

IMMI: the role of well calibration in the context of high geological complexity

Sergio Romahn

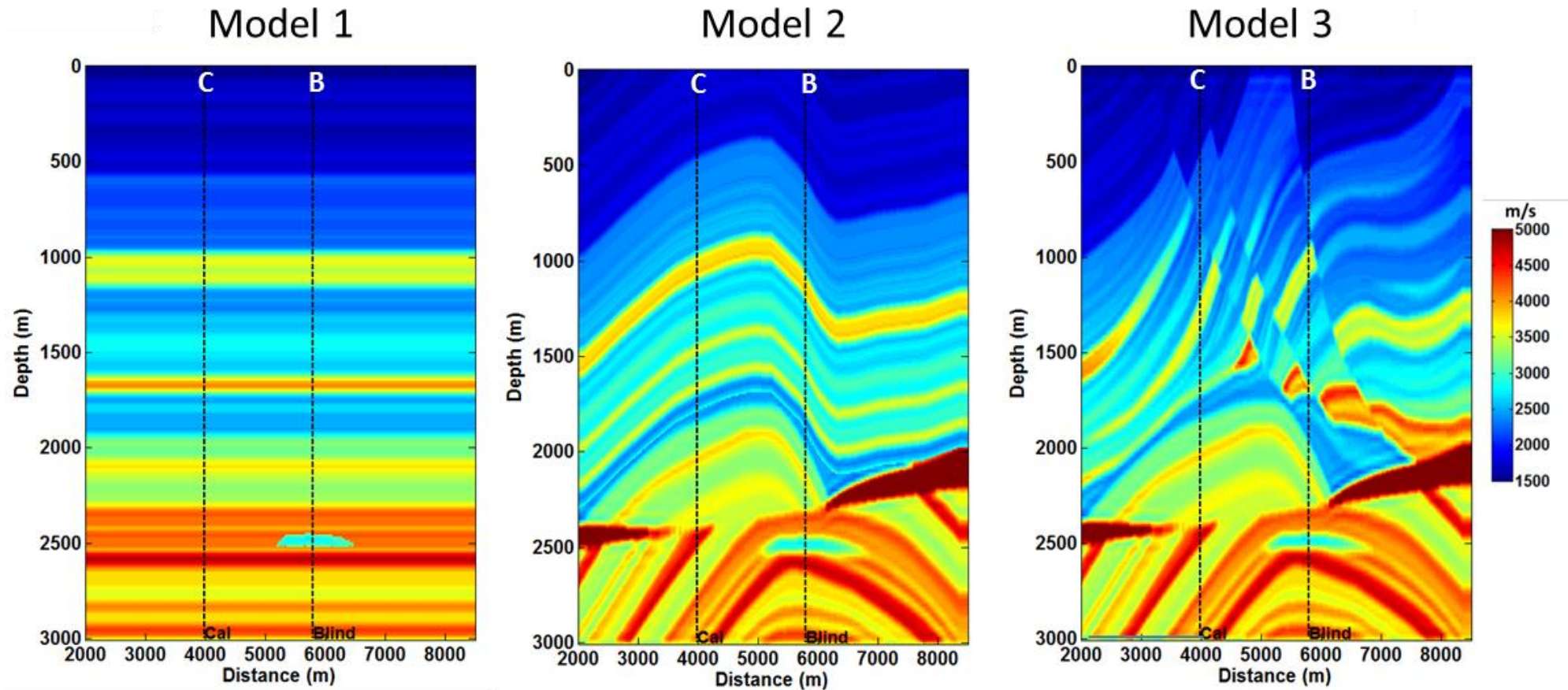
Kris Innanen

Dic-2017

- Introduction
 - IMMI
 - Objective
- FWI process
- Well calibration
- Conclusions
- Future work

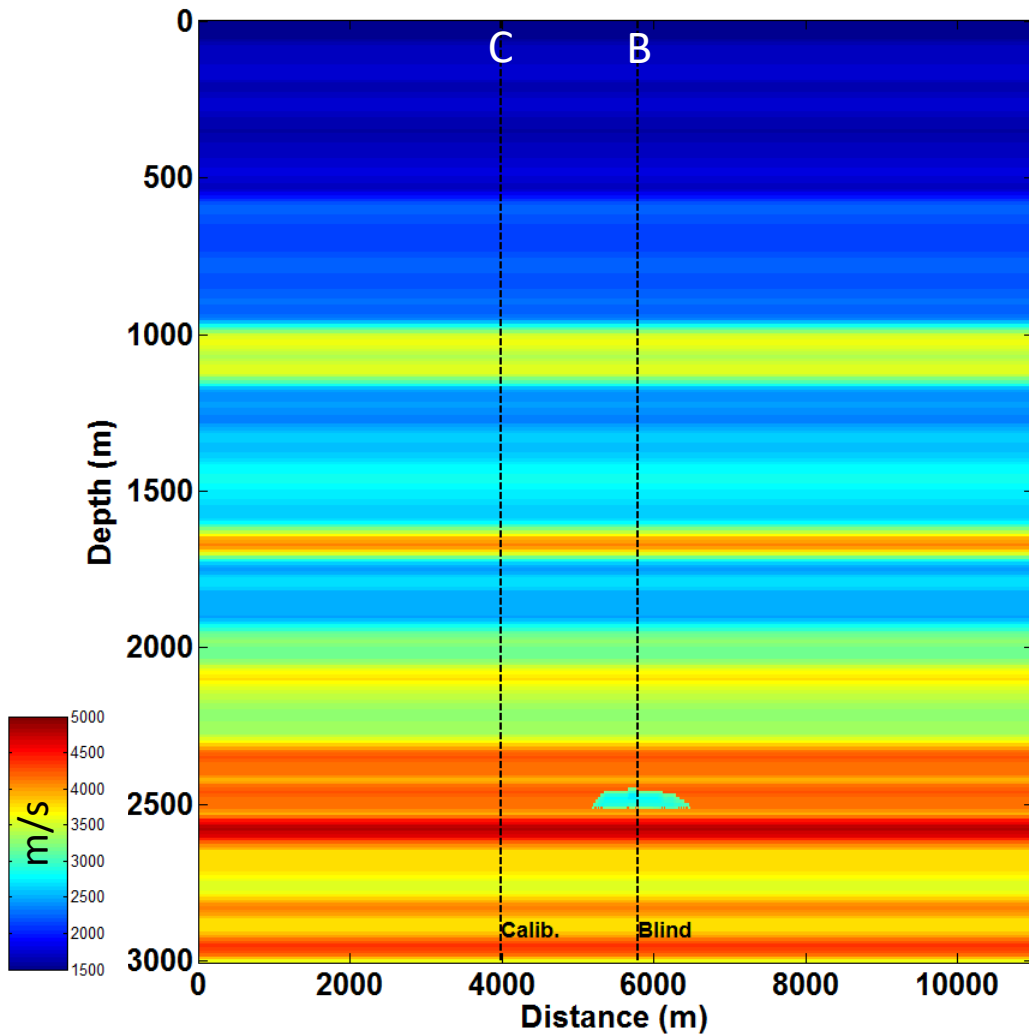
- IMMI was introduced by Margrave, Innanen, & Yedlin in 2012 (chapter 70, CREWES report).
- IMMI stands for iterative, modelling, migration and inversion, which can be seen as the cycle of FWI.
- IMMI proposes the incorporation of standard processing techniques into the process of FWI.
- Examples of IMMI's approach are the use of any migration method to obtain the gradient and the use of well velocity to calibrate it.

To evaluate the role of well calibration in the context of increasingly complex geology

