

Viscosity Estimation Using Seismic Inversion

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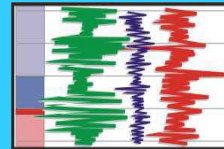
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CREWES



CHORUS

Consortium for Heavy Oil Research by University Scientists



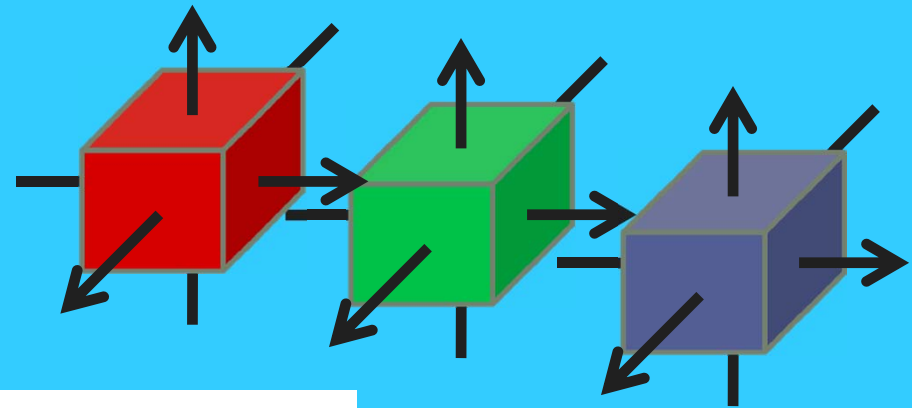
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Enhanced heavy oil production involves lowering the oil viscosity.

Reservoir Engineering Importance

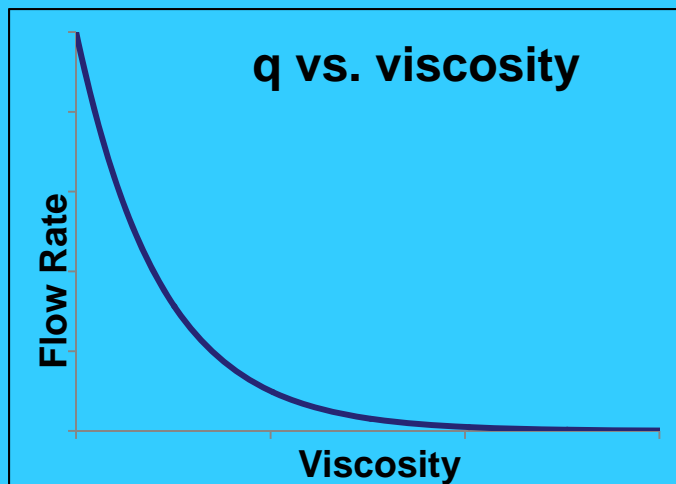
(ref. Vasheghani, 2008)



➤ Darcy's Law, q =flow rate

$$q = \frac{kA \partial P}{\mu \partial x}$$

q : flow rate
 k : permeability
 A : cross sectional area
 μ : viscosity
 P : pressure



Viscosity changes with:
Temperature (thermal mechanisms)
Gas saturation (cold production)

General Methodology

- Estimate Seismic-Q with a series of inversion methods
- Transform Q values to viscosity values with the use of rock physics relations in Biot Squirt Theory (BISQ), as described by Dvorkin et al. (1994).
- Much of this research is found in detail in the 2011 PhD thesis of Fereidoon Vasheghani entitled “*Estimating heavy oil viscosity from seismic data*”.

Inversion Methods Applied to Estimate Seismic-Q

- Traveltime tomography to estimate seismic velocity and ray paths.
- Q-tomography to estimate Q in the subsurface.
- Full waveform inversion using initial models from tomography.

Definition of Q, quality factor

- Solution to wave equation for damped harmonic oscillation

$$A(x, t) = A_0 e^{i(k'x - \omega t)}$$

with complex wavenumber, $k' = k + i\alpha$

$$A(x, t) = A_0 e^{-\alpha x} e^{i(kx - \omega t)}$$

where α is the absorption coefficient.

Definition of Q, the quality factor

- Relation of Q to absorption and wavelength (Toksöz and Johnston, 1981)

$$\frac{1}{Q(\omega)} = \frac{1}{2\pi} \frac{\Delta E}{E} = \frac{1}{2\pi} \frac{\Delta(A^2)}{A^2} = \frac{1}{\pi} \frac{\Delta A}{A}$$

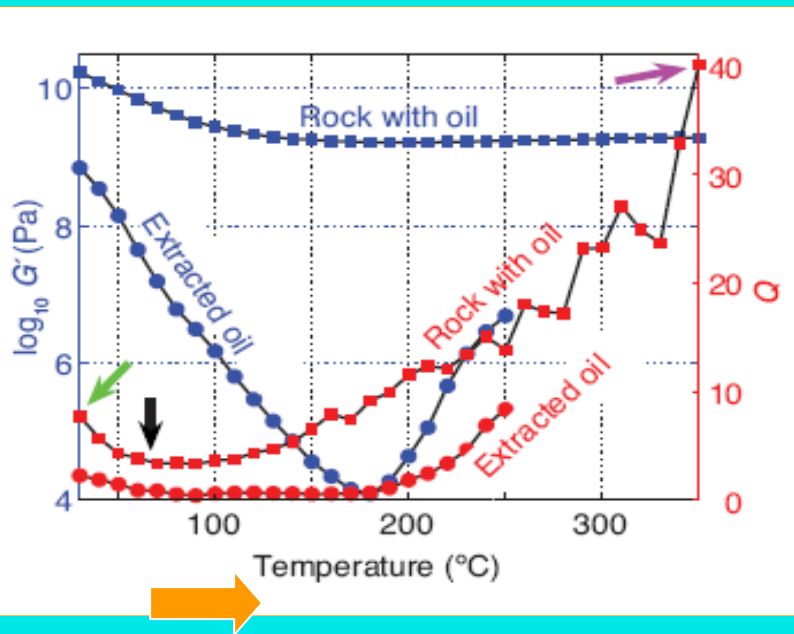
where ΔE is the energy change over one wavelength

$$\frac{1}{Q(\omega)} = \frac{1}{\pi} \frac{A_0(1 - e^{-\alpha\lambda})}{A_0} \cong \frac{\alpha\lambda}{\pi}$$

