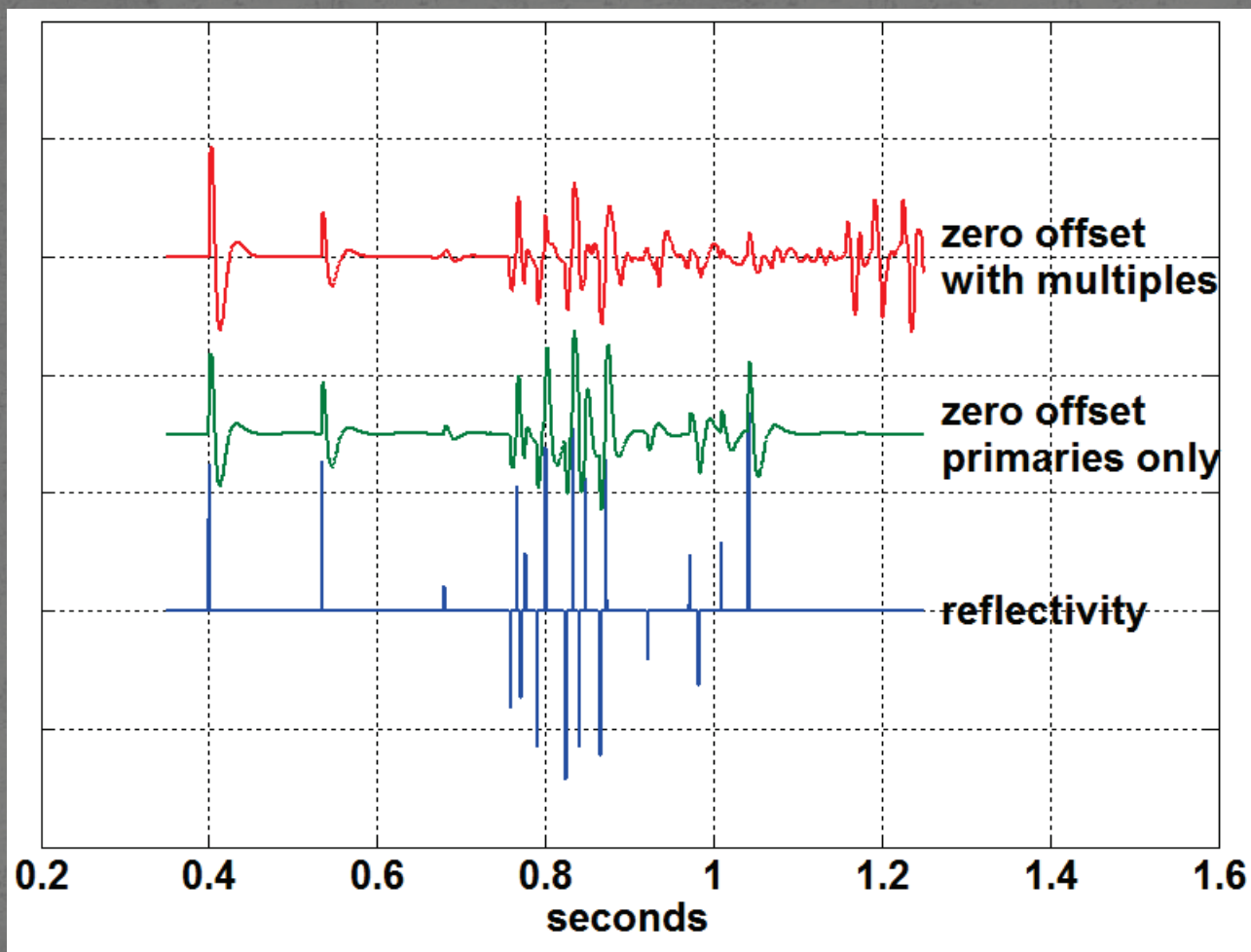




# Zero-offset Traces

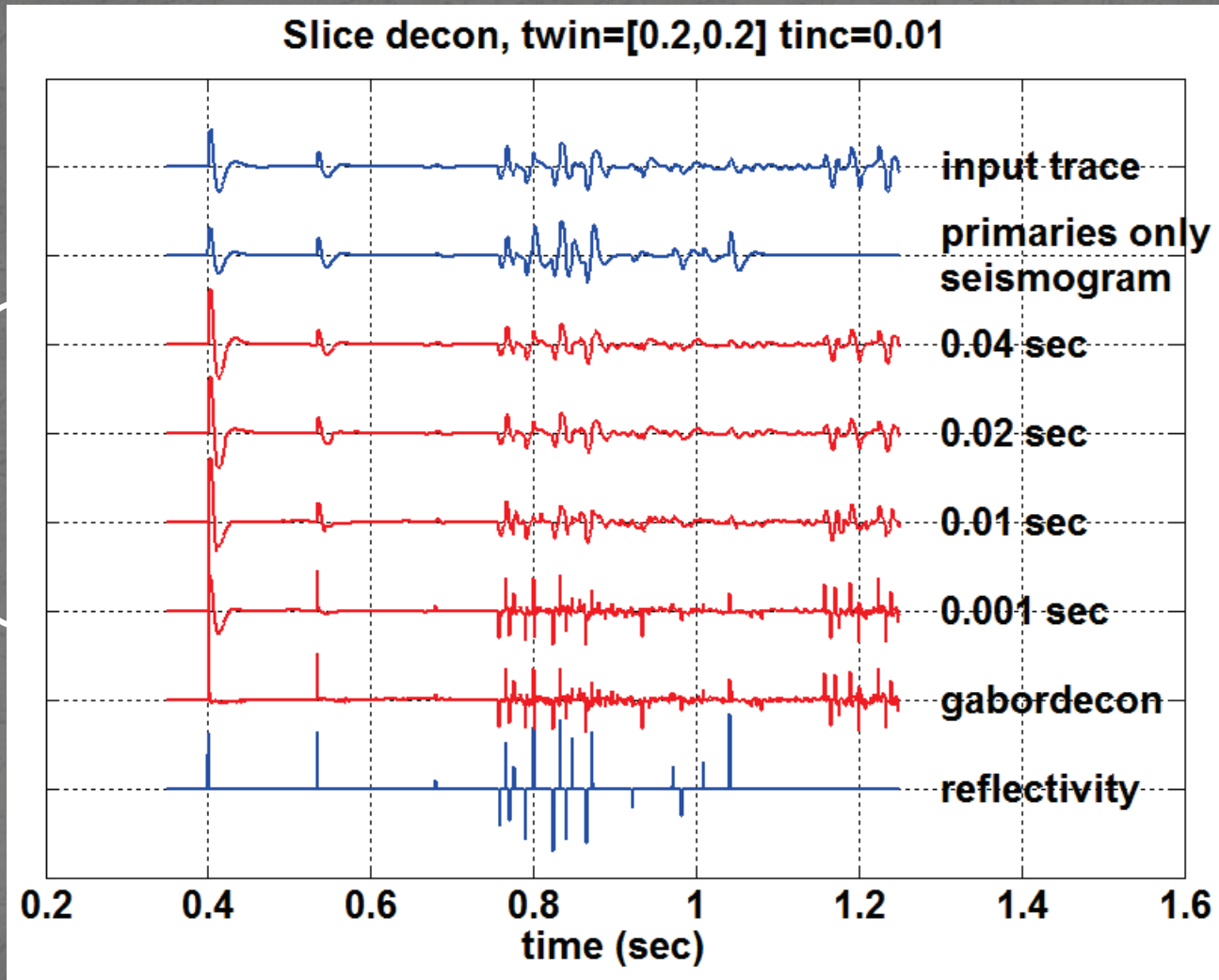


# Zero-offset traces enlargement