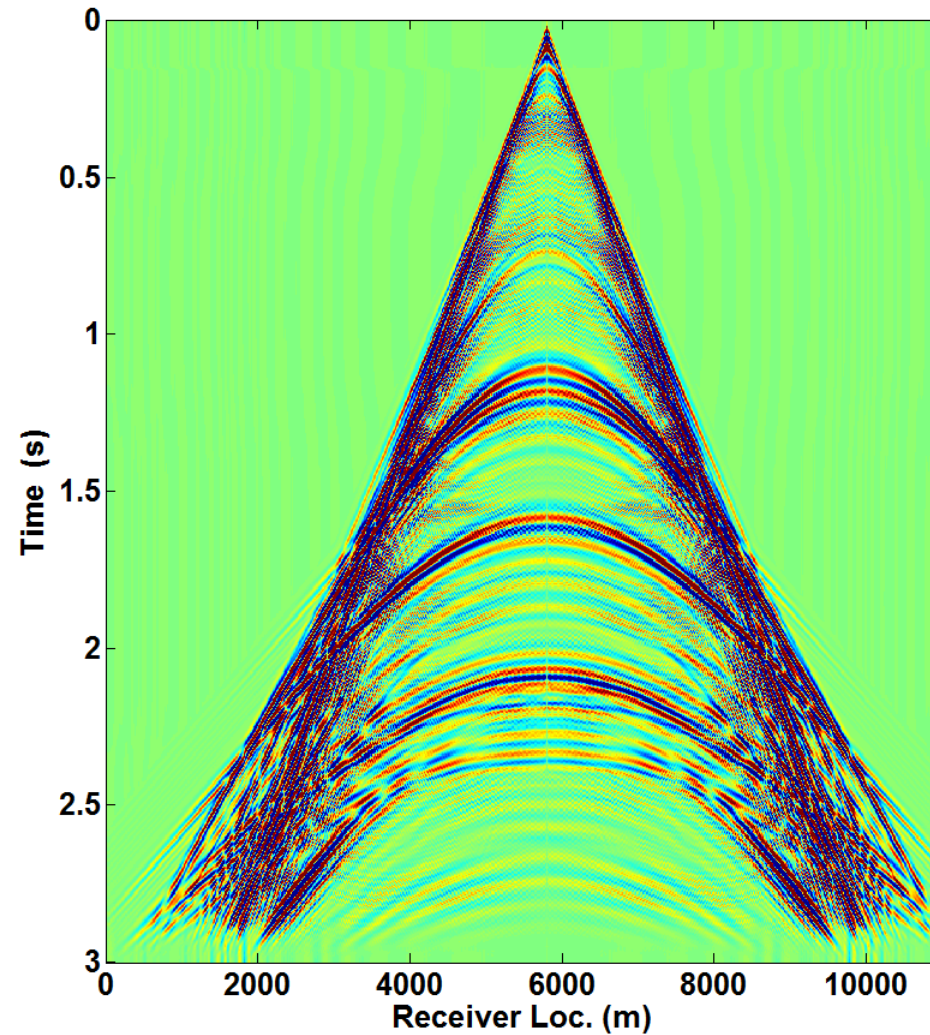


FWI process

Model 1



Observed shot



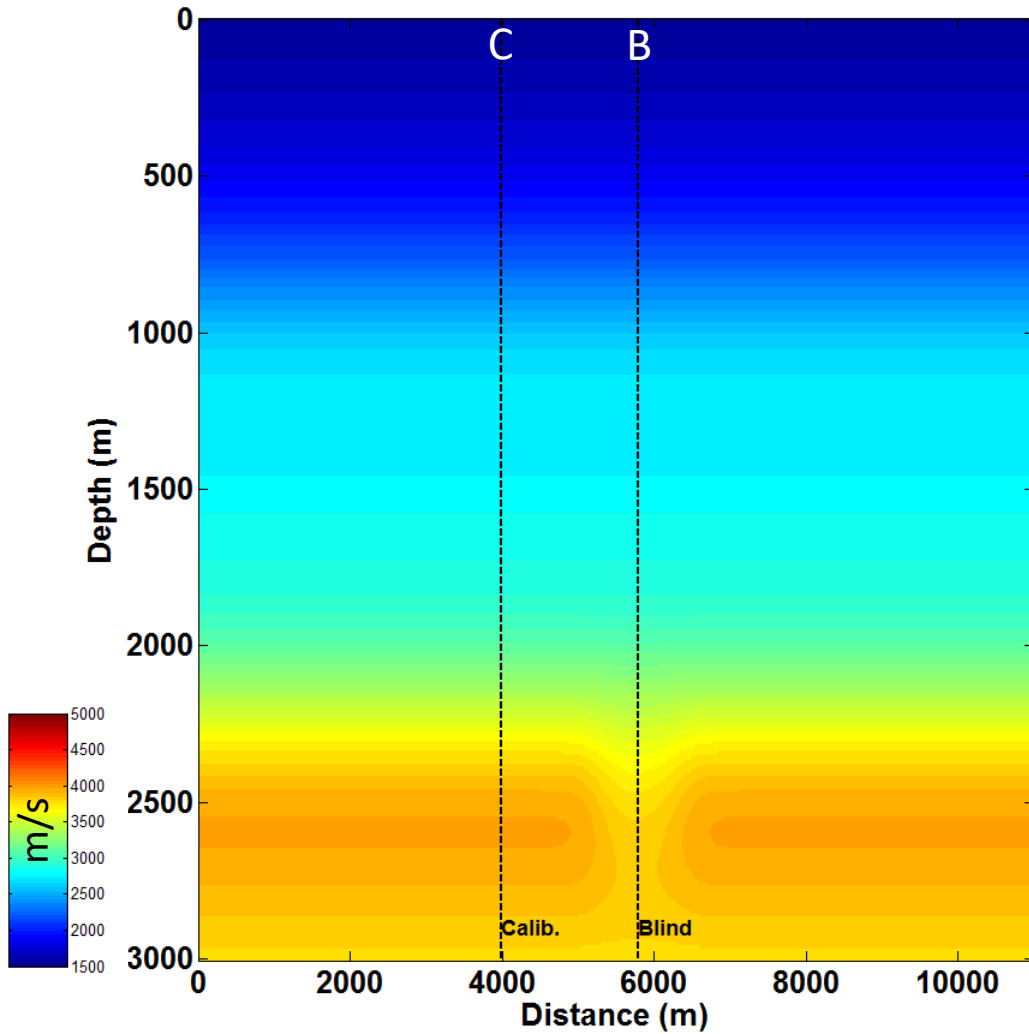
Minimum
phase
wavelet

$f_{\text{dom}} = 20 \text{ Hz}$

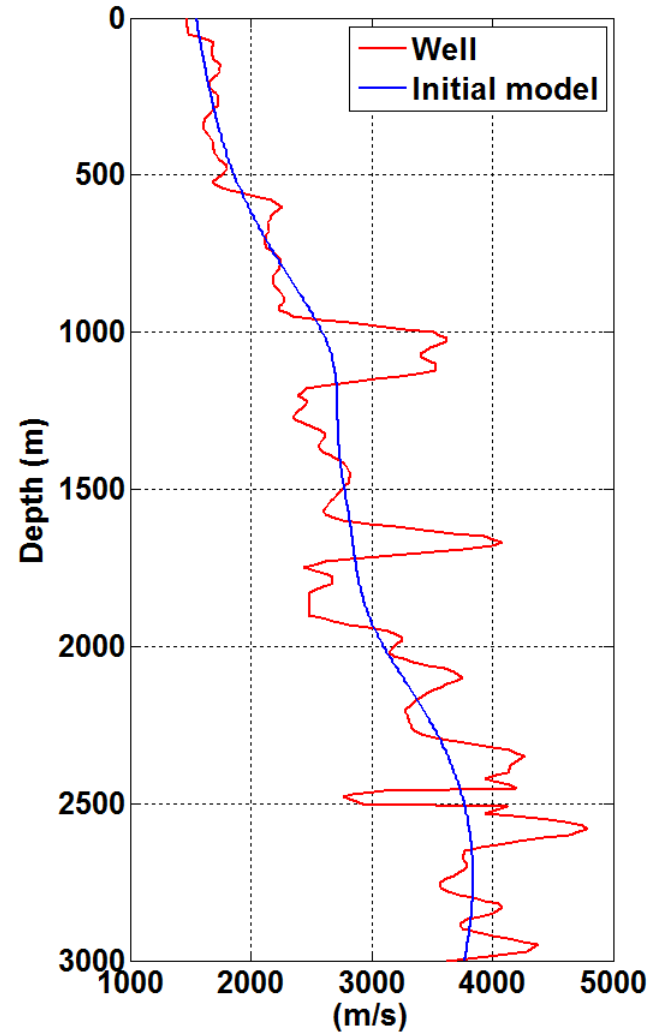
1st step: Modelled shots

Inversion process

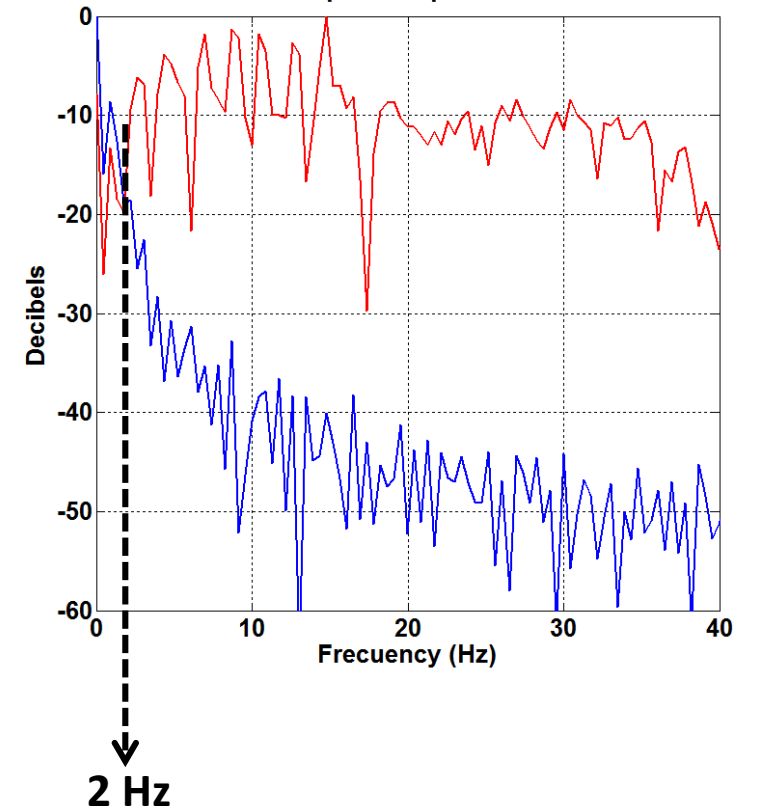
Initial model



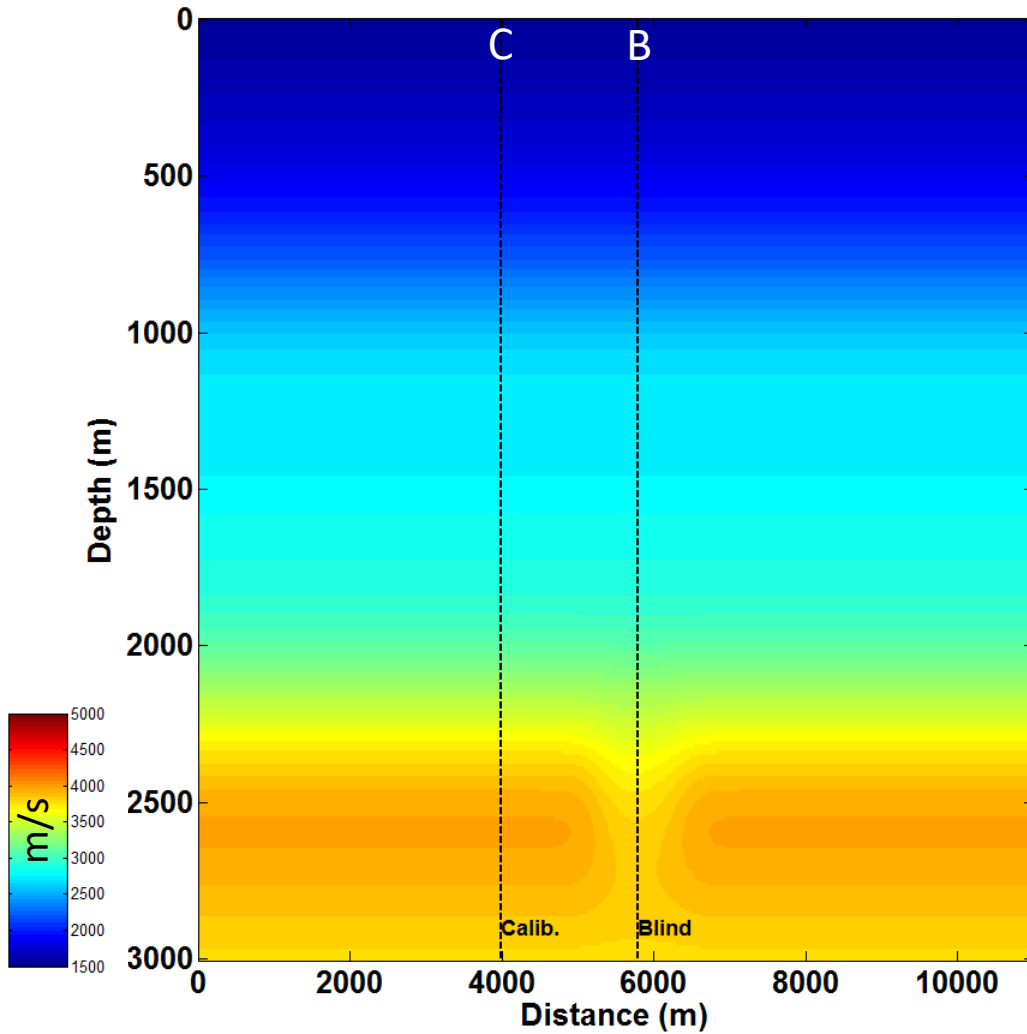
Velocity in well B