$$Q(\omega) \cong \frac{\pi}{\alpha\lambda}$$

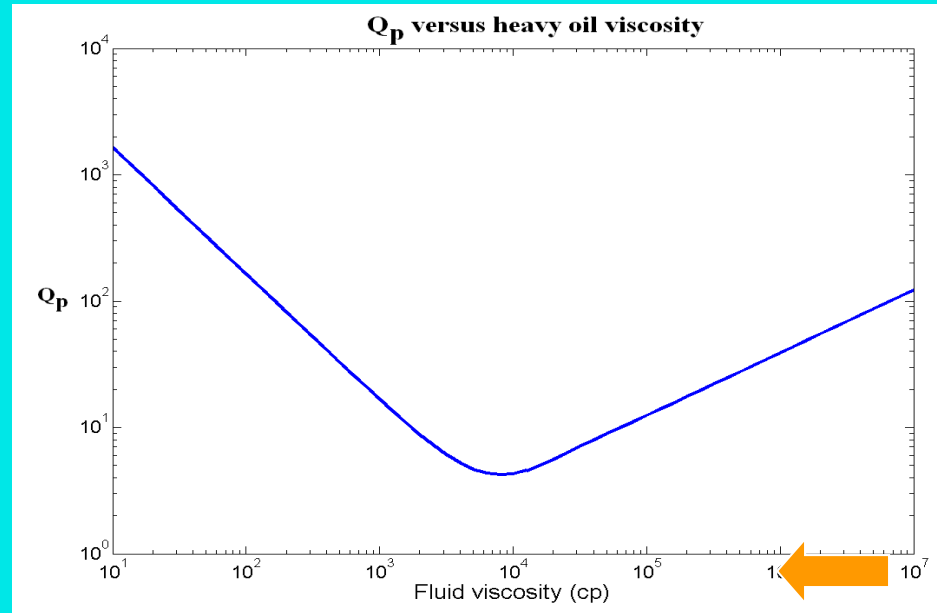
Rock Physics: Lab results & BISQ (Biot + Squirt flow model)

Measured in lab



(Behura et al, 2007)

Theoretical values



- Both lab measurements and BISQ calculations show that quality factor decrease to a minimum then increases with viscosity (temperature).

Model-based Inversion

(Lines and Treitel, 1984, among others)

- Define model parameters, x .
- Compute model response, f .
- Compare f to data values, y .
- Minimize $e=y-f$, “error of fit”.
- We can minimize e (often in a least squares sense).
- Solve for parameter change vector,

$$A\Delta x = b = y - f^0$$

Jacobian Matrix

- The Jacobian matrix, A , is a rectangular matrix of size n by p and its cost of computation can control the cost of the inversion.
- n = no. of data points
- p = no. of model parameters:

$$A_{ij} = \frac{\partial f_i}{\partial x_j}$$

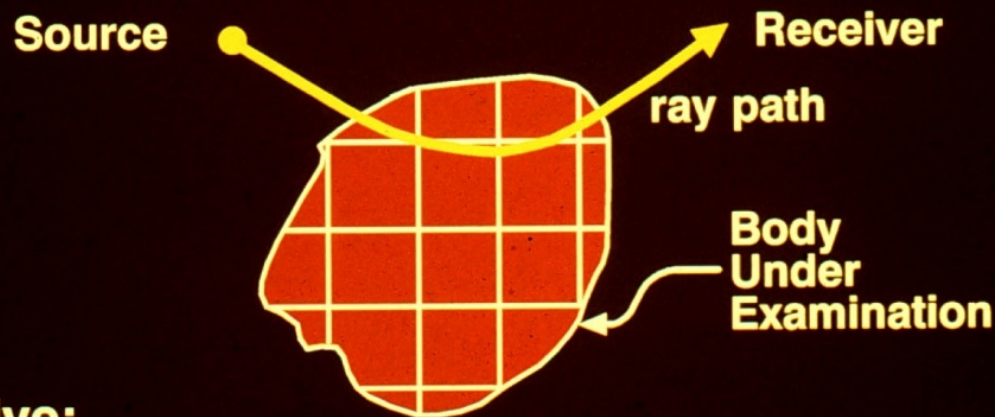
Use Seismic-Q to Estimate Fluid Viscosity

- Heavy oil viscosity can be estimated using seismic-Q measurements.
- We shall discuss the use of two inversion methods to estimate Q:
 - Q-tomography
 - Full waveform inversion for Q.

TOMOGRAPHY

- **Definition:**

The word “tomography” means section (Greek word “tomos”) drawing (“graphy”).



- **Objective:**

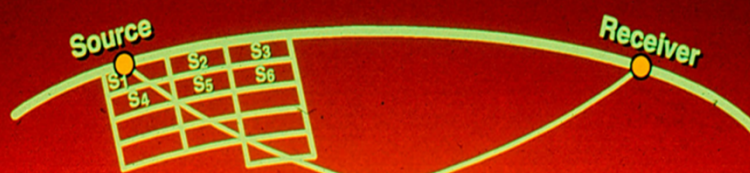
Given the set of observations gathered near the surface of a body, reconstruct the material properties within the body.

Traveltime Tomography

- A type of model-based inversion where ray tracing is used to compute seismic traveltimes.

Solution To Linear Problem

1. Discretize S
2. Collect lots of t - time data



$$\begin{bmatrix} \delta t^1 \\ \vdots \\ \delta t^N \end{bmatrix} = \begin{bmatrix} & & \\ & D_{ij} & \\ & & \end{bmatrix} \begin{bmatrix} \delta s^1 \\ \vdots \\ \delta s^M \end{bmatrix}$$

D_{ij} = distance i^{th} ray travels in j^{th} cell
Very Sparse

Usually # Rows \gg # Columns = $O(10^3)$

Comparison of Traveltime and Attenuation Tomography

- Traveltime equations

$$\mathbf{D}\mathbf{s} = \mathbf{t}$$

- Attenuation (Centroid Method (Quan and Harris, 1997))