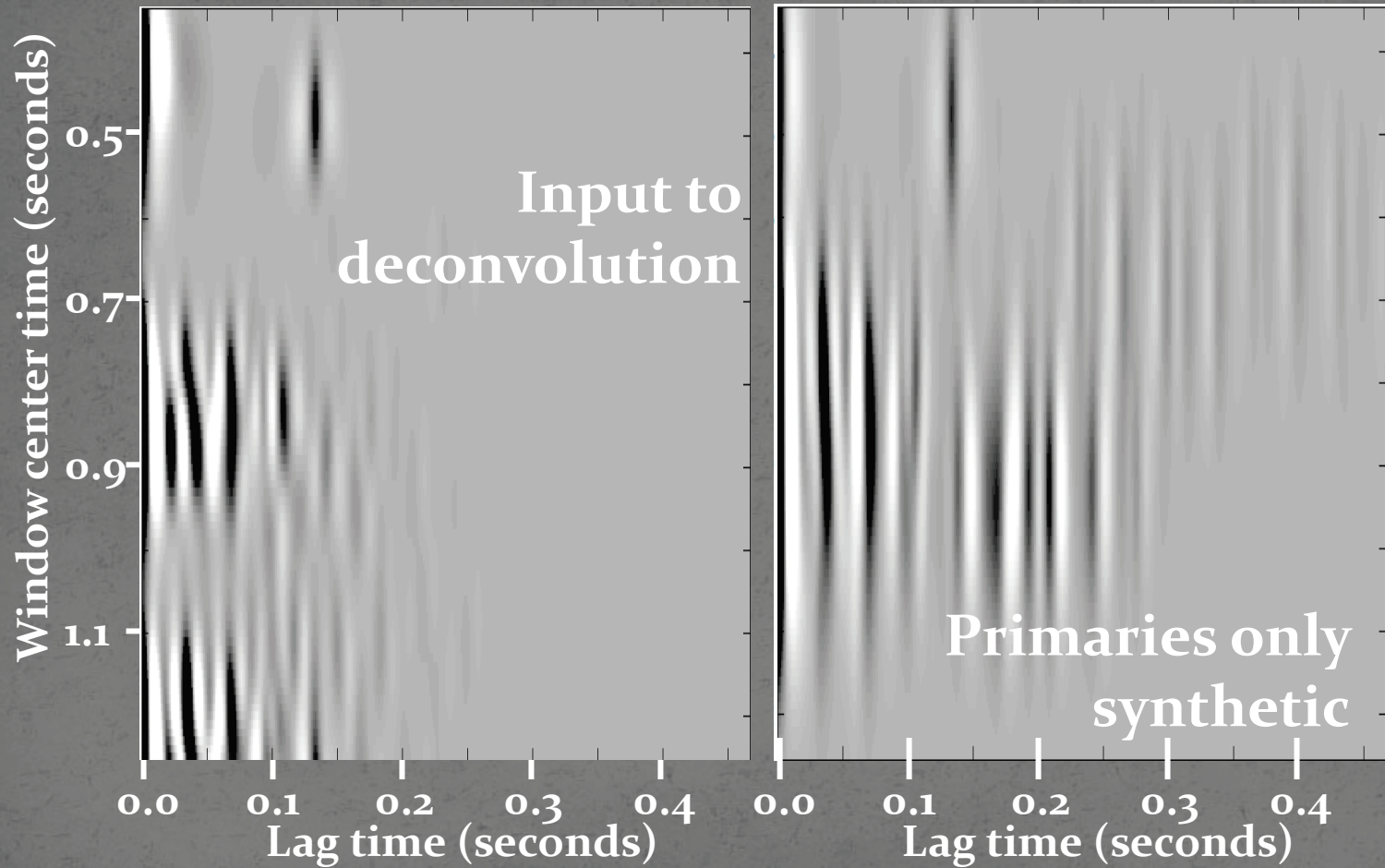


# *slicedecon*: varying prediction lag

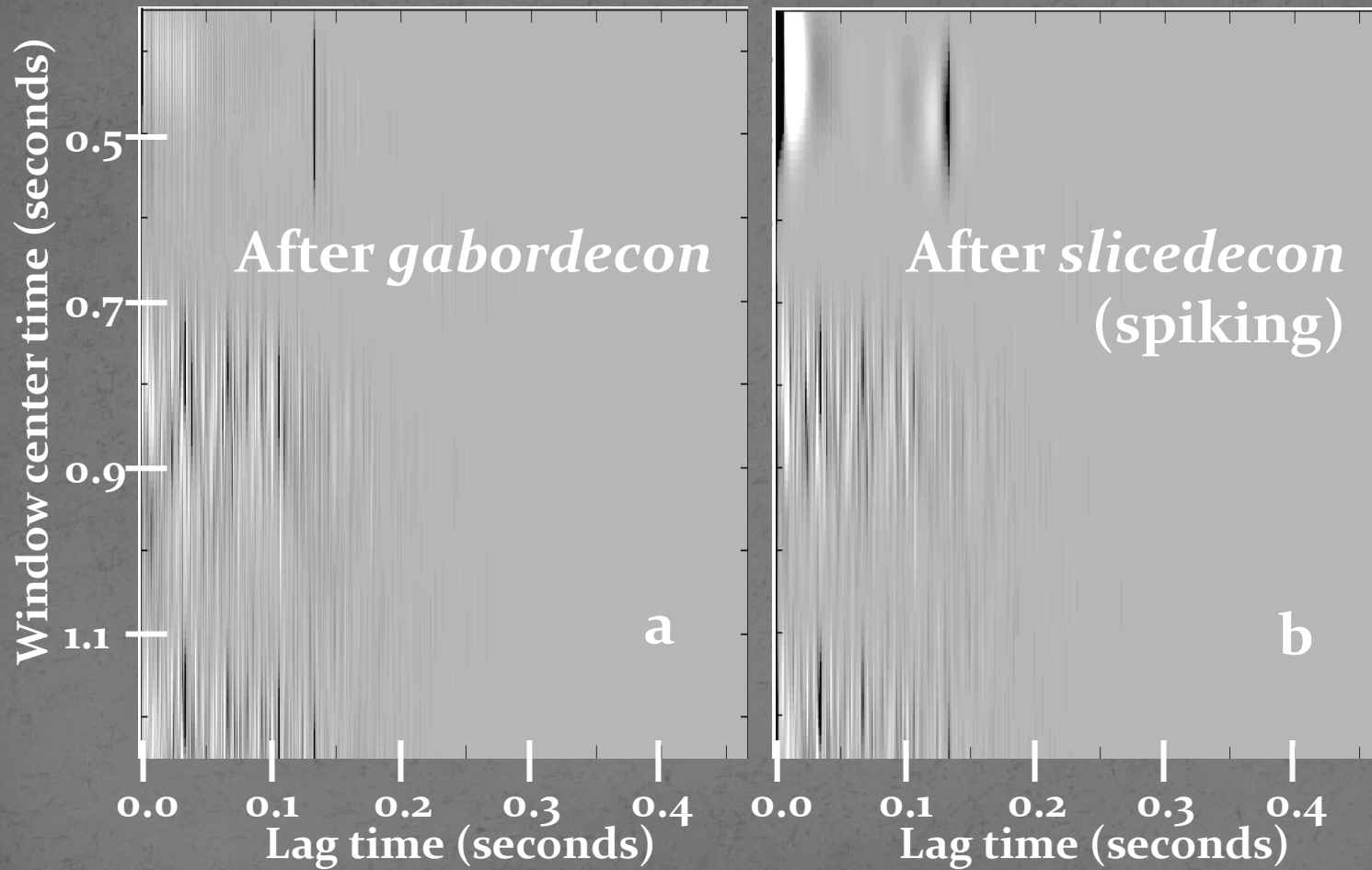
*slicedecon*



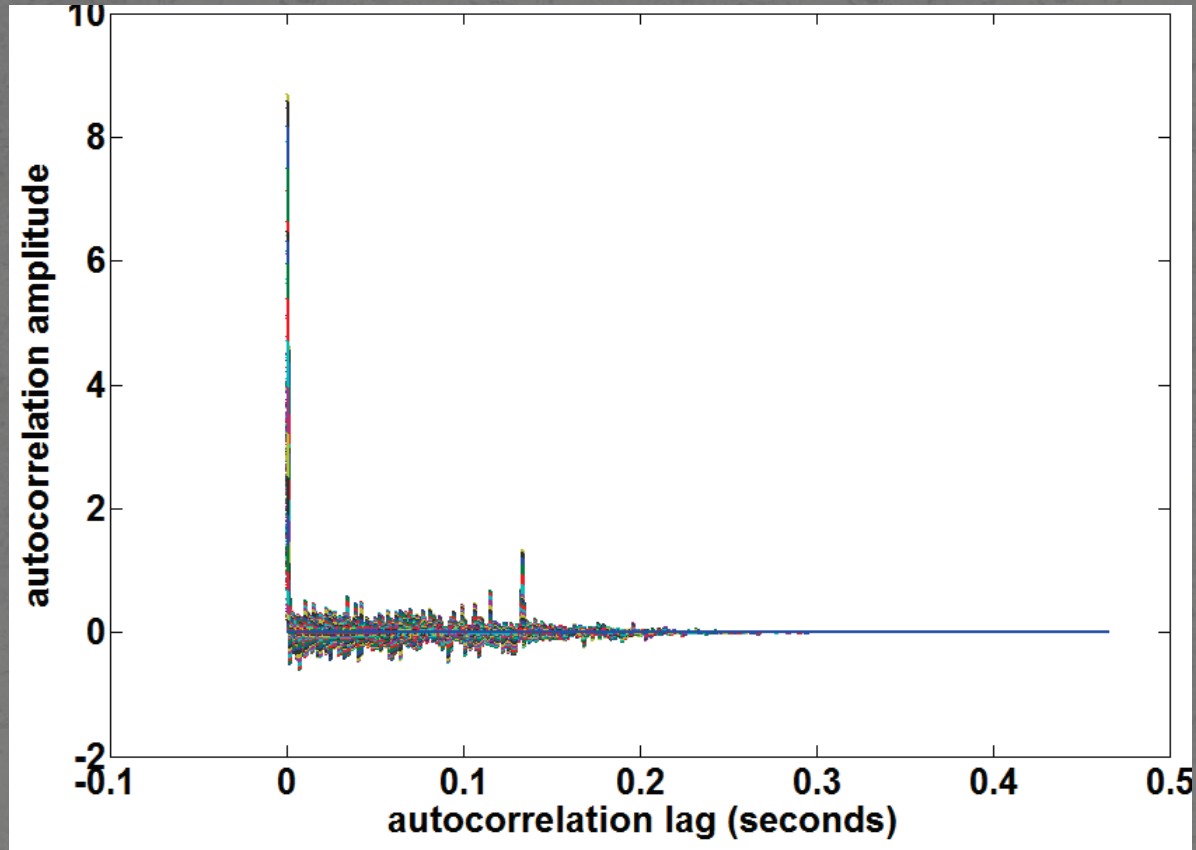