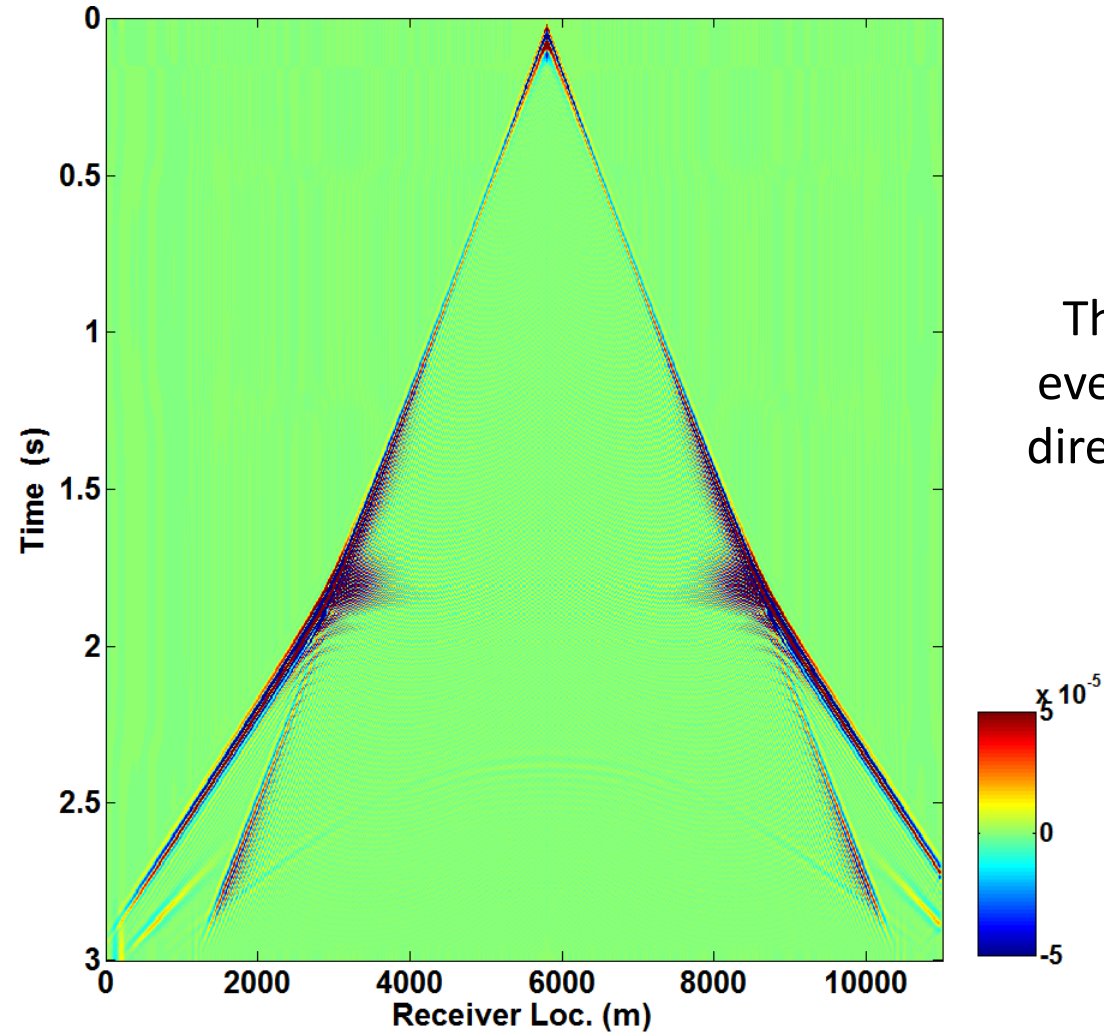
Reflectivity amplitude spectra



Initial model

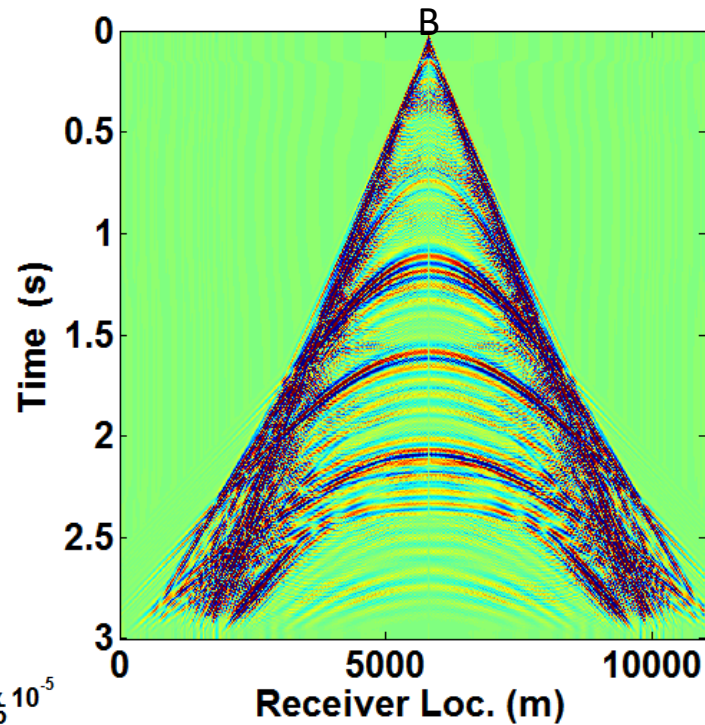


Modelled shot

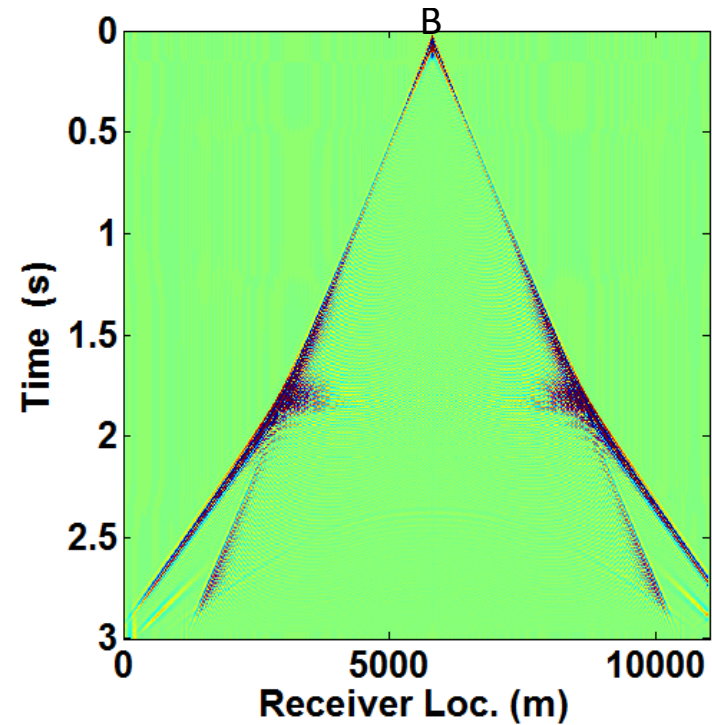


The main event is the direct arrival

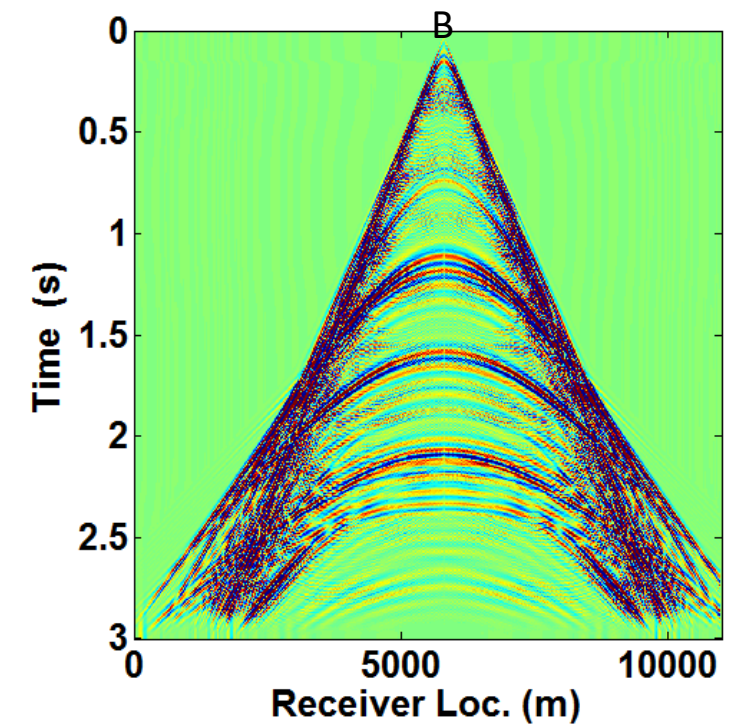
Observed shot

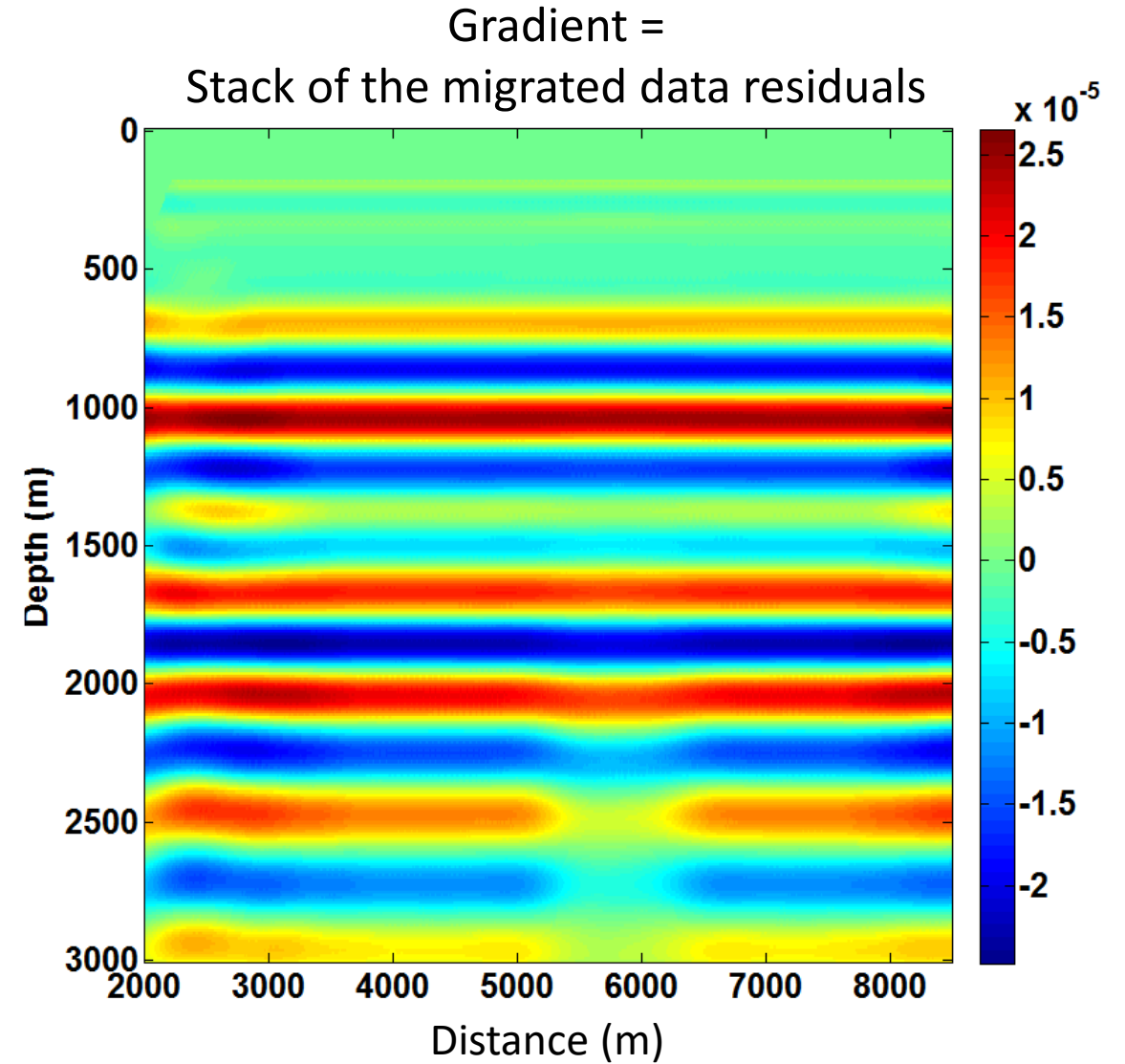
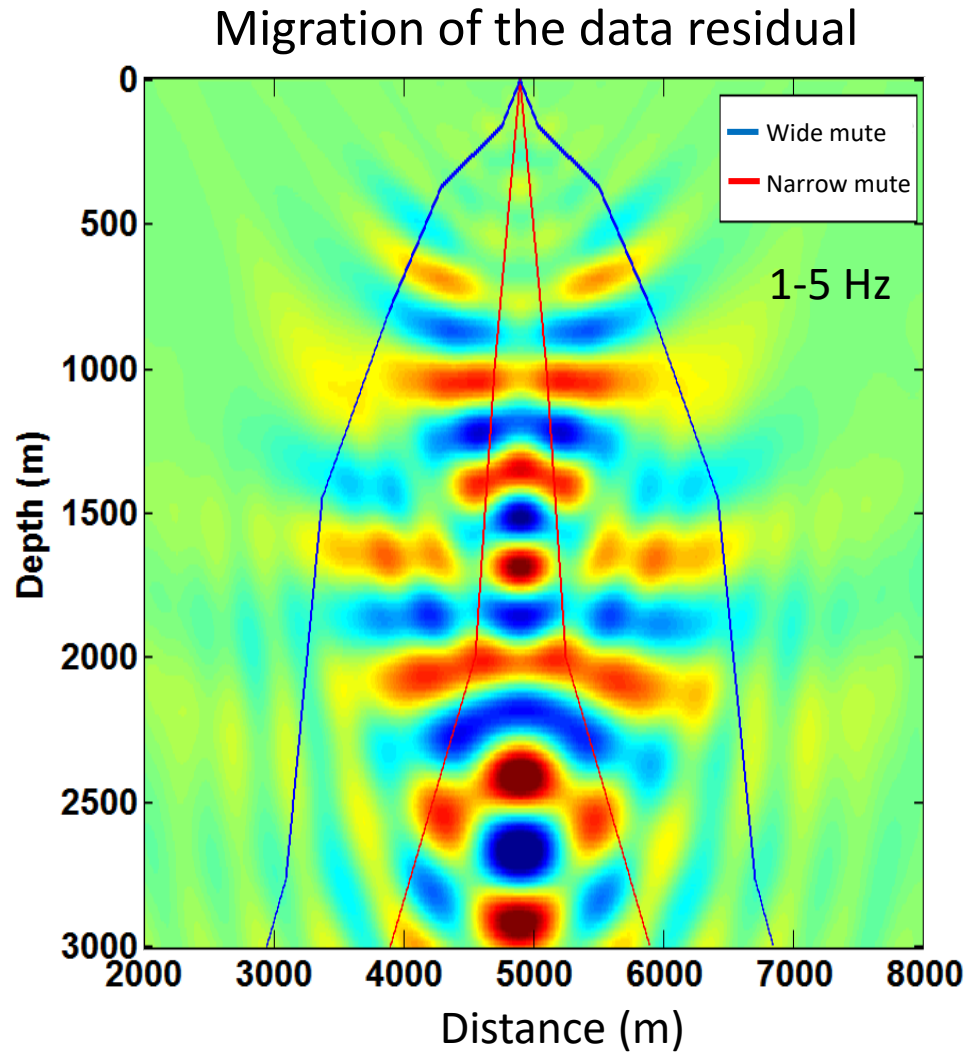