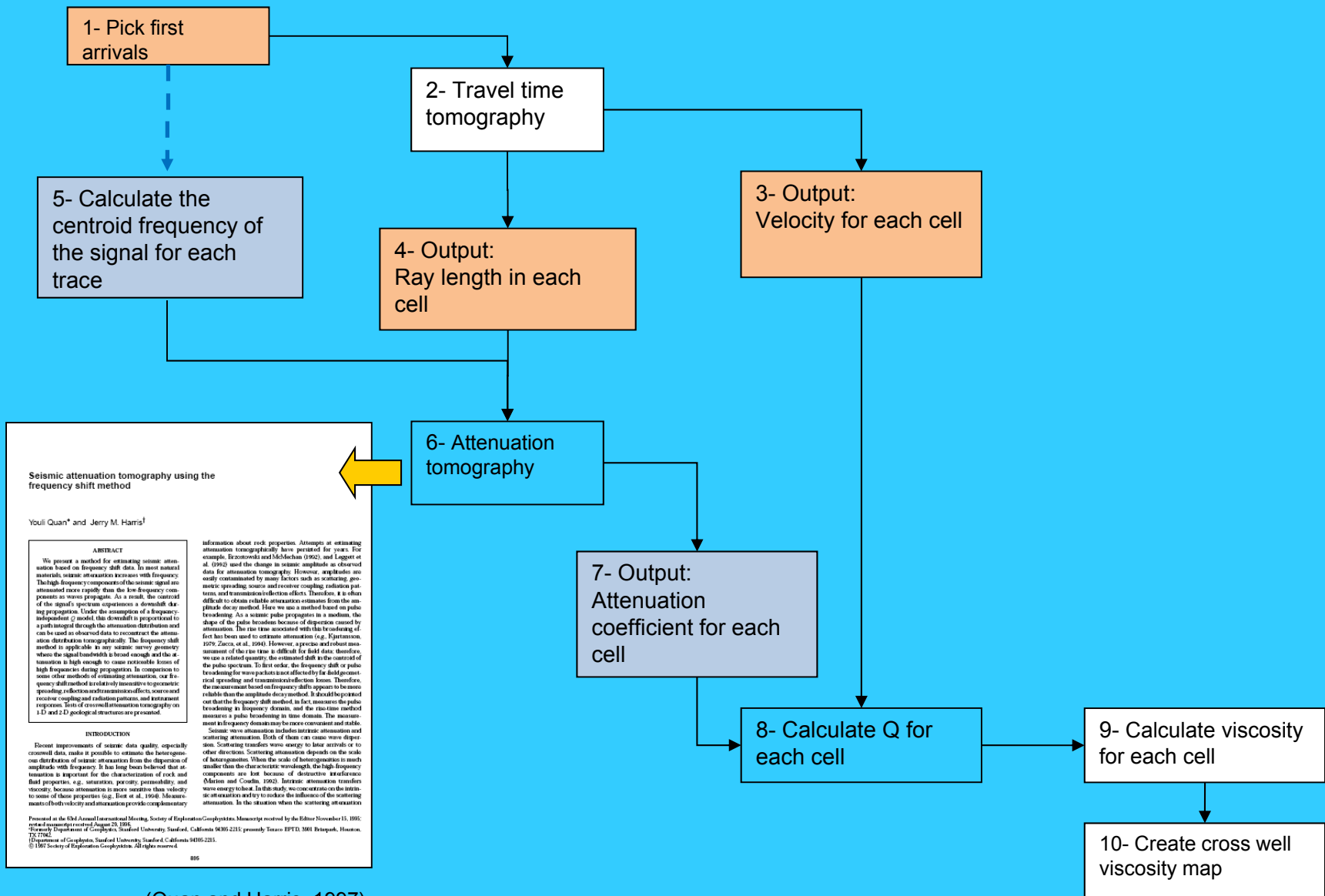
$$\mathbf{D}\alpha_0 = \mathbf{f}_s - \mathbf{f}_r$$

α_0 = attenuation coefficient/frequency

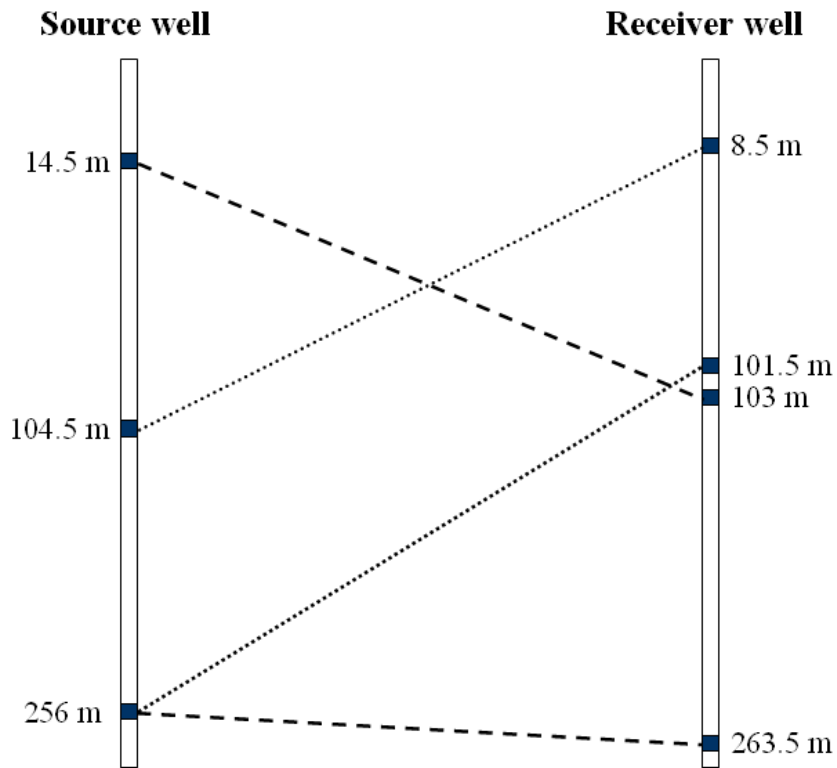
\mathbf{f}_s = centroid frequency at source normalized by variance