# Nonstationary Autocorrelations



# Nonstationary Autocorrelations

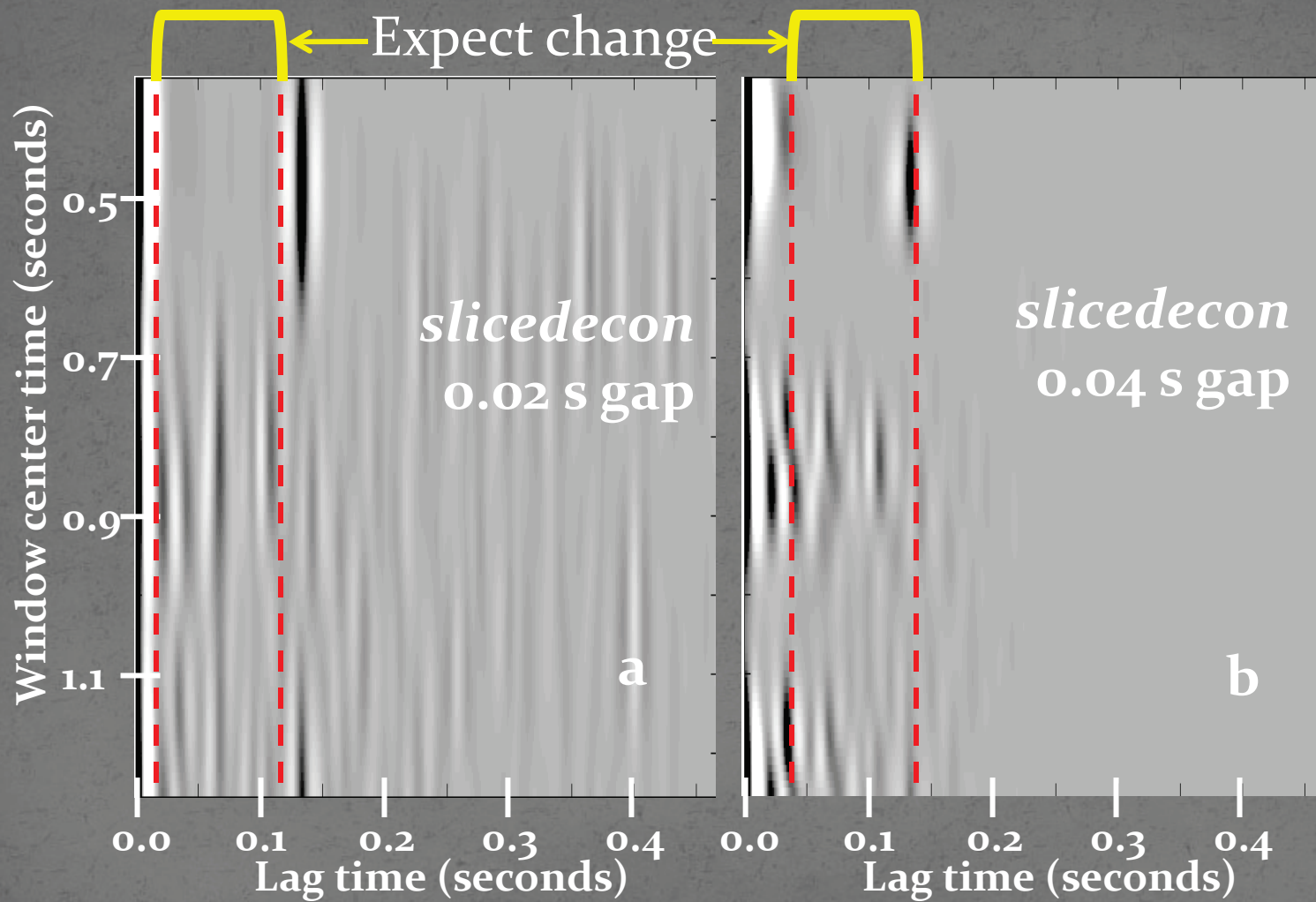


# Nonstationary Autocorrelation