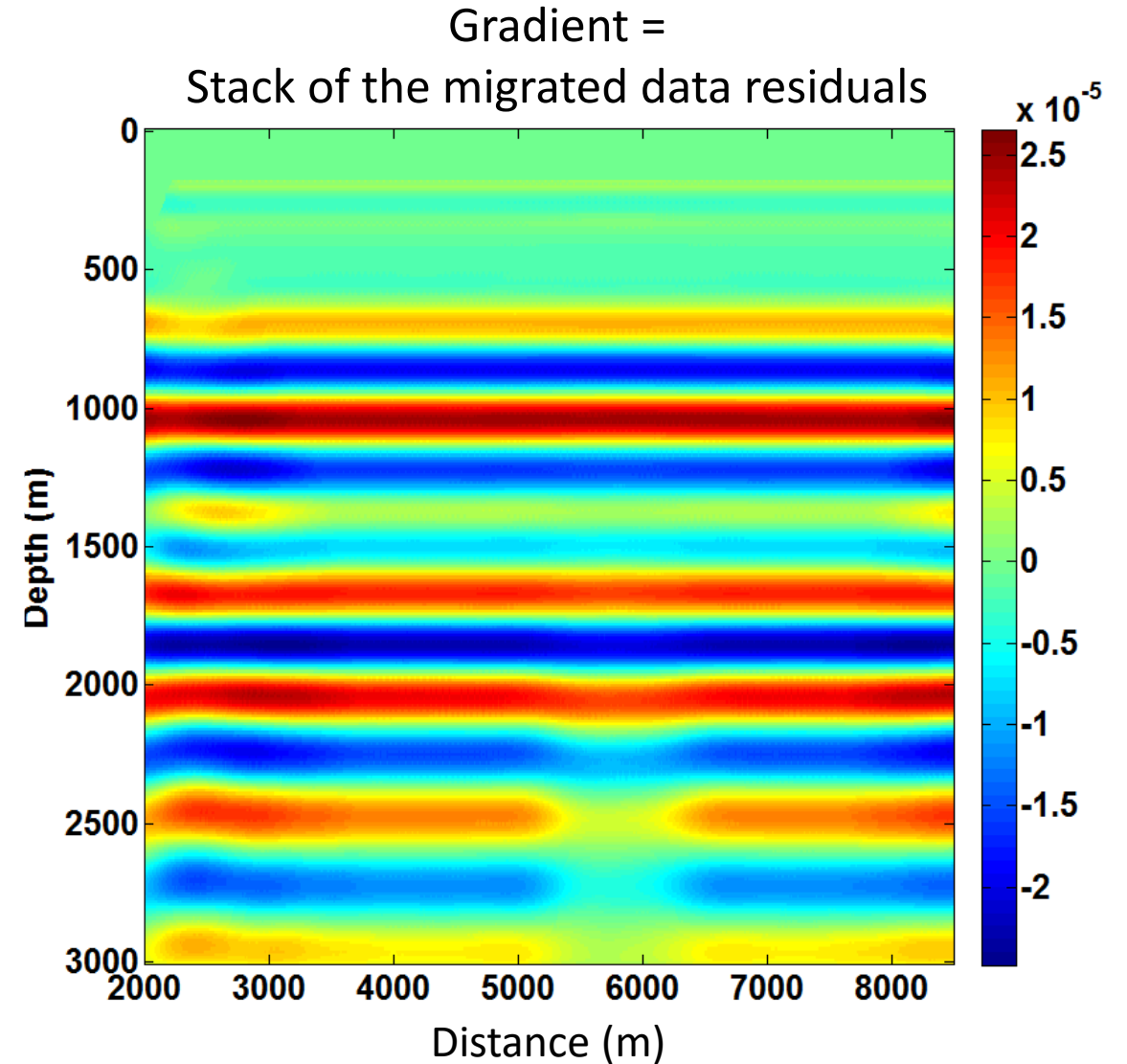
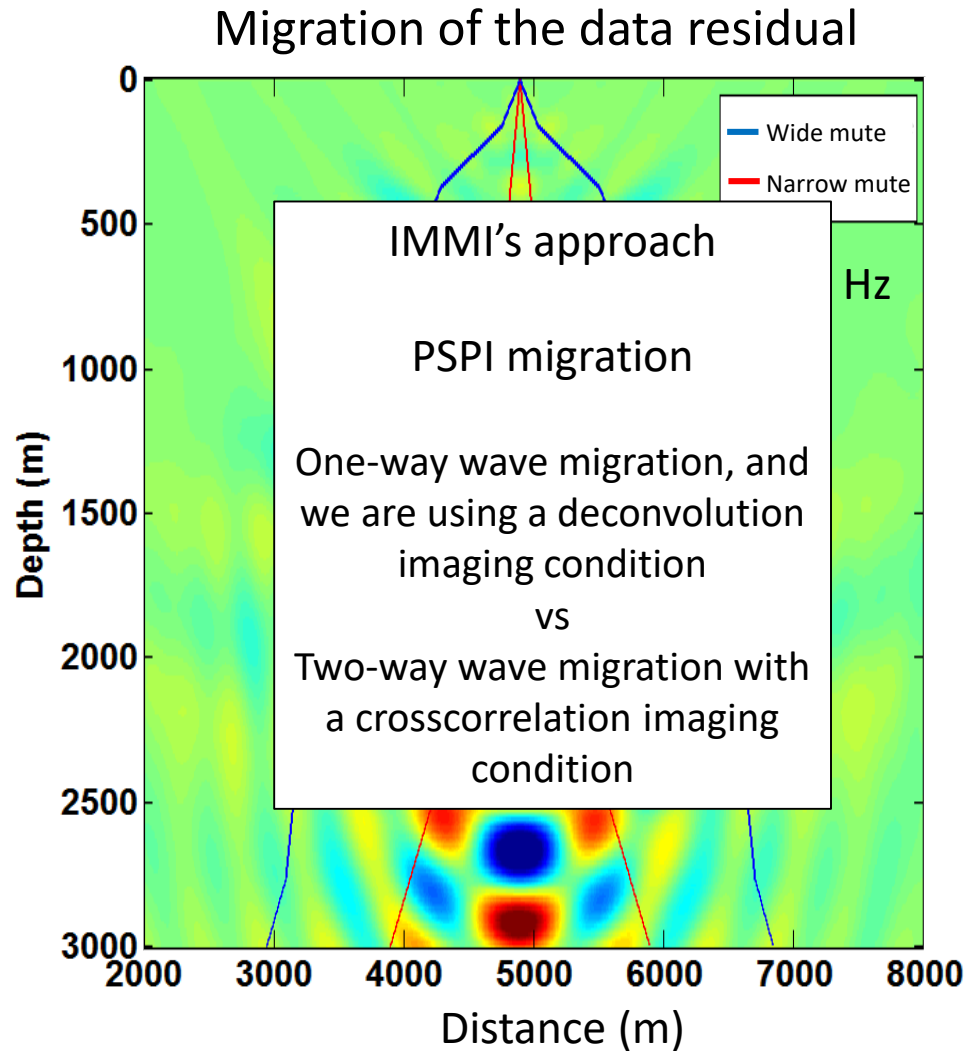
Modelled shot