\mathbf{f}_r = centroid frequency at receiver normalized by variance

Methodology

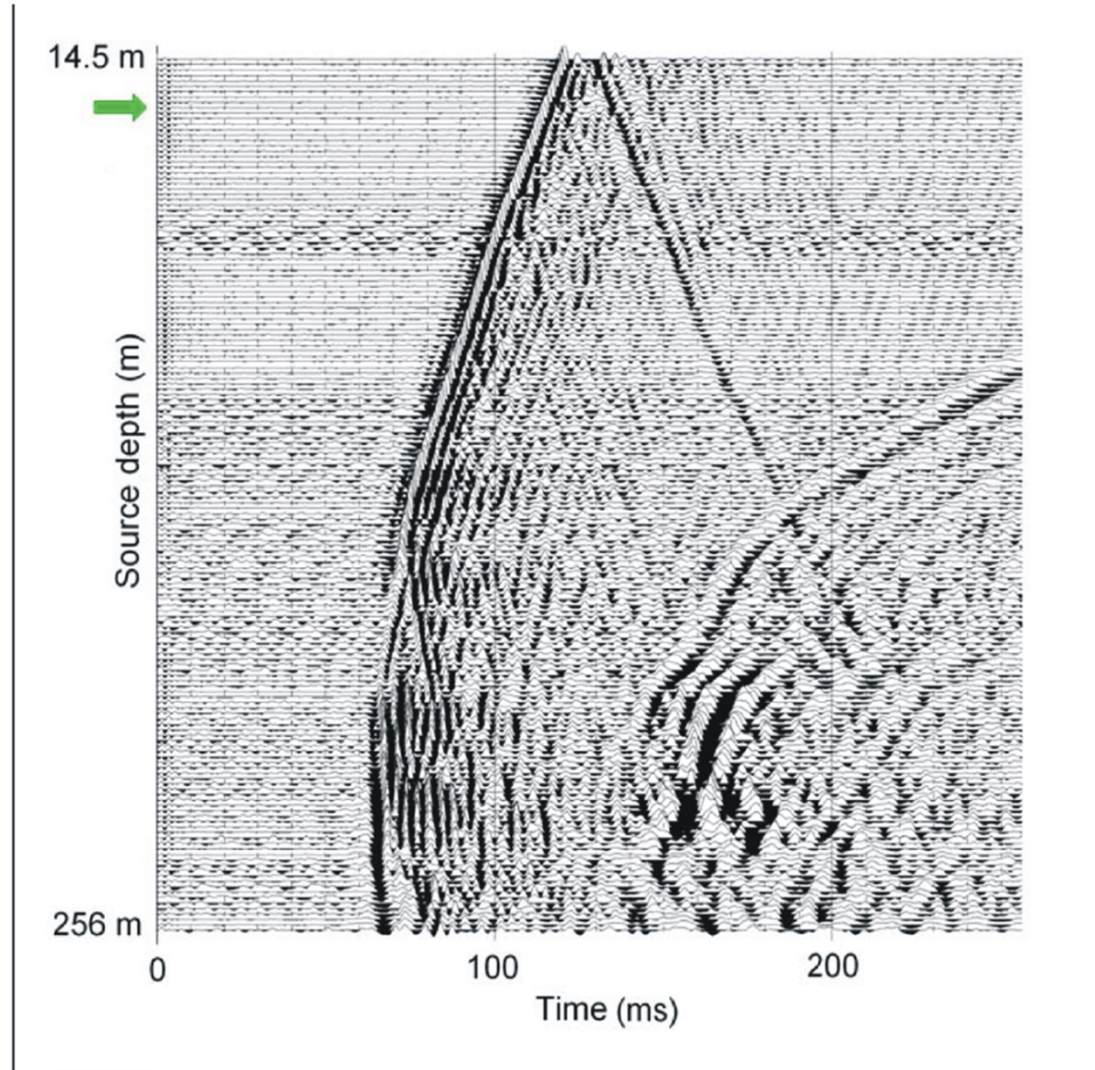


Crosswell Acquisition Parameters

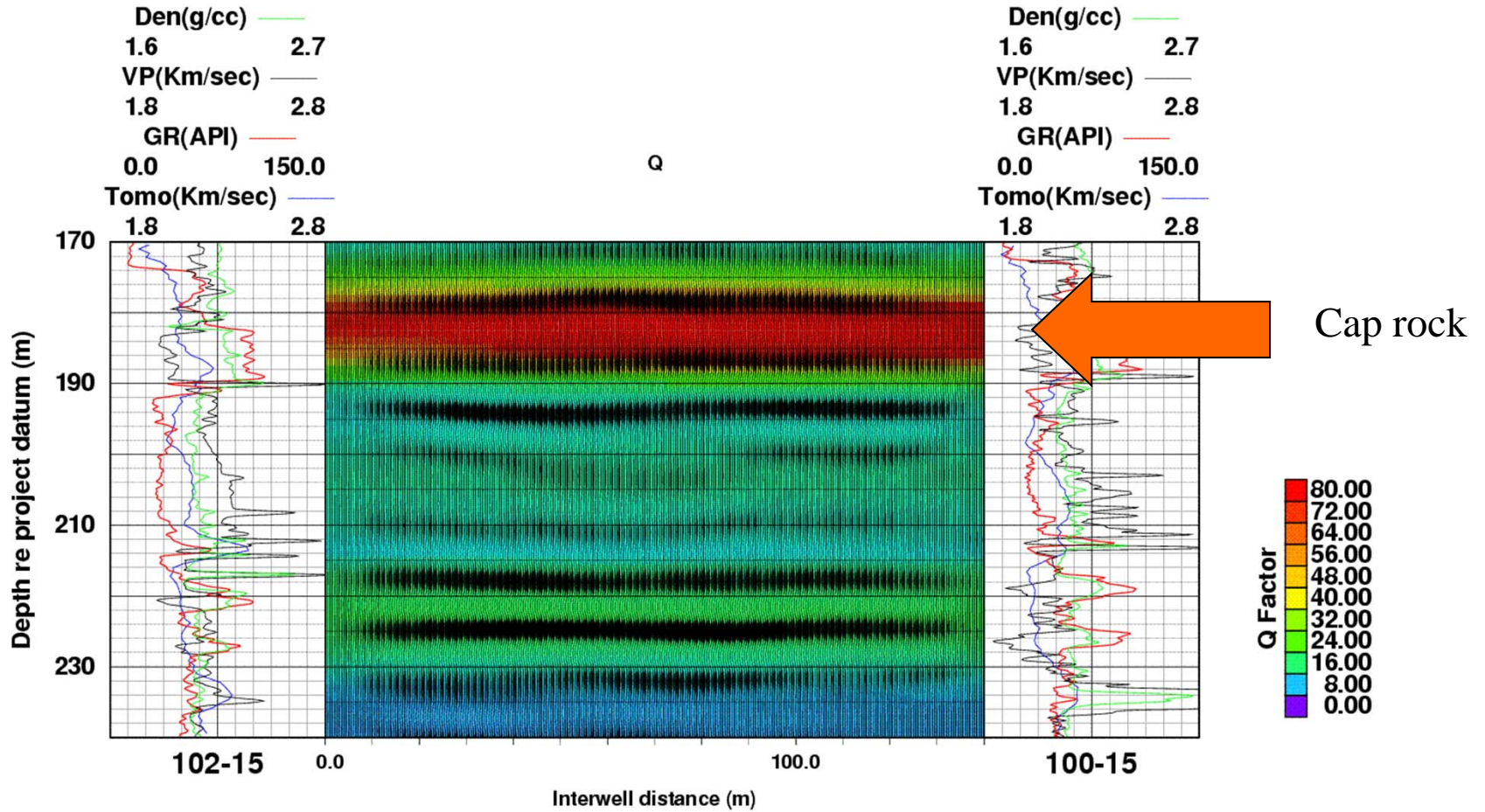


Well spacing	140 m
Receiver spacing	1.5 m
Source spacing	1.5 m
Frequency range	30-600 hz
Dominant frequency	420 Hz
Zone of interest	188-218 m