sideways

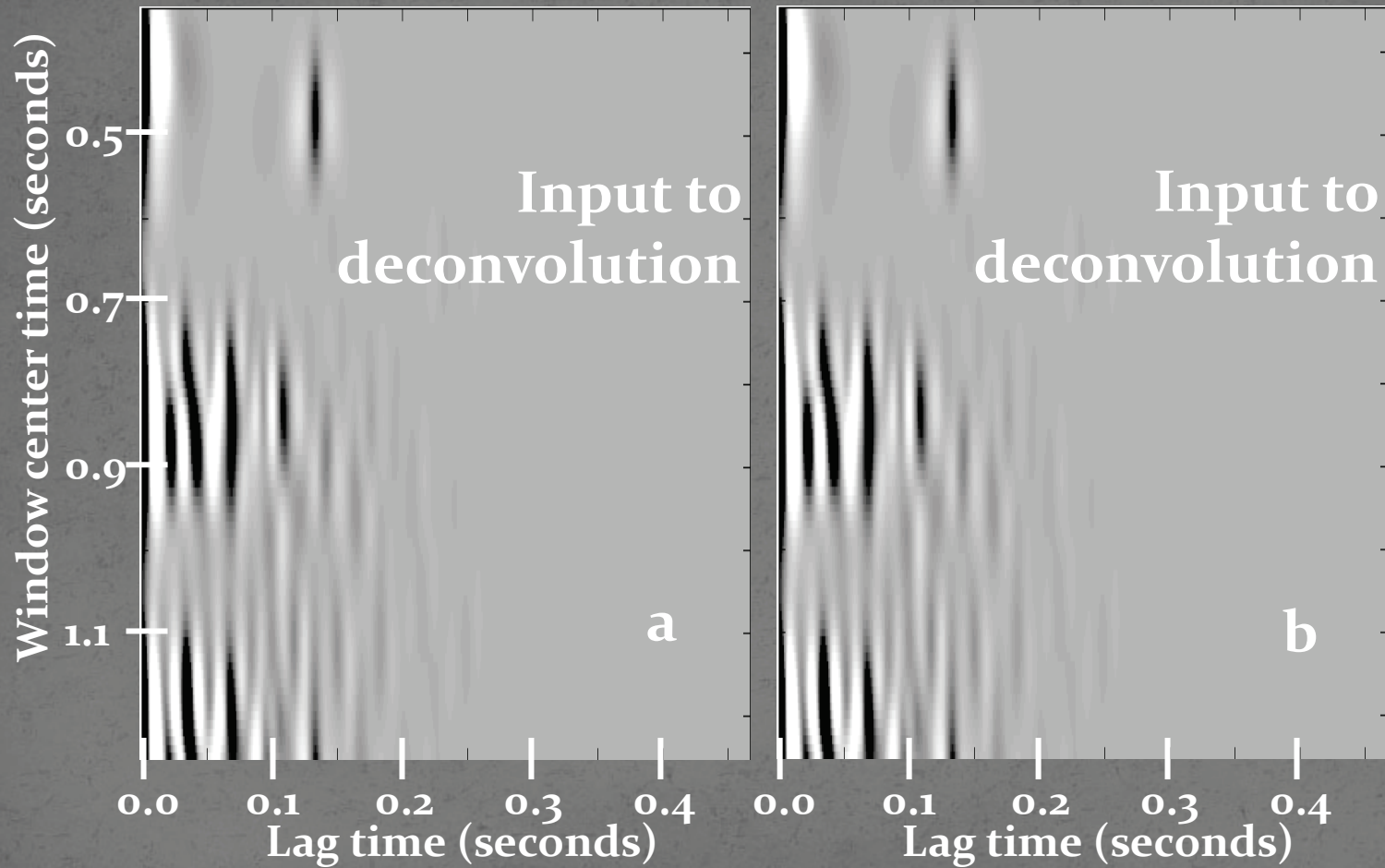


The timeslices of the nonstationary autocorrelation after *gabordecon* are plotted superimposed.