Data residual





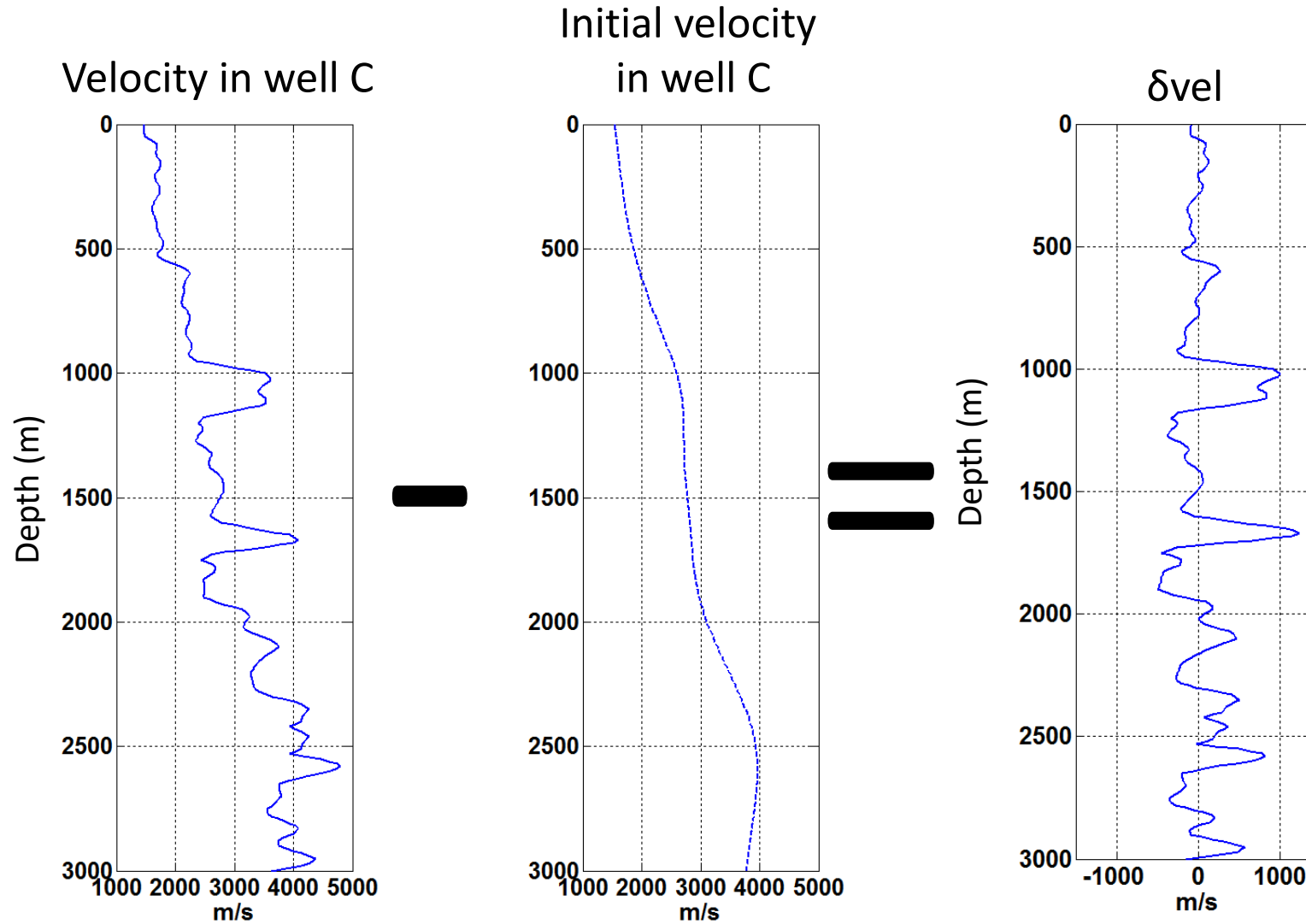


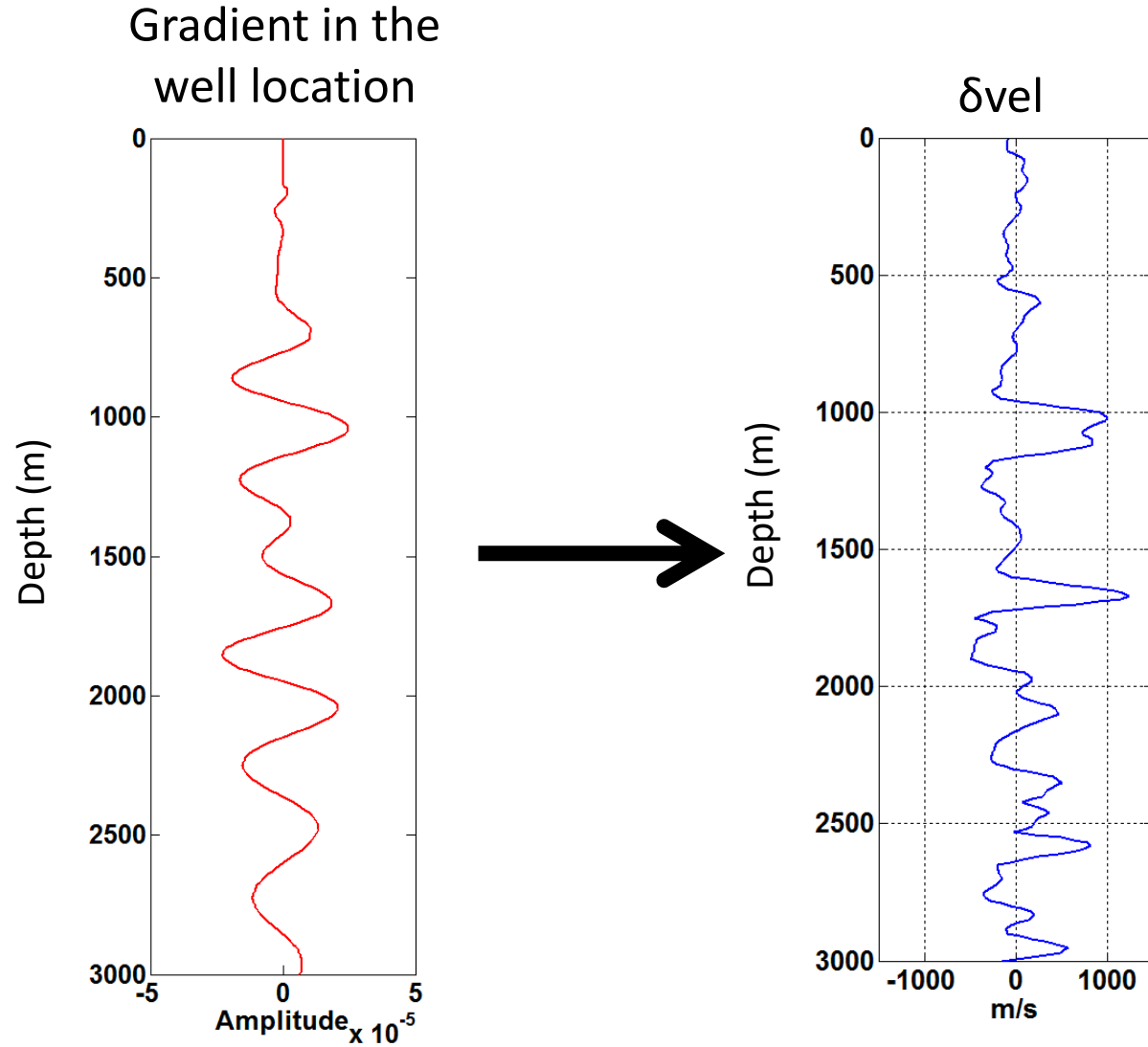
IMMI's approach

Well calibration

vs

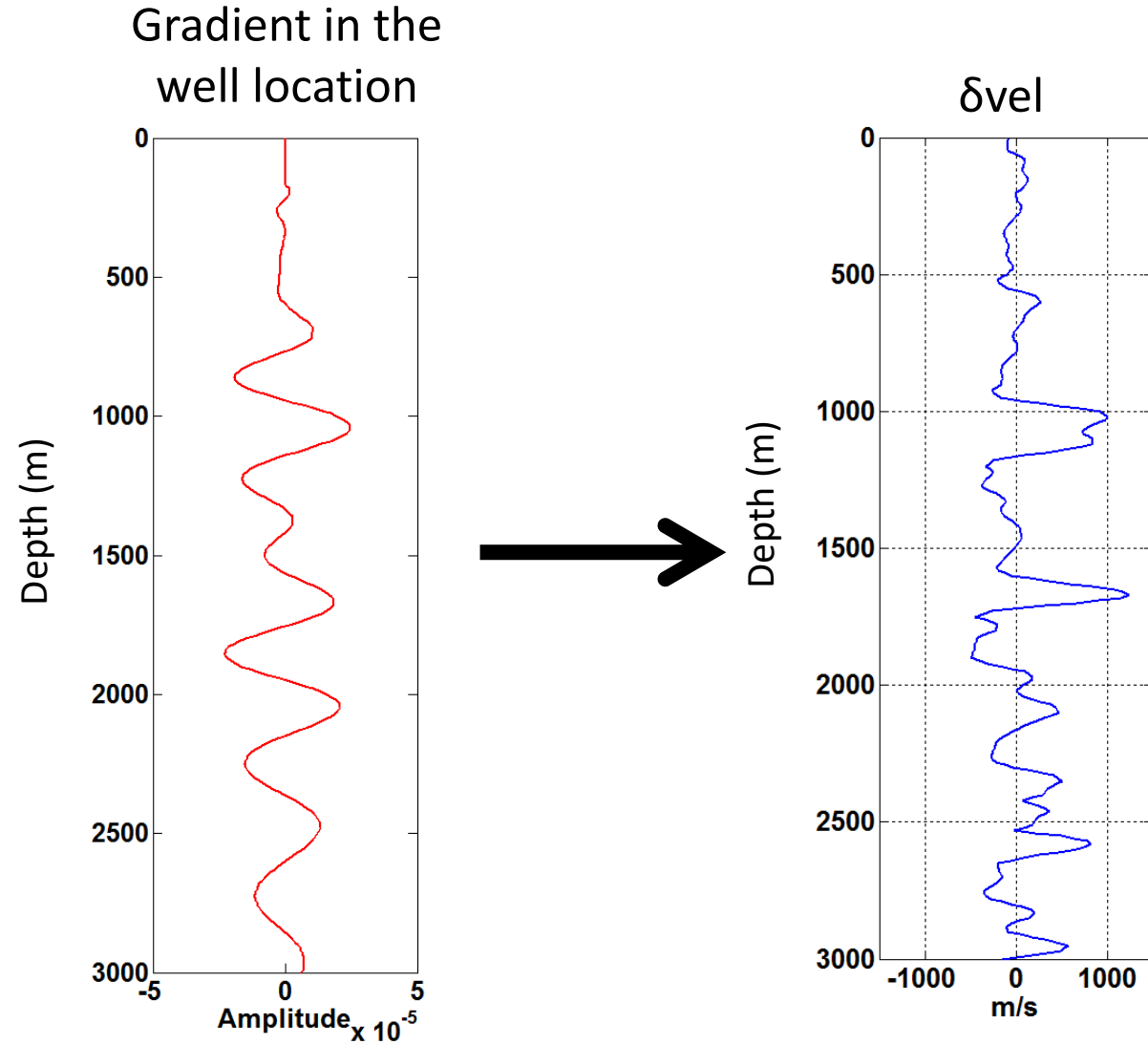
Line search method or an approximation of the inverse Hessian matrix

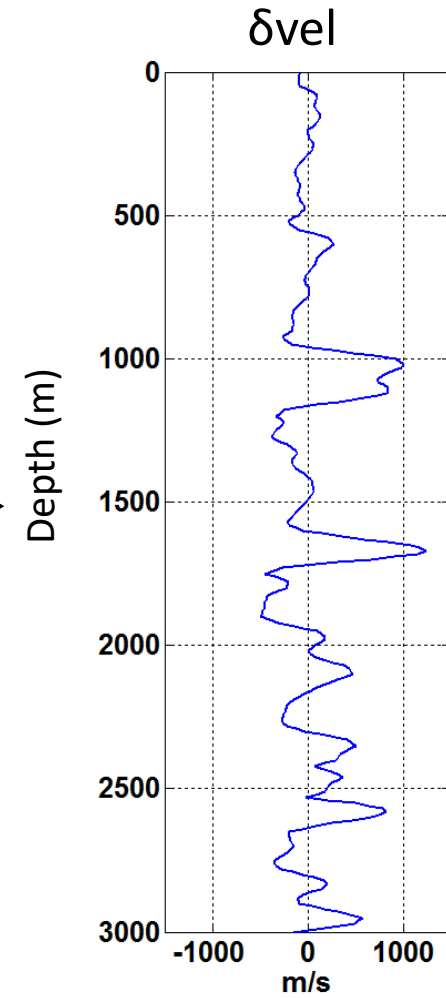
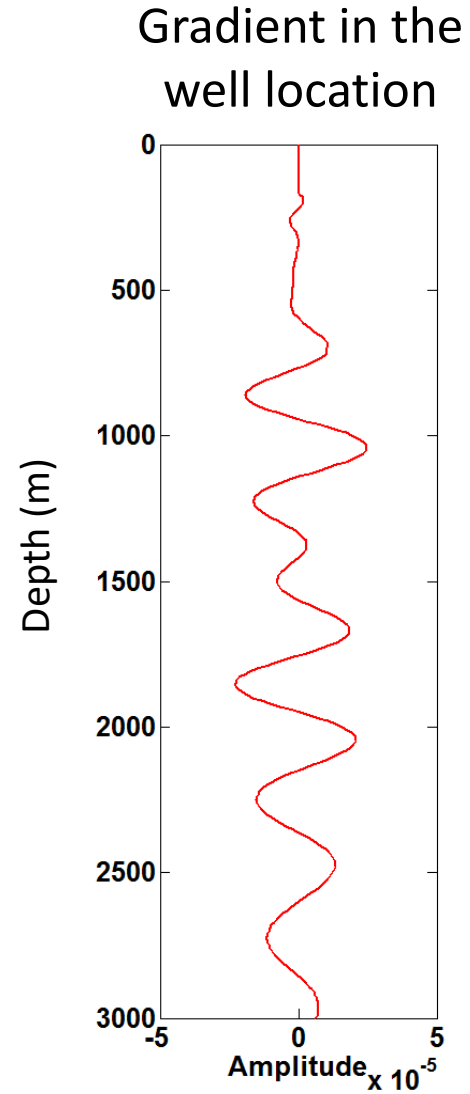
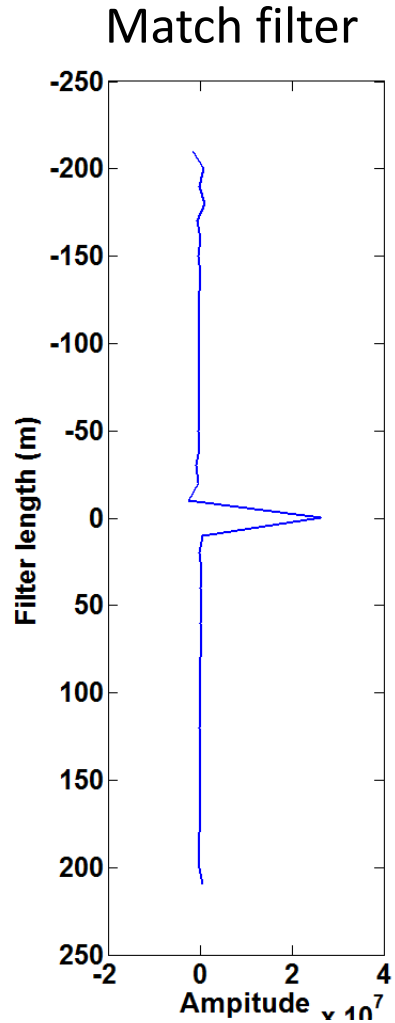




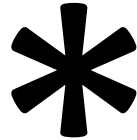
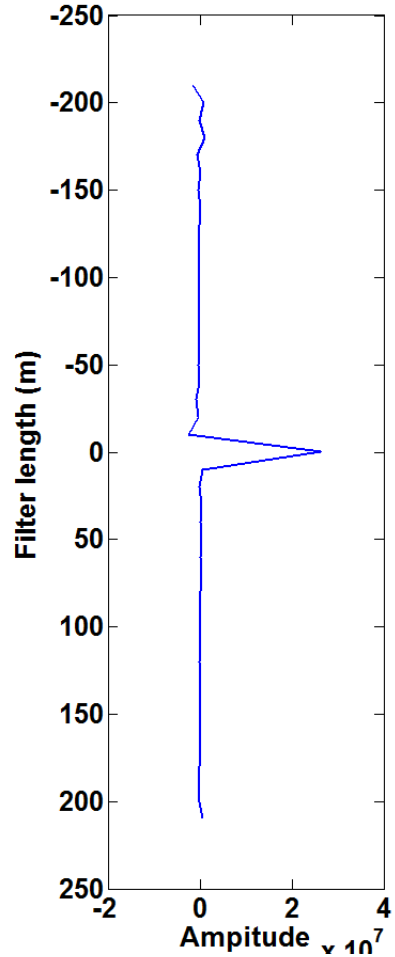
An Amplitude scalar a so that $\delta vel - ag$ is minimized by least squares

A phase rotation φ , so that, δvel and the calibrated gradient have a similar phase



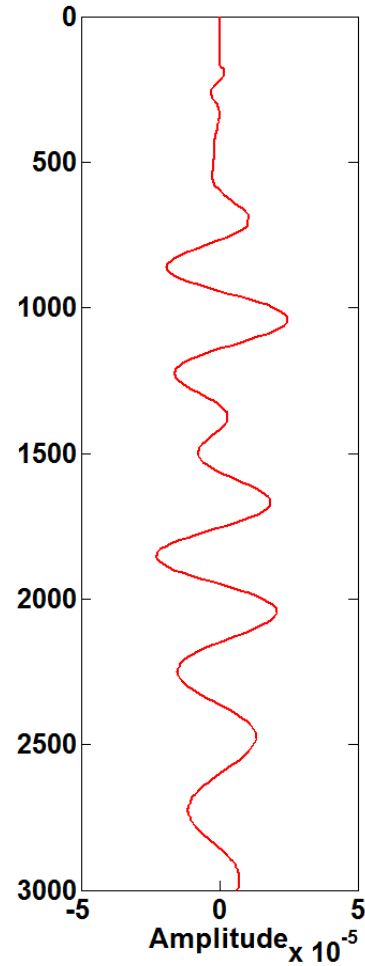


Match filter

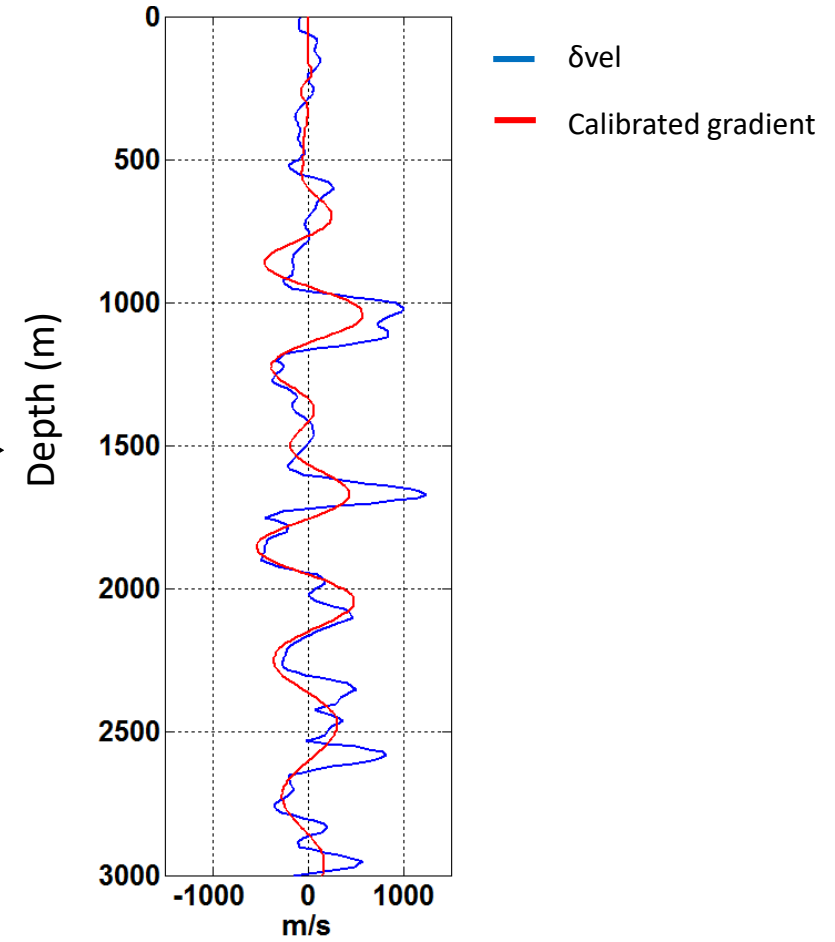


Depth (m)