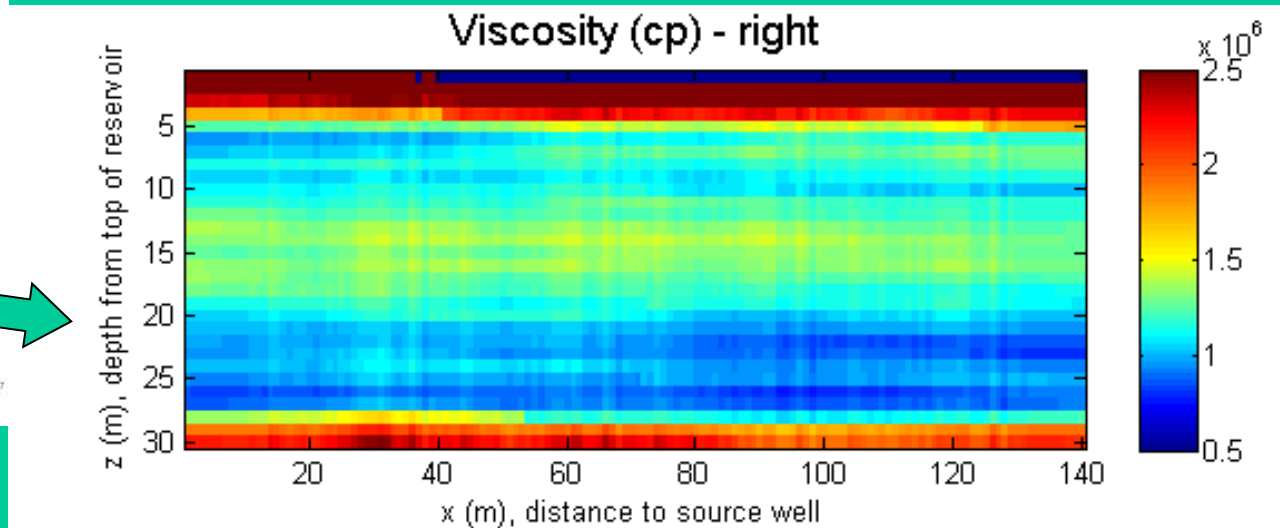
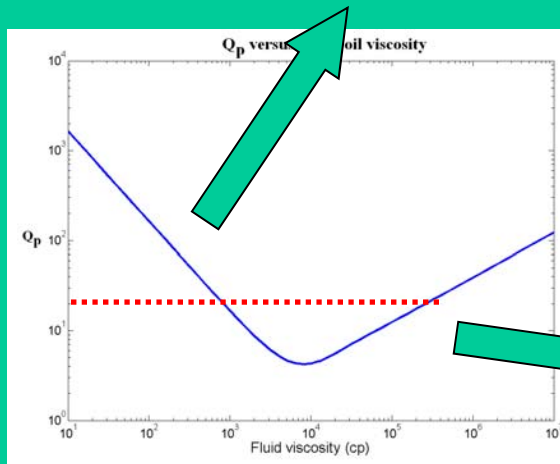
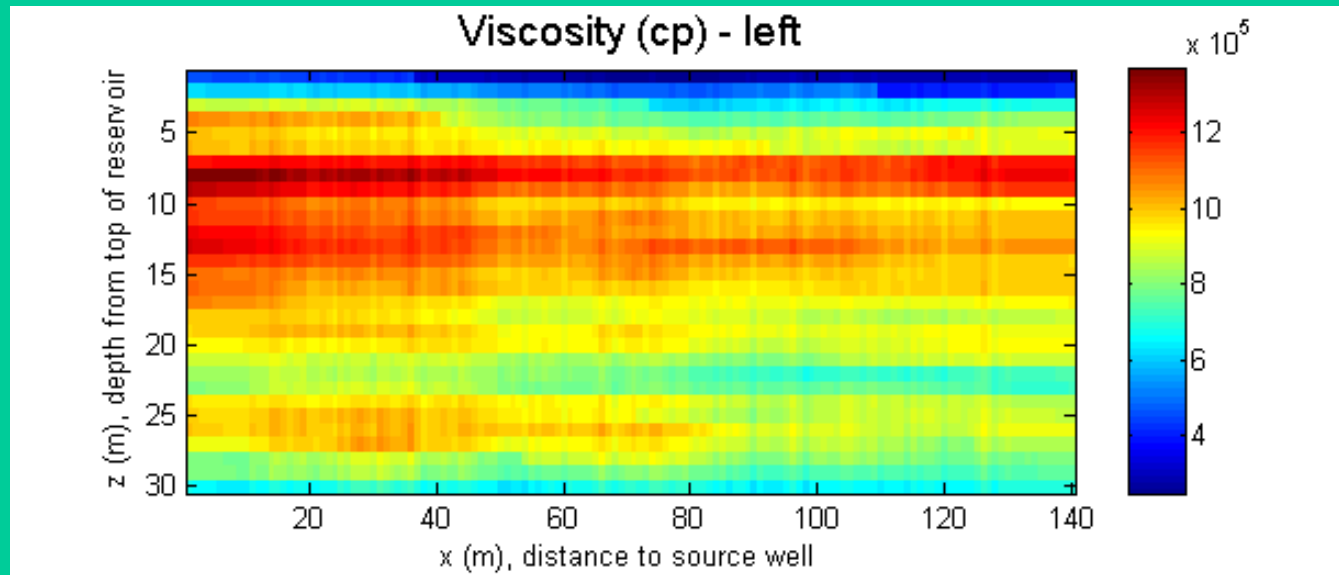
Crosswell Receiver Gather: Receiver Depth 205m



Quality factor



Viscosity: ambiguity

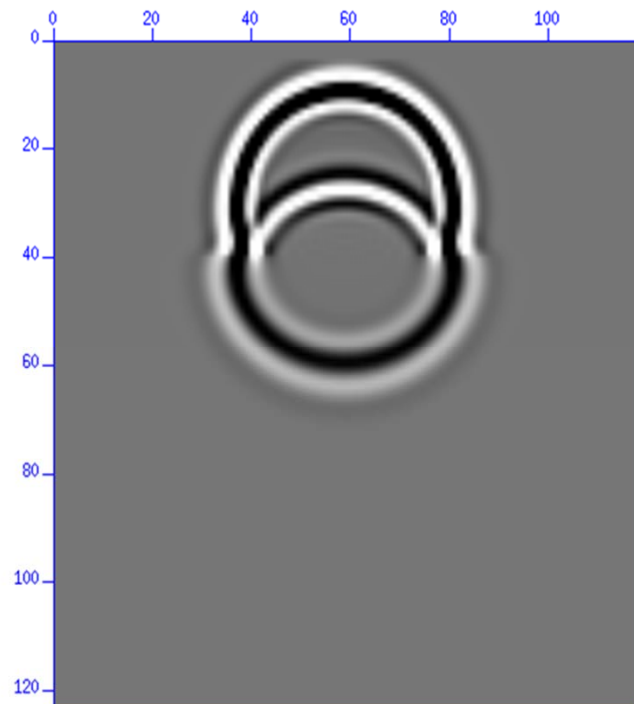


Full waveform inversion for estimation of seismic-Q

A model-based inversion method.