# Nonstationary Autocorrelation



# Nonstationary Autocorrelation

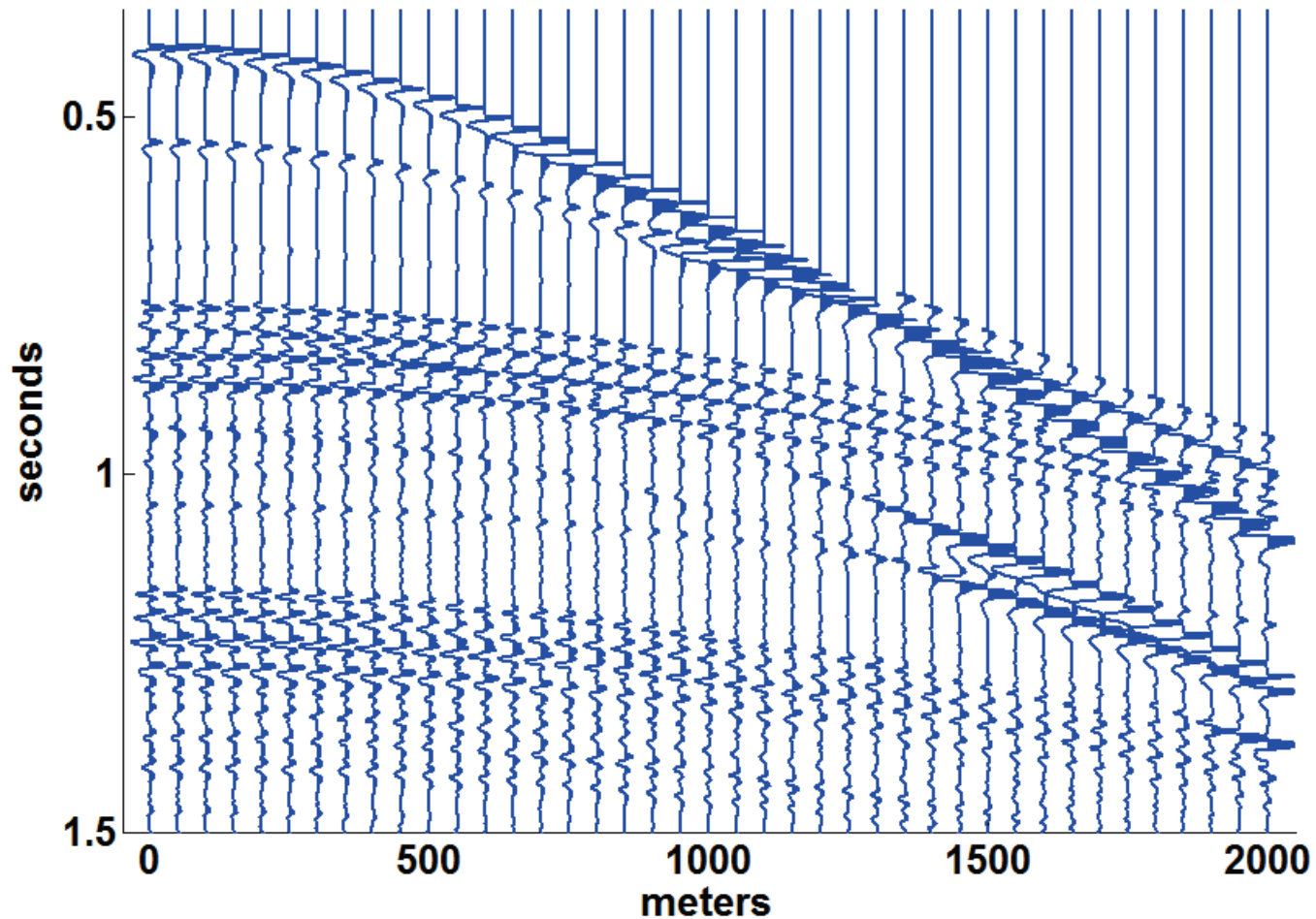




# Synthetic Gather

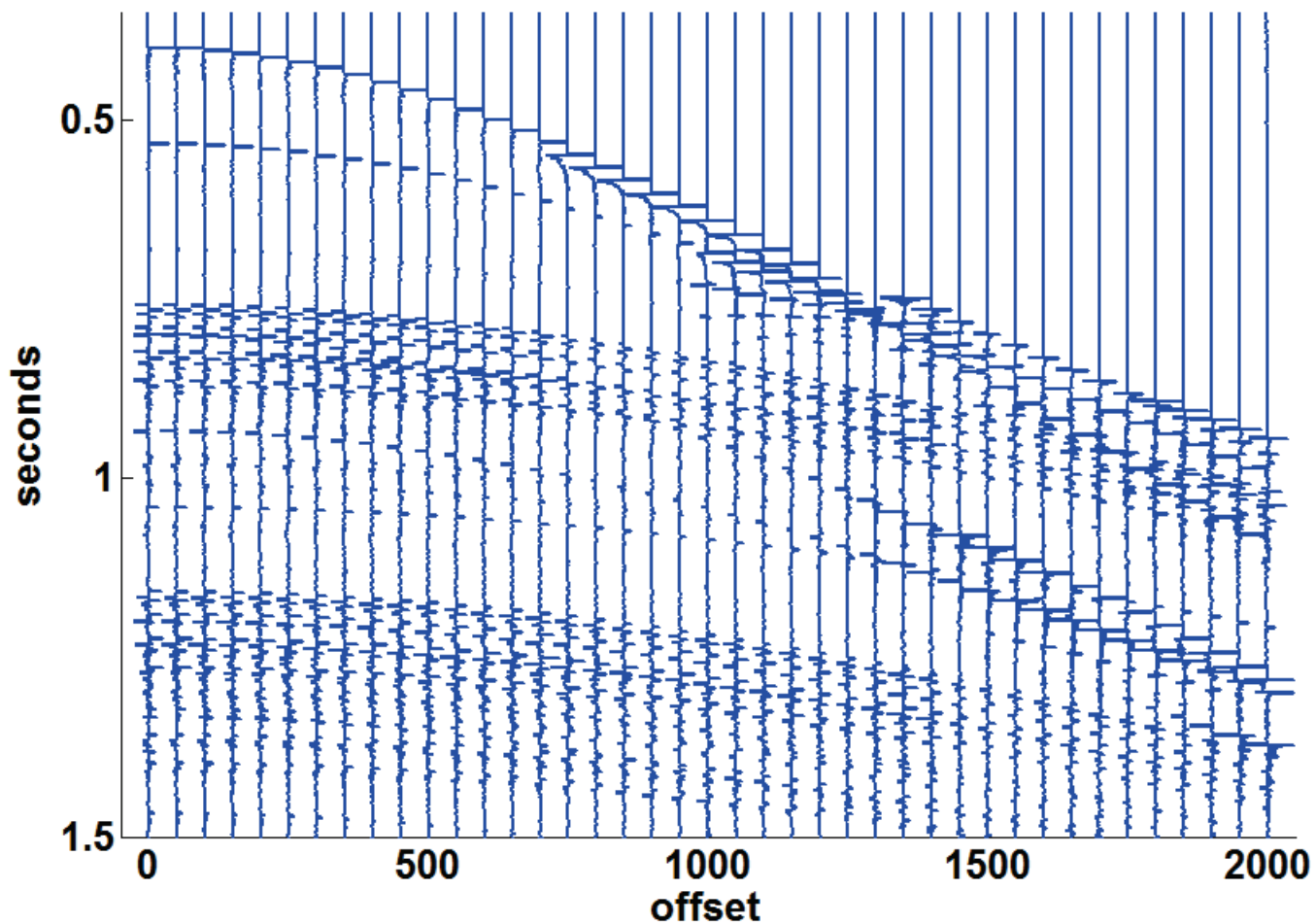
thanks to Pat Daley

**Pat's 3-bounce synthetic after gain**

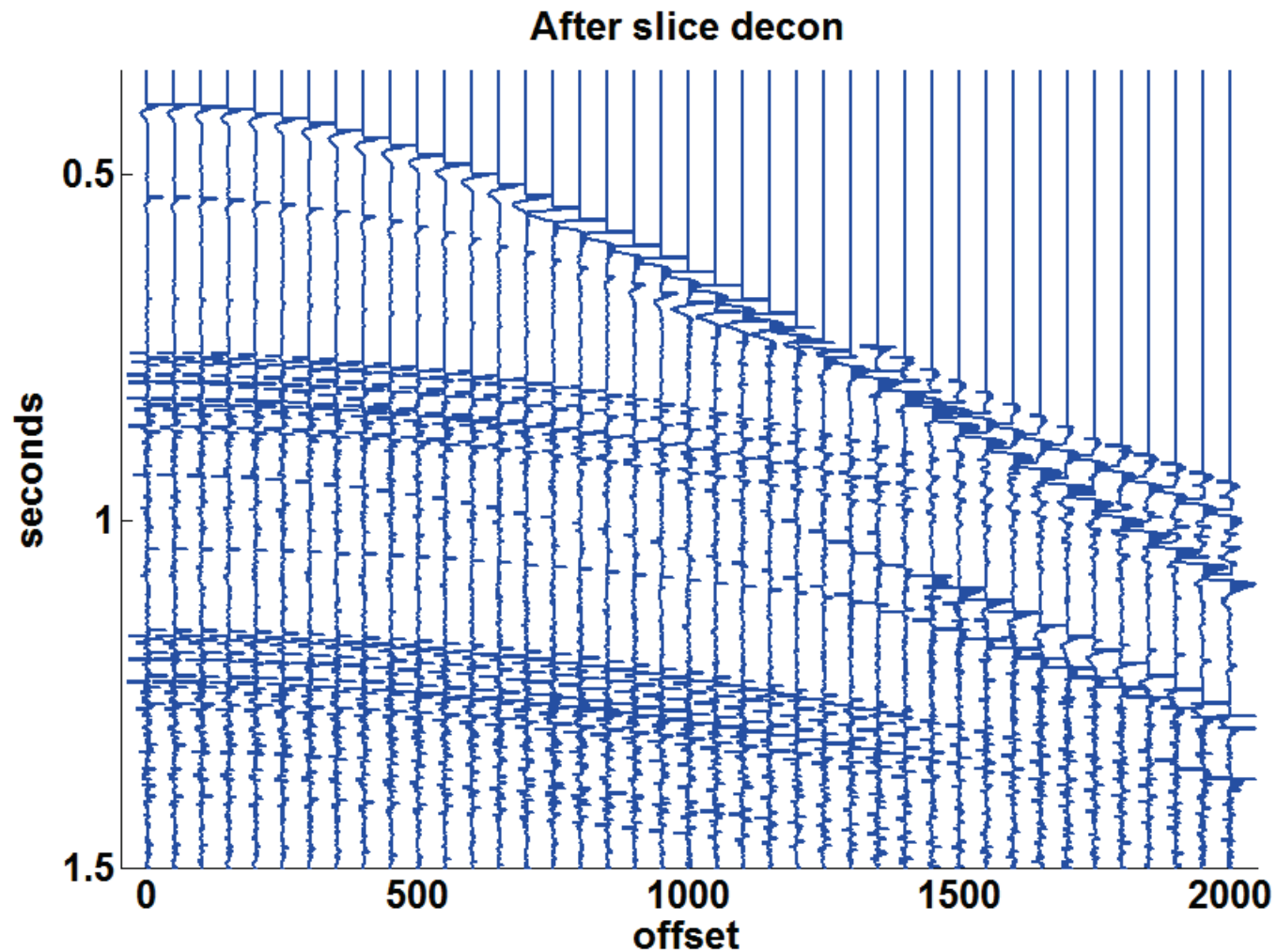


# *After gabordecon*

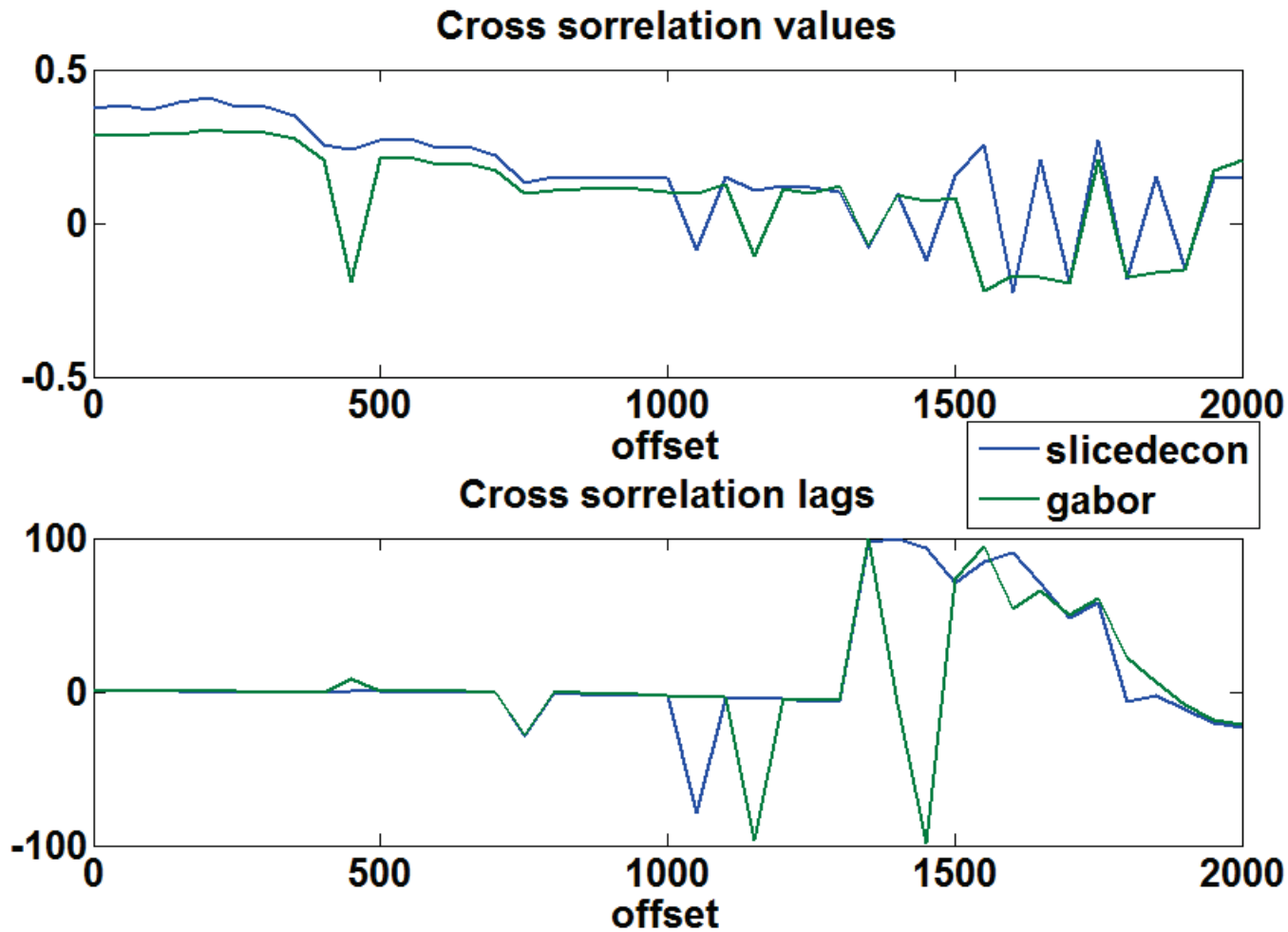