Gradient in the well location



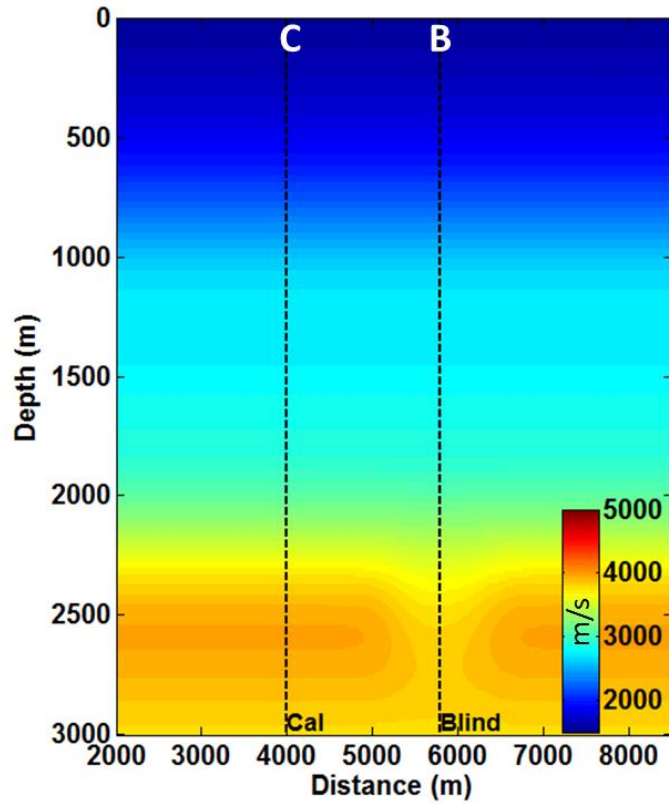
δ vel and calibrated gradient



4th step: Updated velocity model

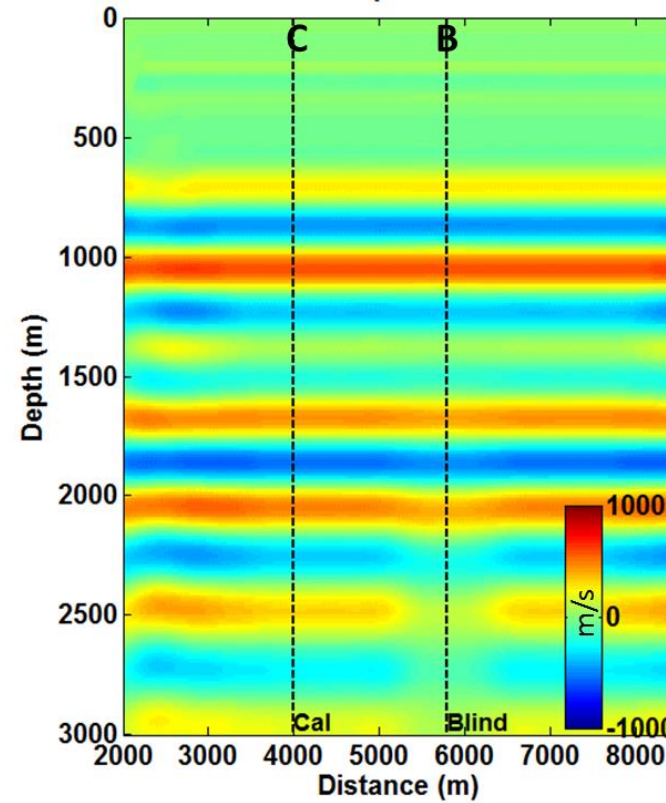
Inversion process

Initial model



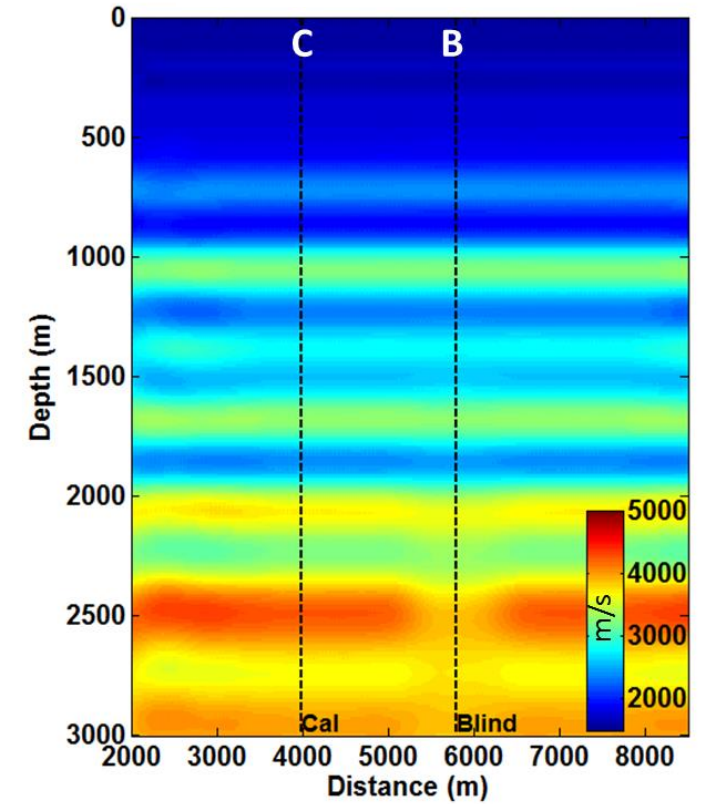
+

Velocity update

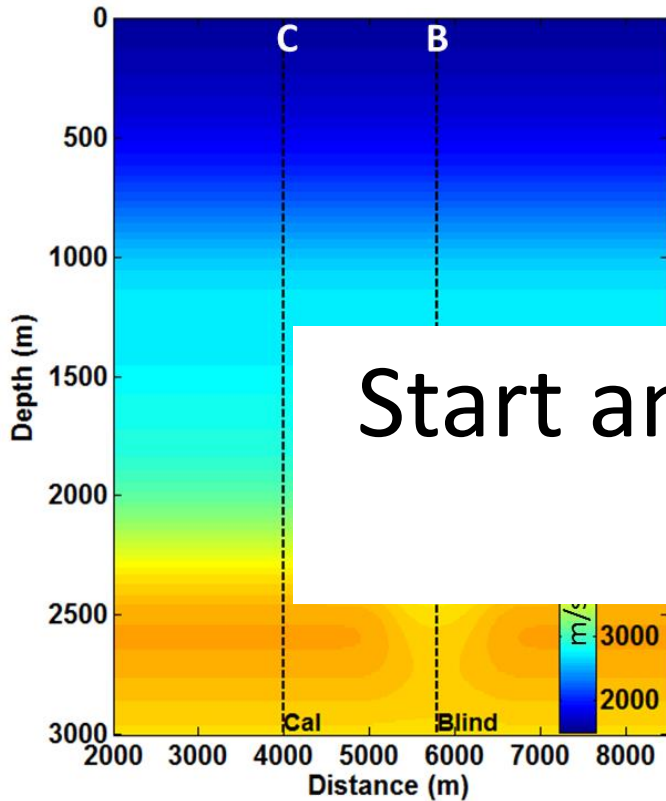


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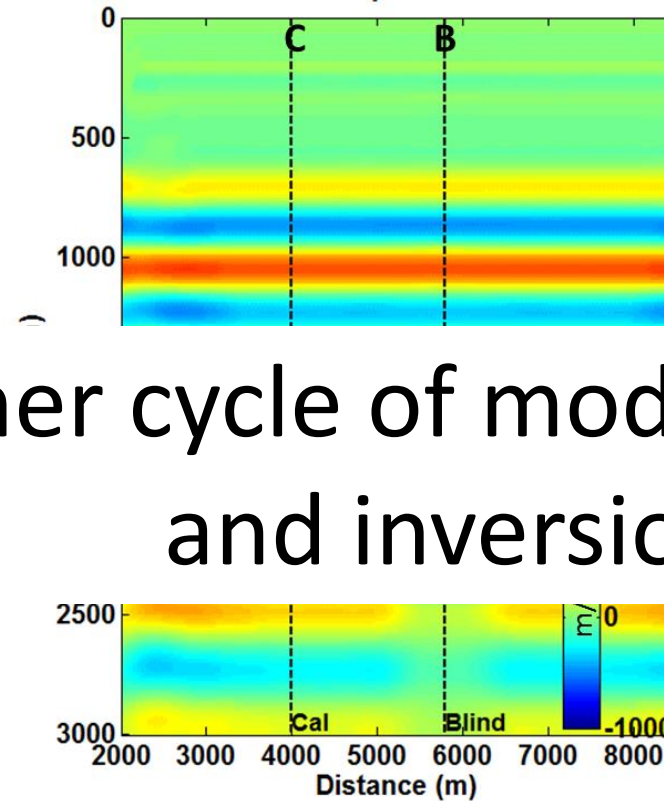
Inverted velocity model