Finite-difference modeling

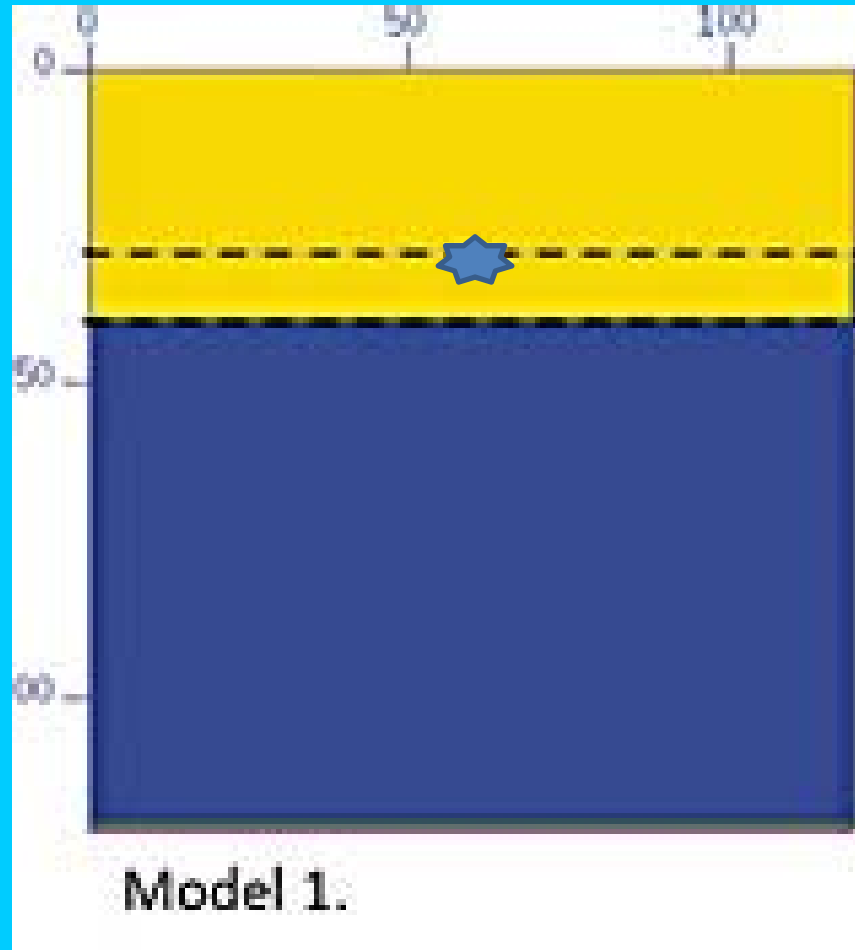
- Tests were done using finite-difference Fortran code from Carcione (2007).



impedance model snapshots

Two-layer model to illustrate reflections due to impedance and Q contrasts

- Use Shot at grid point (60,30)
- Use line of receivers at varying depths with receiver spacings of 1 grid point
- In models vary the impedance for yellow layer and blue layer

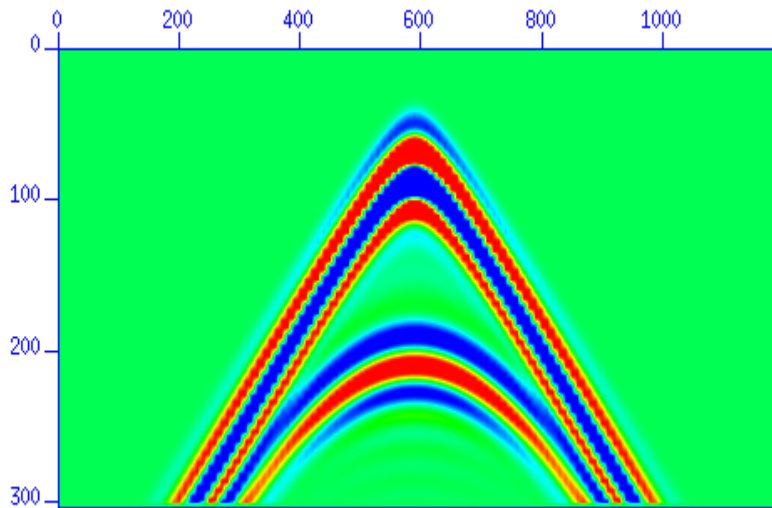


Reflections on Impedance

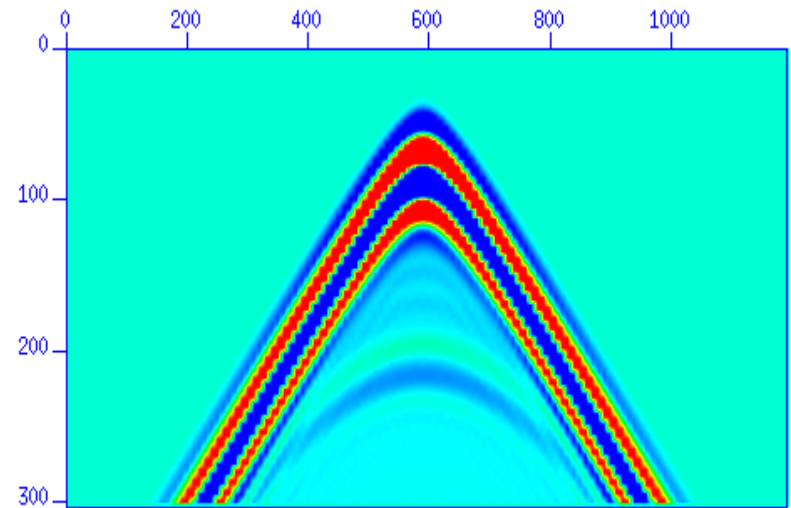
- The reflections from contrasts in the real component of impedance (density*velocity) will be much greater than reflections from Q contrasts.
- Consider case for source at grid (60,30) and line of receivers at row 25, giving rise to reflections.

Comparison of Impedance-only contrast and Q-only contrast

- Model 1 (left). Layer 1 impedance = 1500000; Layer 2 impedance= 5000000; Q = 210000 for both layers.
- Model 2 (right) Impedance constant; Layer 1, Q=210000; Layer 2 Q=2*pi. (Scale factor = 100.)