**After gabor decon**



# After *slicedecon* (spiking)

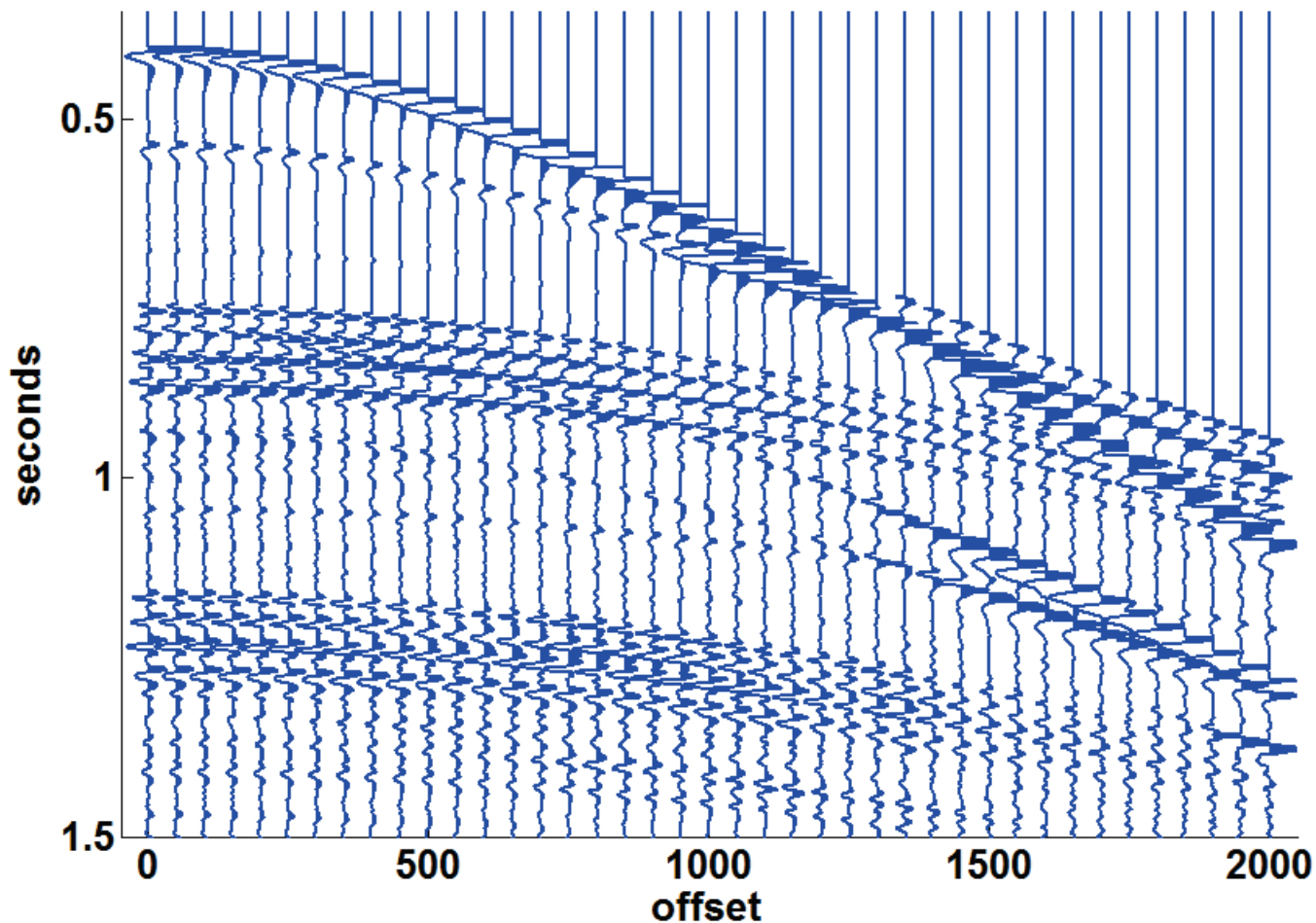


# Comparisons to Reflectivity

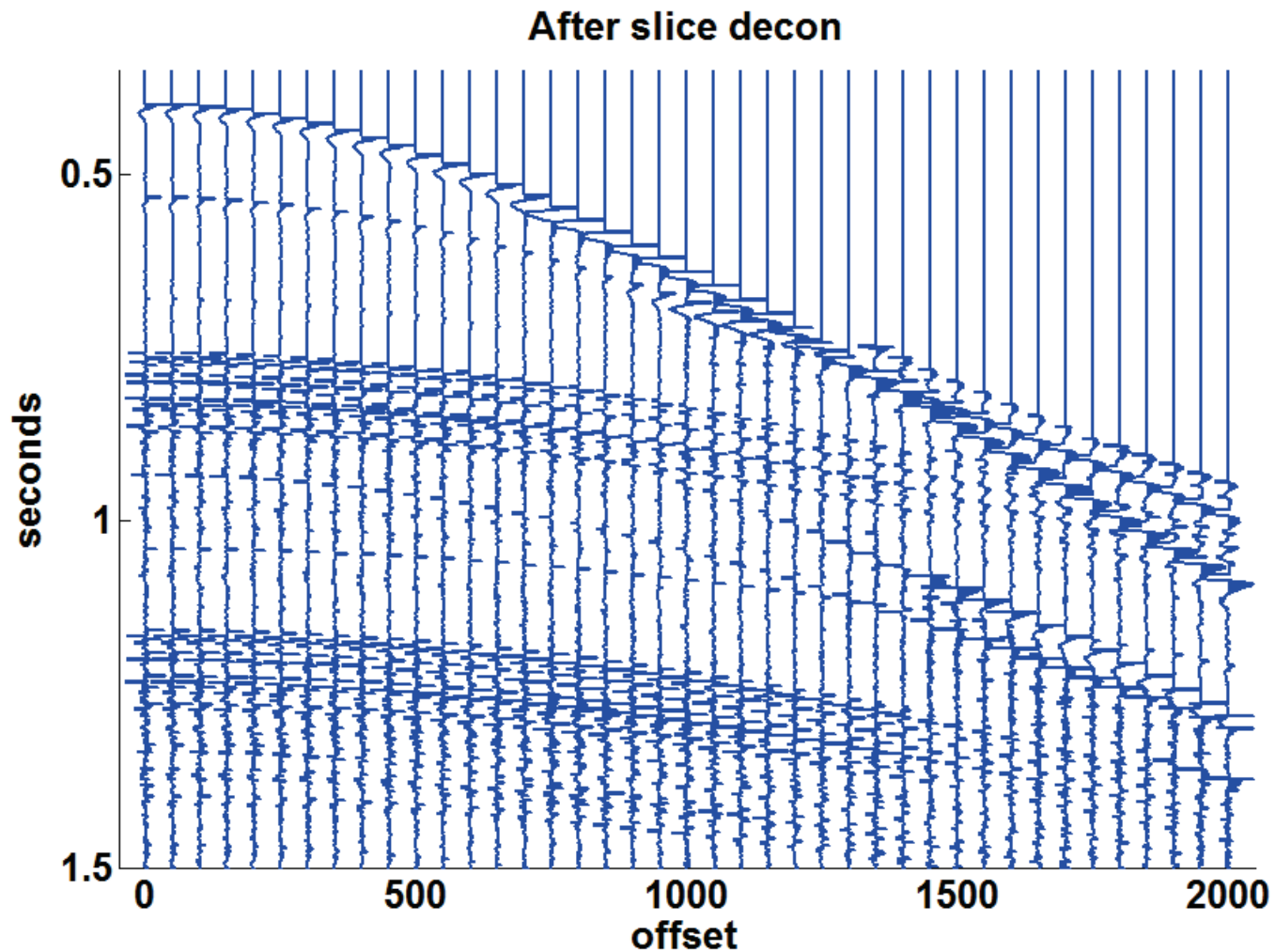


*After slicedecon (gap 0.1 seconds)*

**After gapped slicedecon**

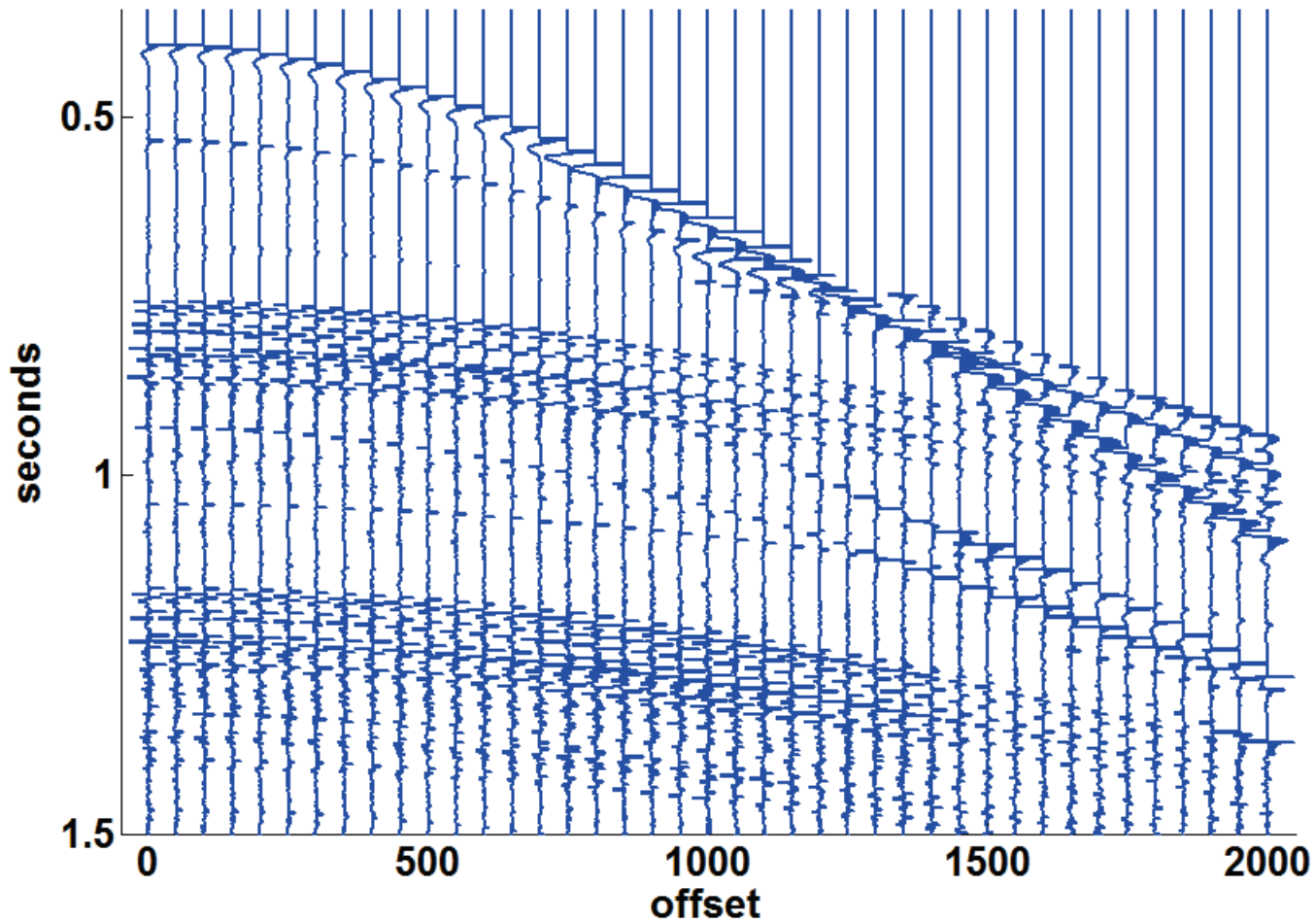


# After *slicedecon* (spiking)



# After *slicedecon* (gapped+spiking)

After gapped+spiking *slicedecon*



# Conclusions

- A direct extension of gapped predictive deconvolution to a nonstationary process has been accomplished.
- Prediction operators are designed independently in each Gabor window.
- When *slicedecon* is run as a spiking deconvolution, the results are comparable to *gabordecon*.
- When *slicedecon* is run as a gapped process, nonstationary autocorrelations show expected changes, but trace changes are very subtle.
- Gapped *slicedecon* followed by spiking *slicedecon* shows subtle but encouraging results.



# Acknowledgements

We thank our industry sponsors for their generous support which makes our work possible. We thank Pat Daley for creating our synthetic gather.