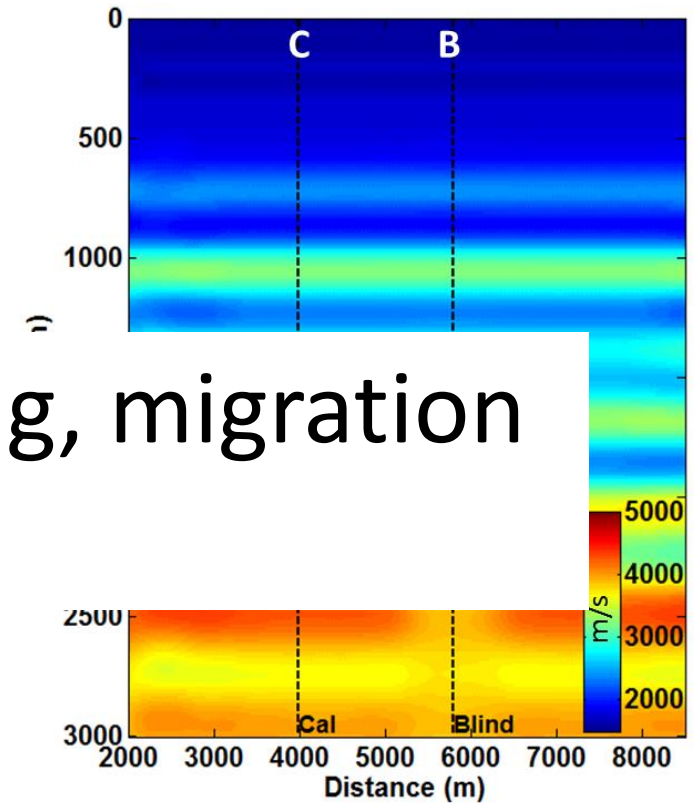
Initial model



Velocity update

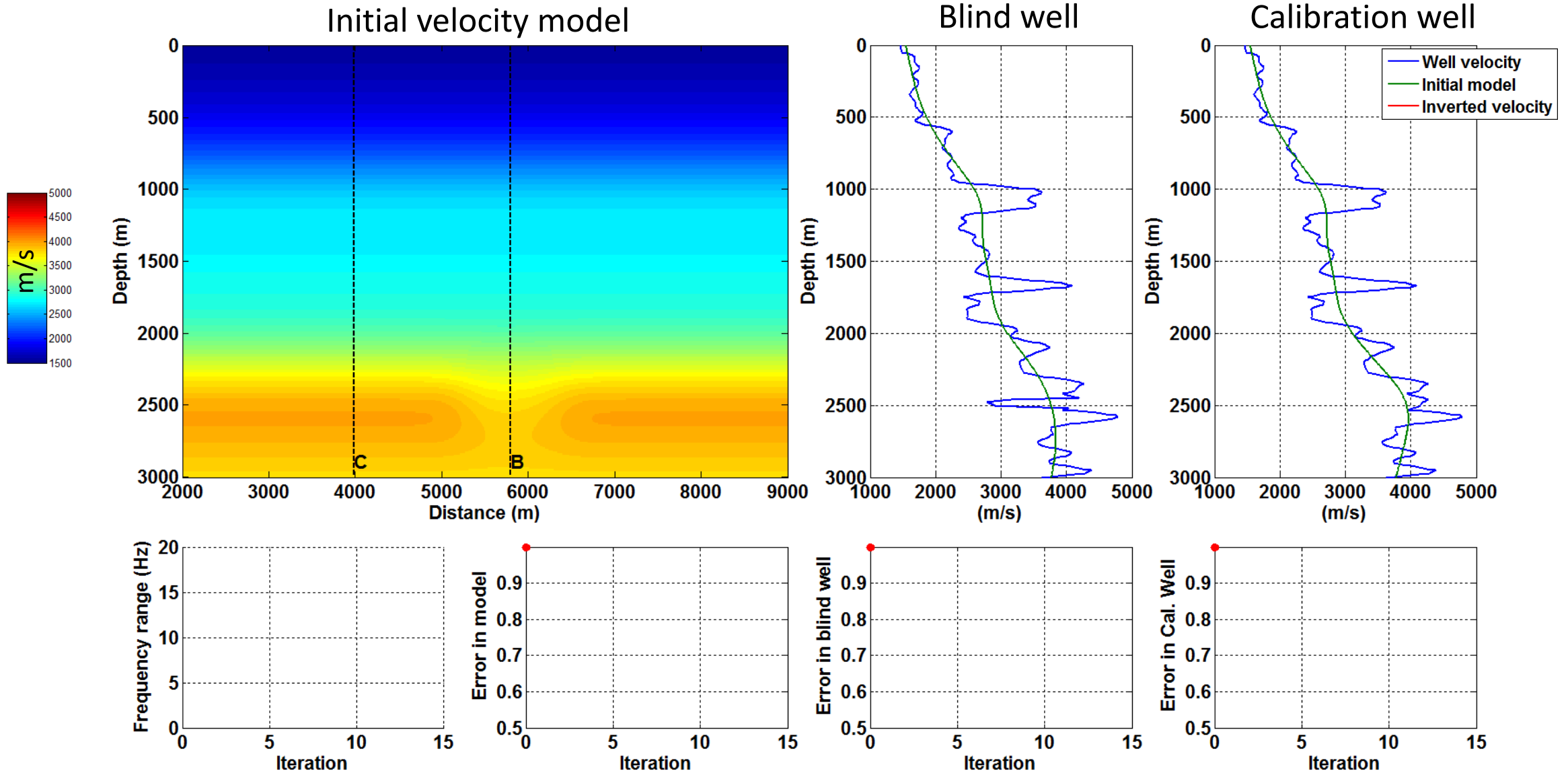


Inverted velocity model



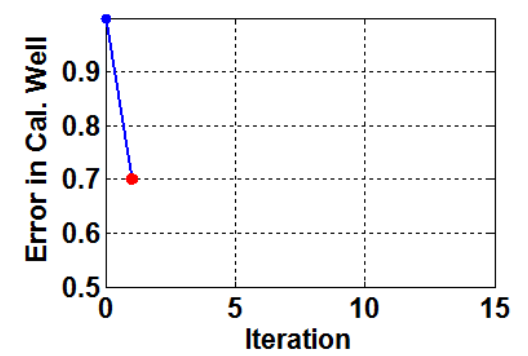
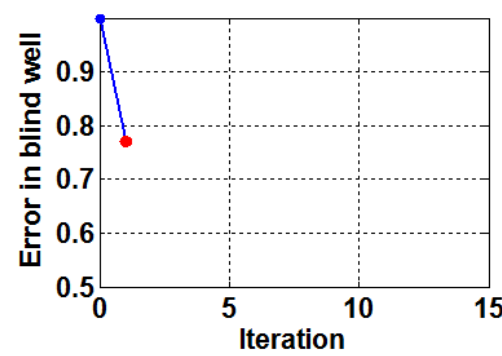
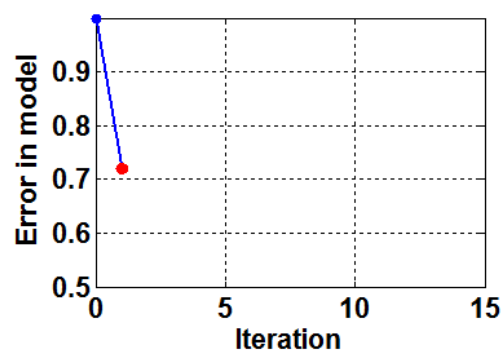
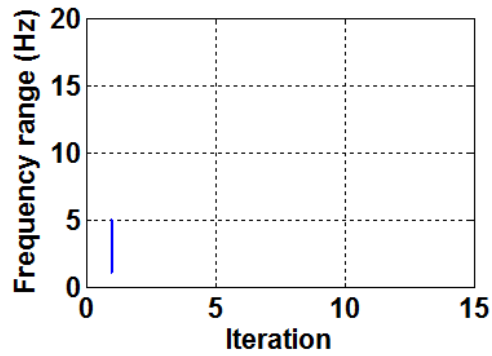
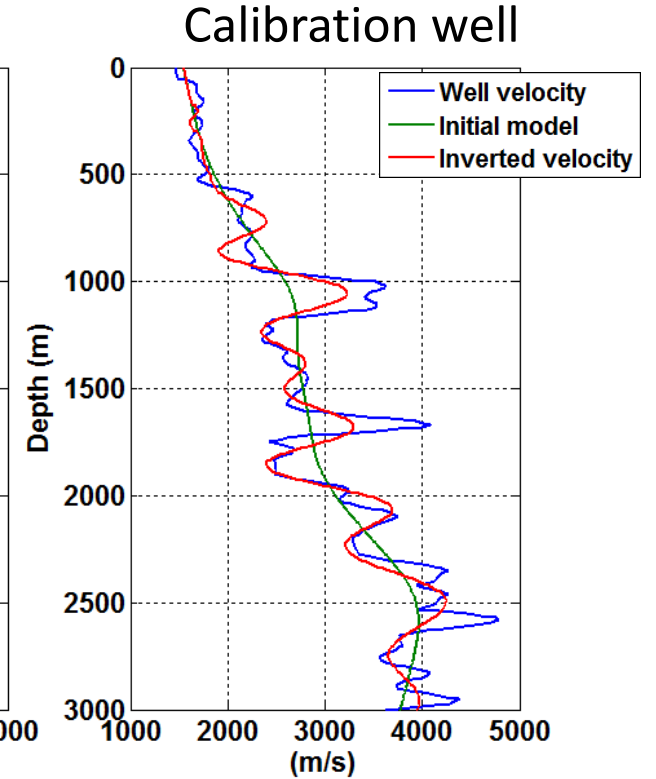
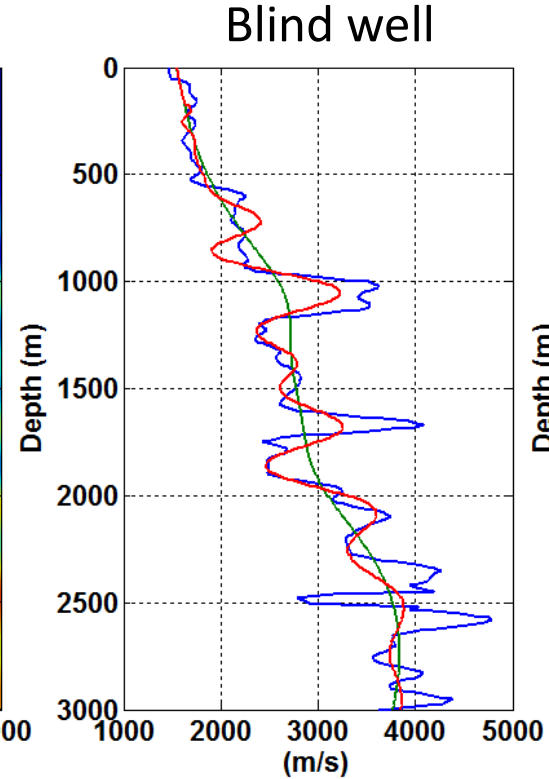
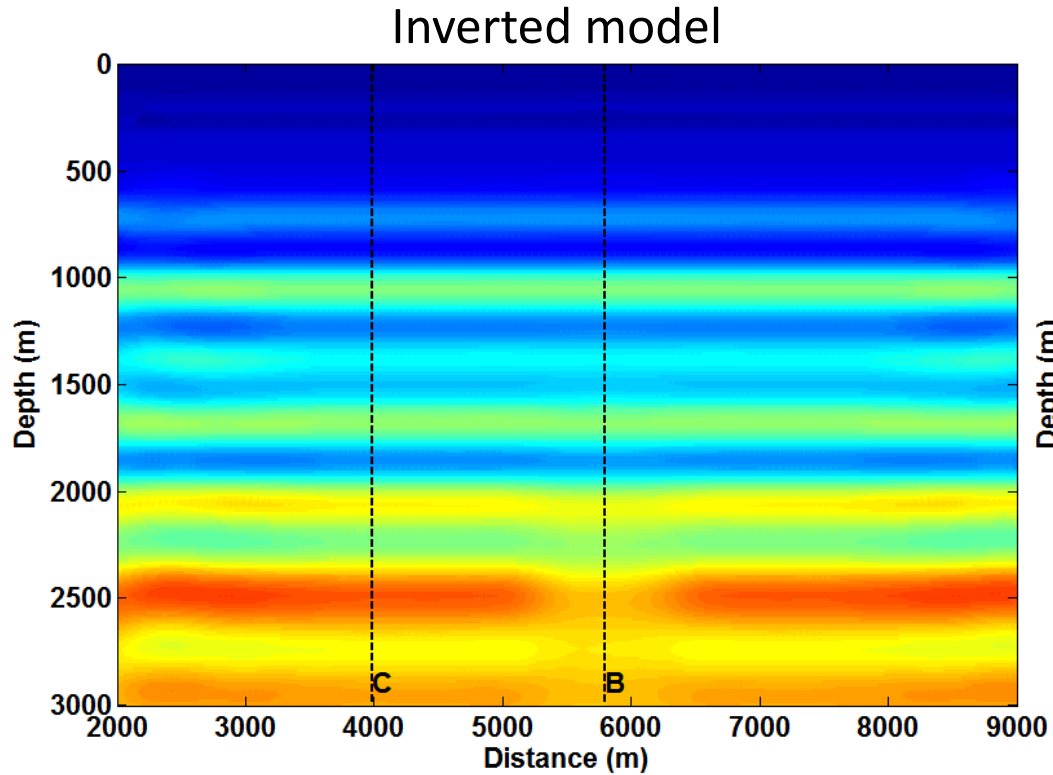
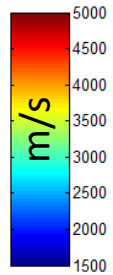
Start another cycle of modelling, migration and inversion

Evolution of the inverted model with more iterations



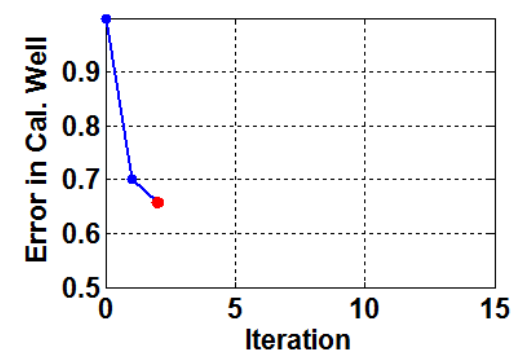
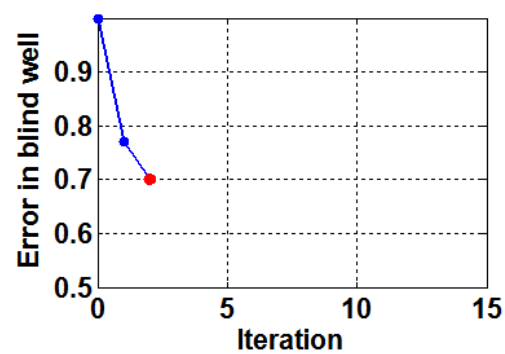
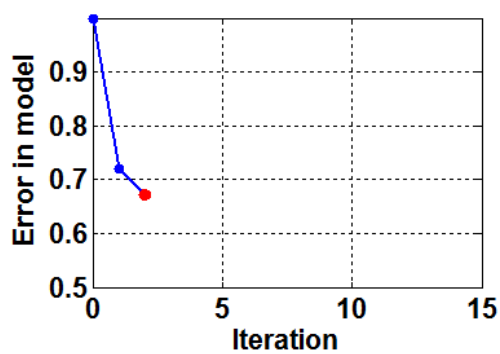
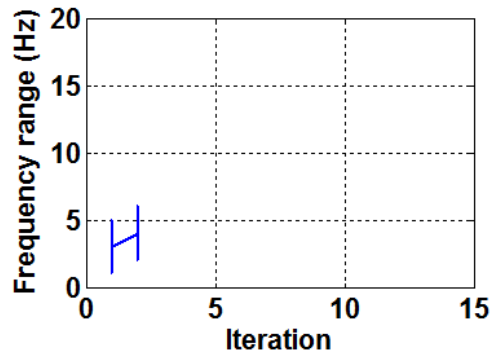
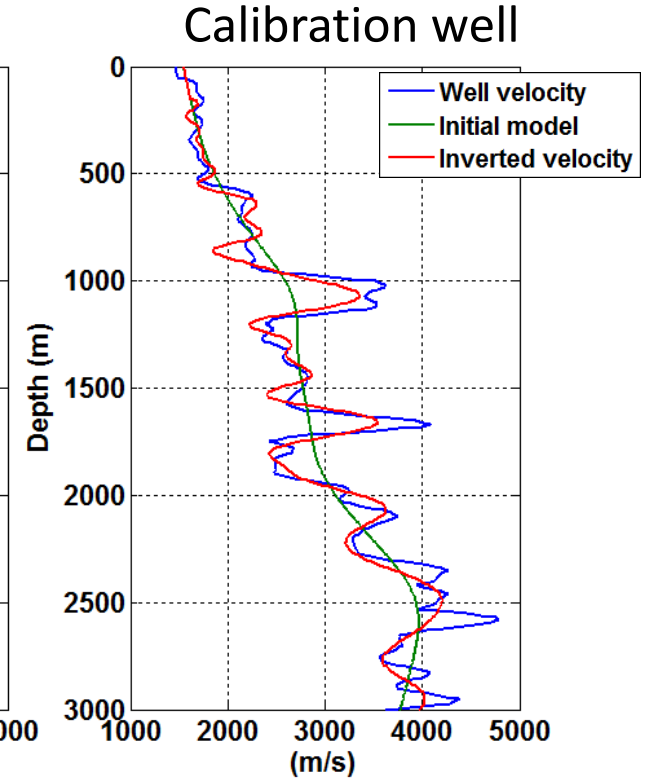
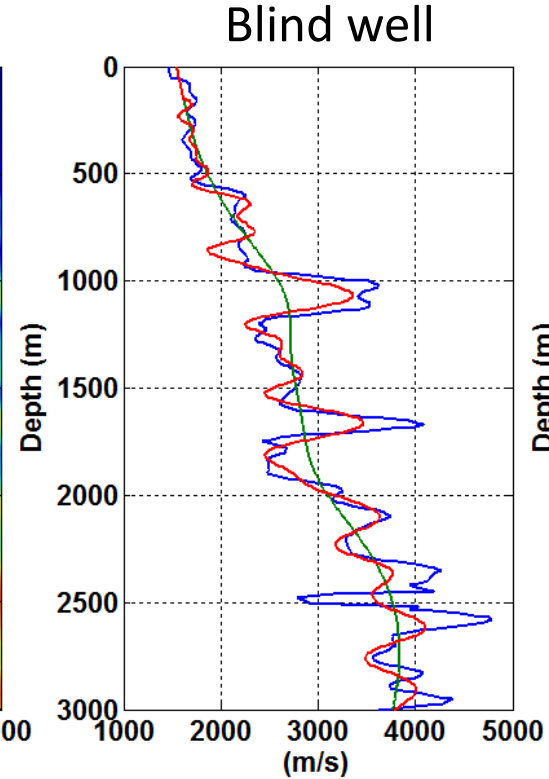
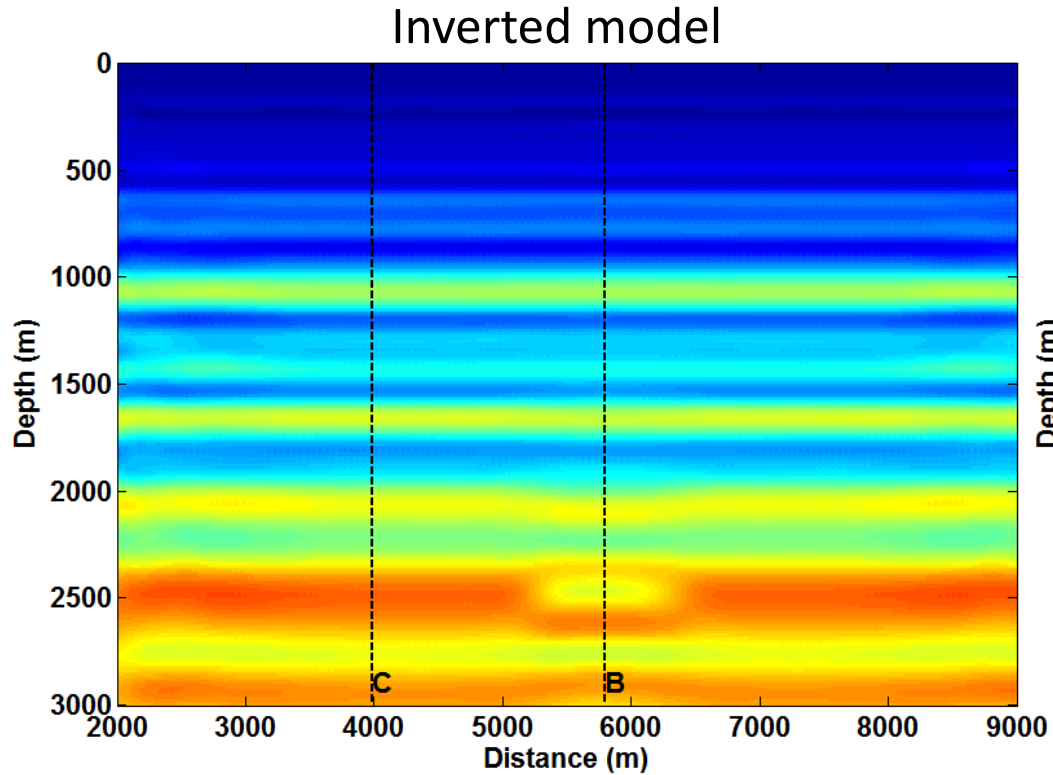
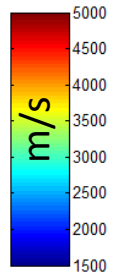
Evolution of the inverted model with more iterations