Q contrast-high gain



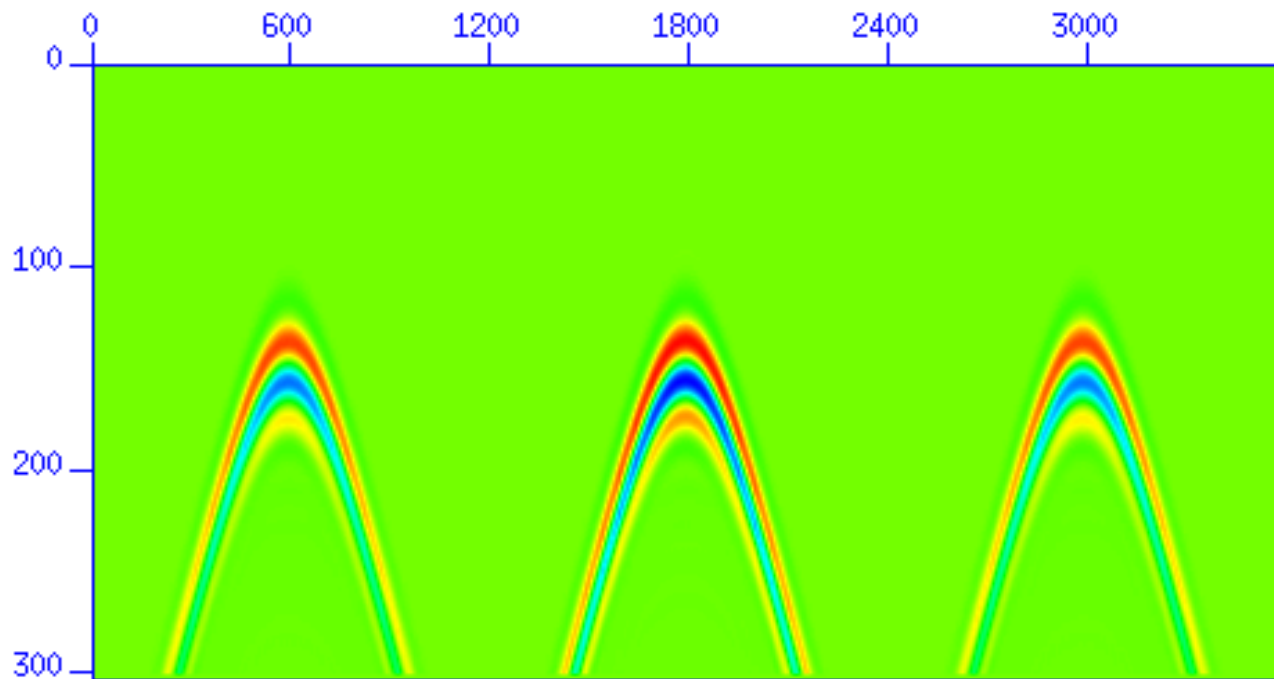
Q contrast-high gain

Use seismograms dominated by transmitted arrivals to estimate Q

- The reflections from contrasts in the real component of impedance (density*velocity) will be much greater than reflections from Q contrasts.
- Nevertheless all transmitted and reflected arrivals are used in full waveform inversion.

Convergence of Inversion

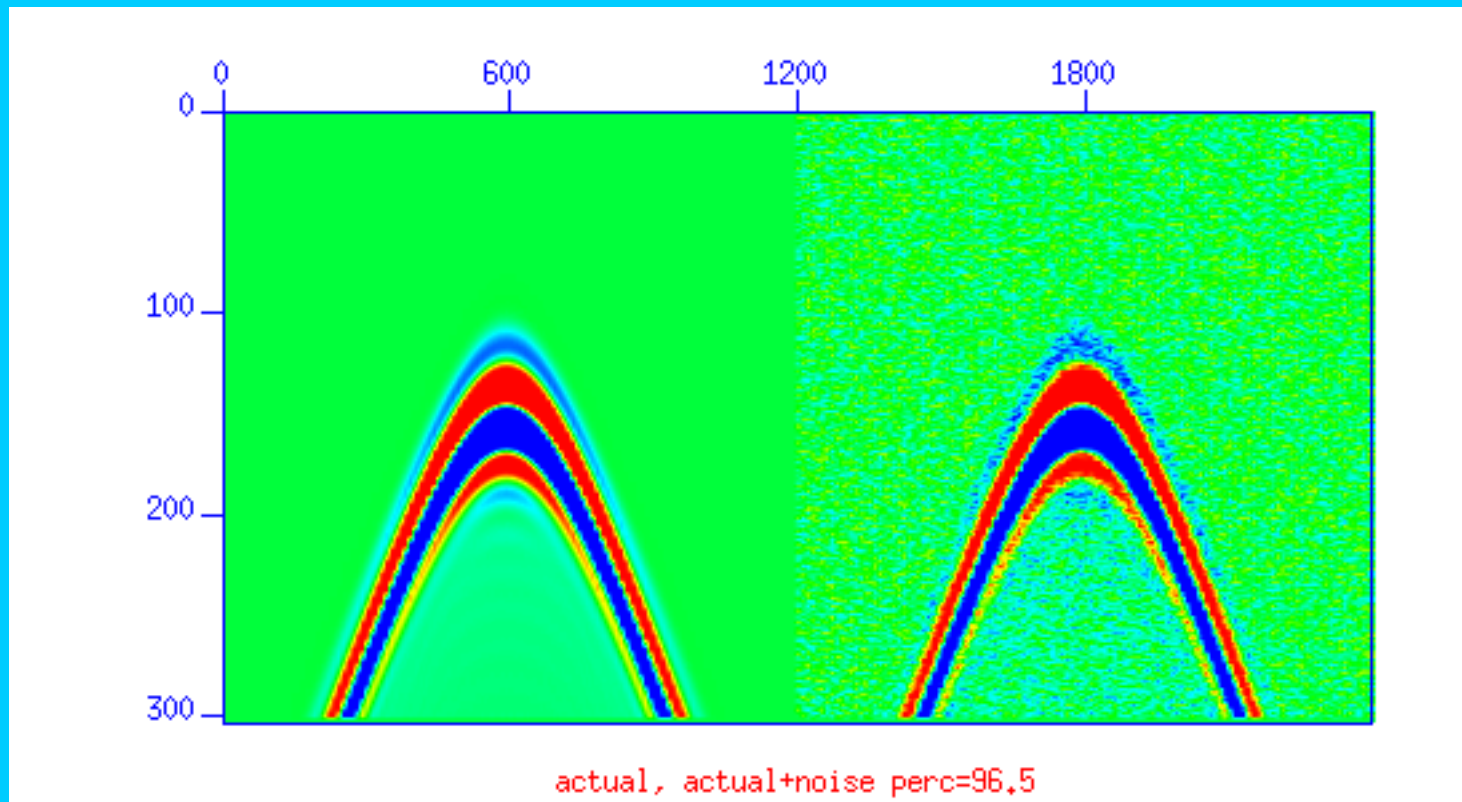
- Model responses for input data ($Q=6.28$), initial guess ($Q=15$), and converged answer ($Q=6.09$)(after 3 iterations).



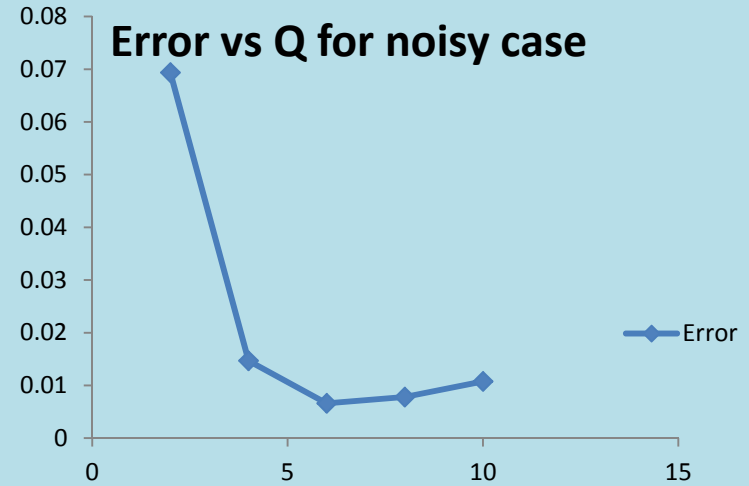
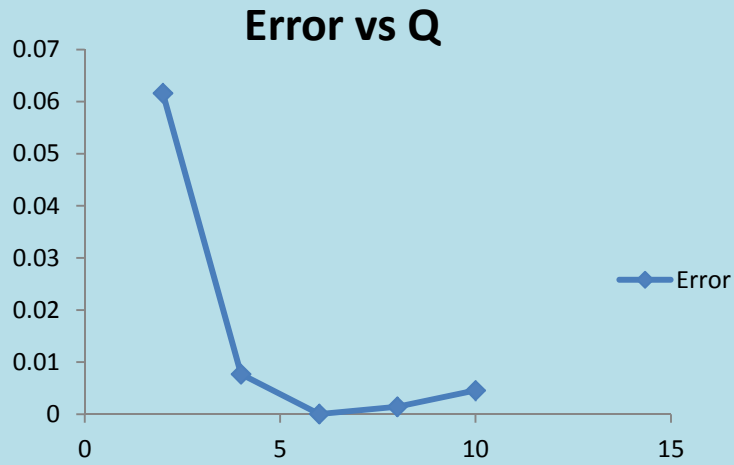
actual, initial, convergence

Effect of Modest Levels of Additive Noise on Full Waveform Inversion

- Compare inversion solutions for pure signal versus solutions with small amounts of noise (S/N in signal zone about 5).

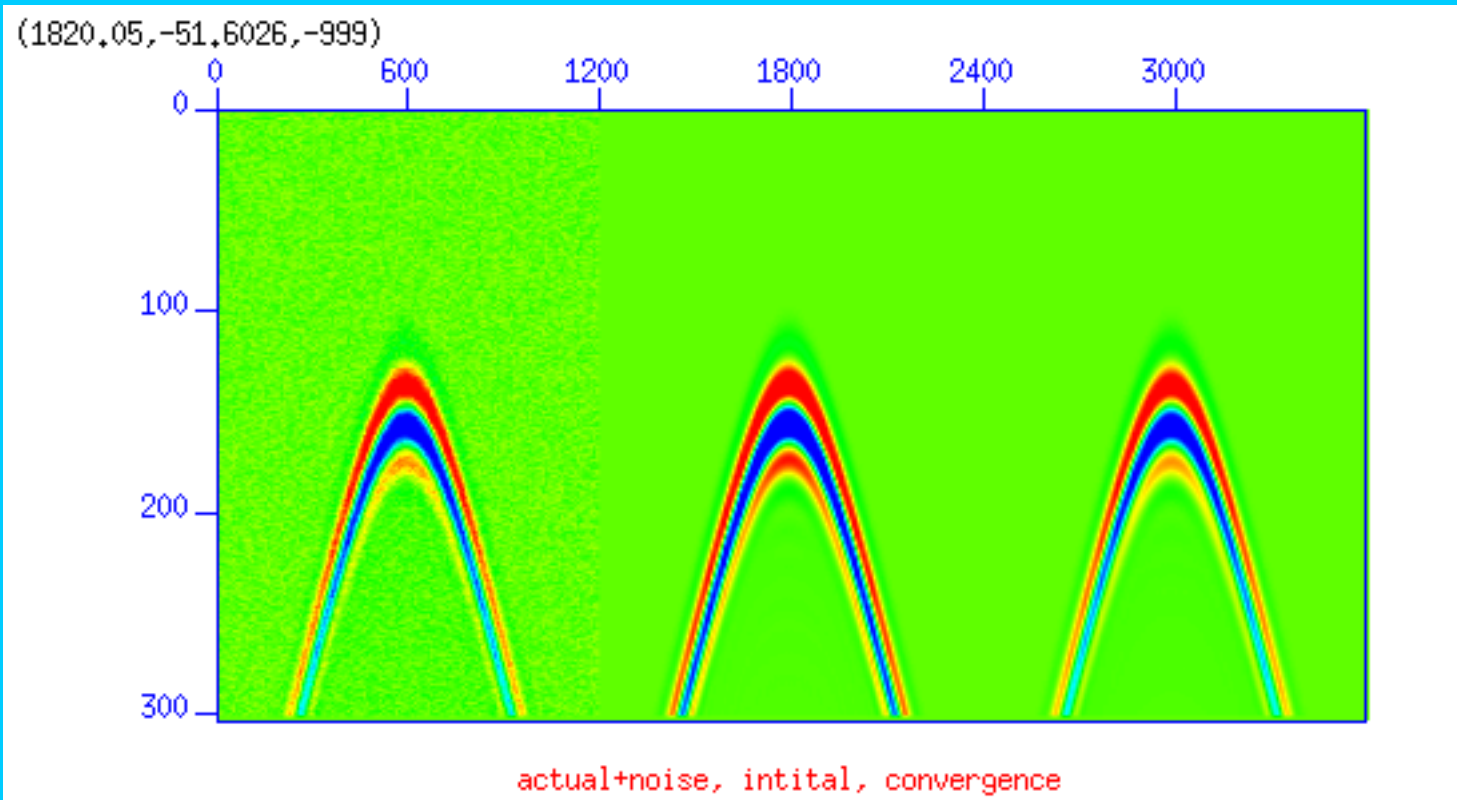


Error vs Q value



Convergence of Inversion

- Model responses for input data + noise ($Q=6.28$), initial guess ($Q=15$), and converged answer ($Q=6.33$)(after 3 iterations).



Preliminary Results

- Full waveform inversion for these simple Q-estimation problems is not overly sensitive to additive noise with zero mean.

$$A^T A \Delta x = A^T (b + n)$$

- $A^T n \rightarrow 0$ if noise, n , is random with zero mean.
- Error of data fit deteriorates slightly with noise but accuracy of Q estimate is consistent.

Conclusions

- Heavy oils are considered viscoelastic materials and their shear properties are important.
- Both theory and measurements show that Q has a decreasing-increasing behavior with viscosity.
- Q -tomography and full waveform inversion methods can be effectively used for Q -estimation.
- The inversion methods could be used in sequence with tomographic results being used as input for full waveform inversion.
- Full waveform inversion produces Q estimates based on the entire waveform. FWI appears to be robust for noisy data with moderate amounts of noise.
- More model and real data tests are needed.

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