Iteration
1



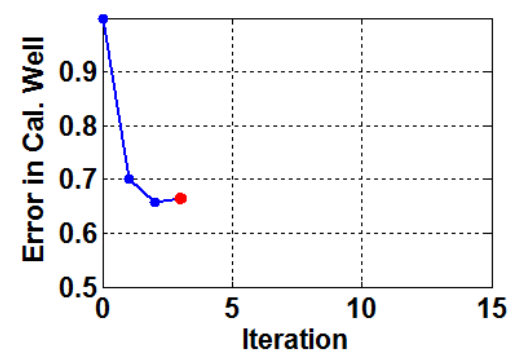
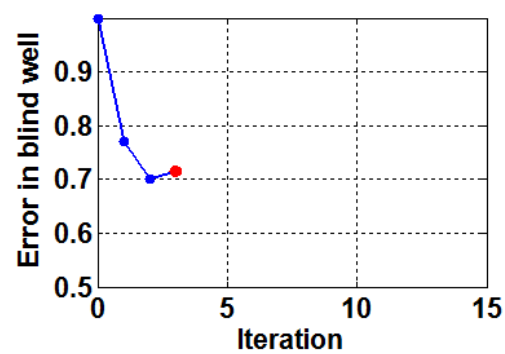
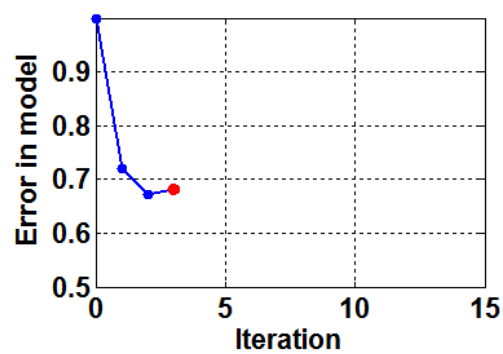
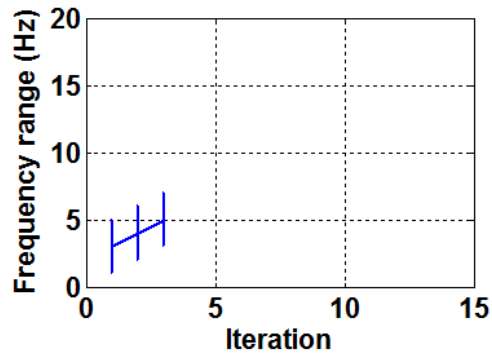
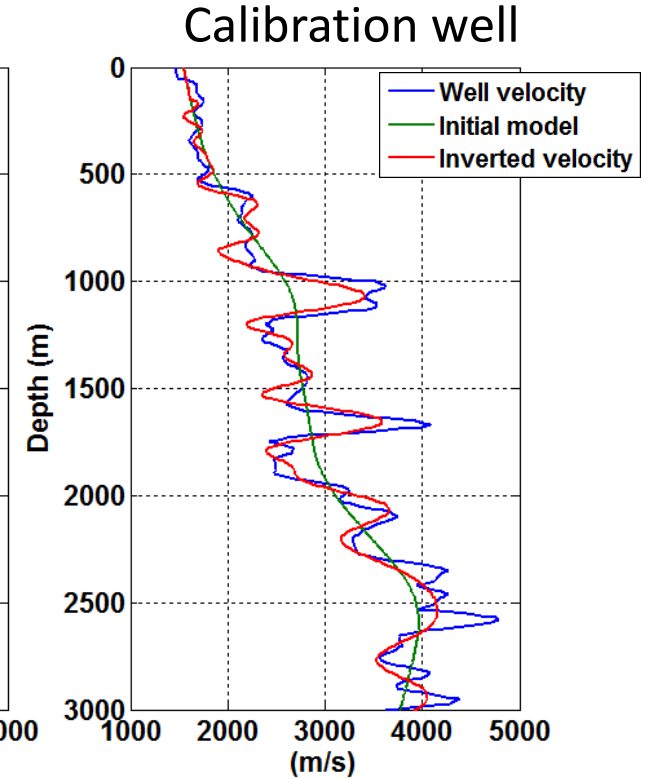
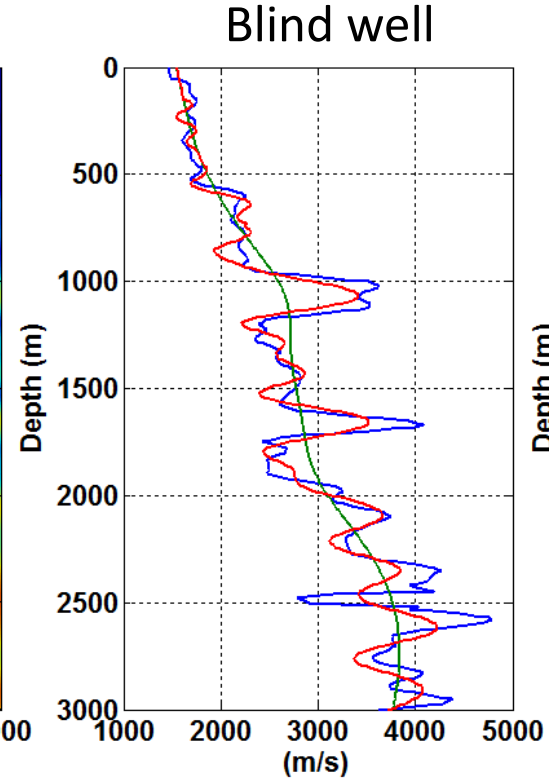
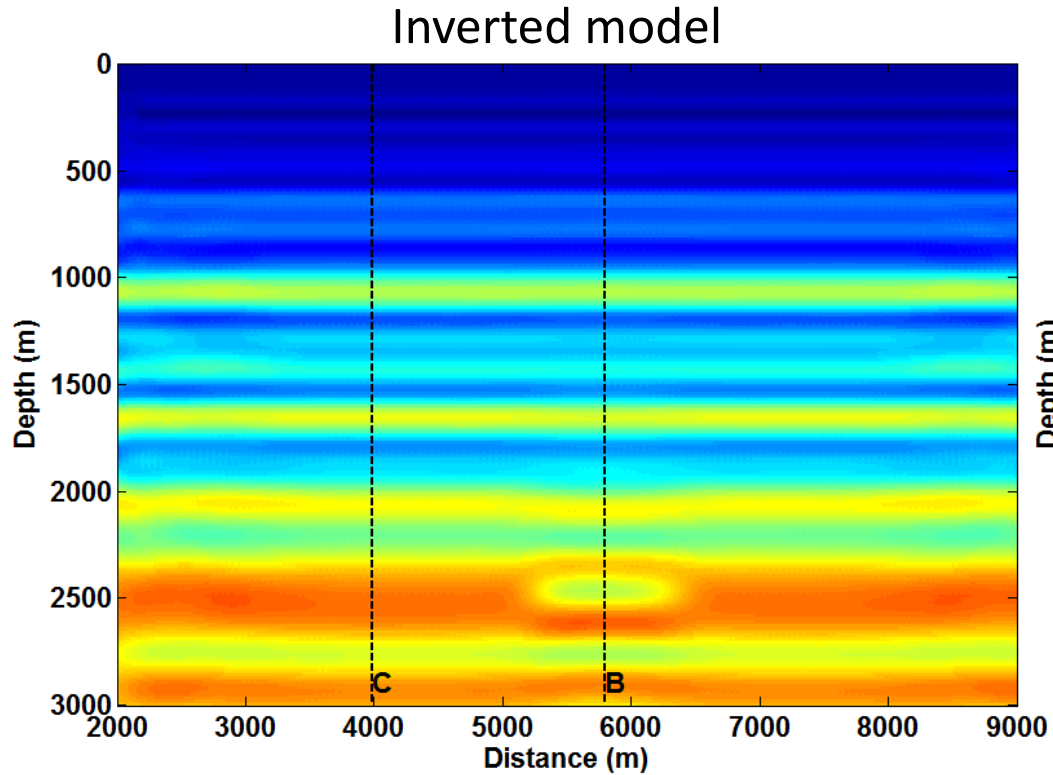
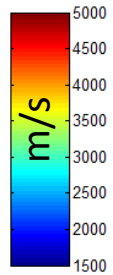
Evolution of the inverted model with more iterations

Iteration
2



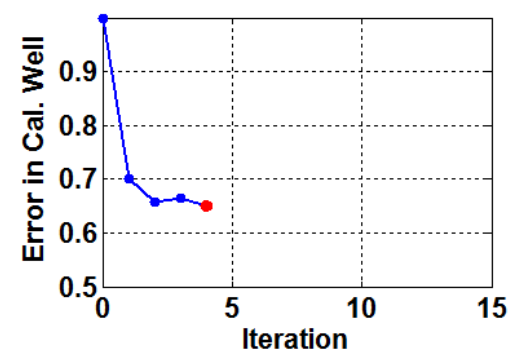
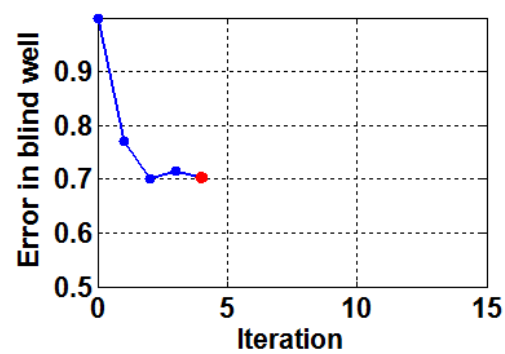
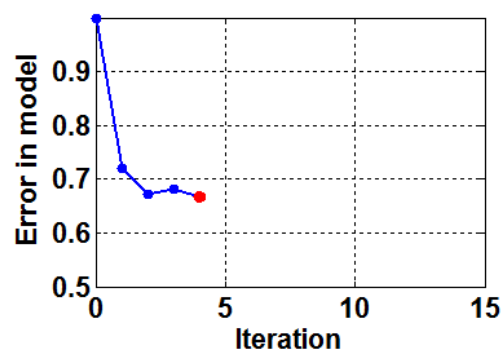
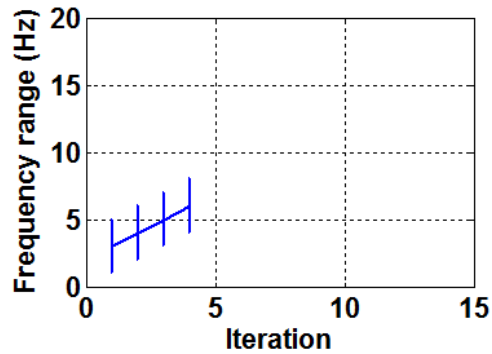
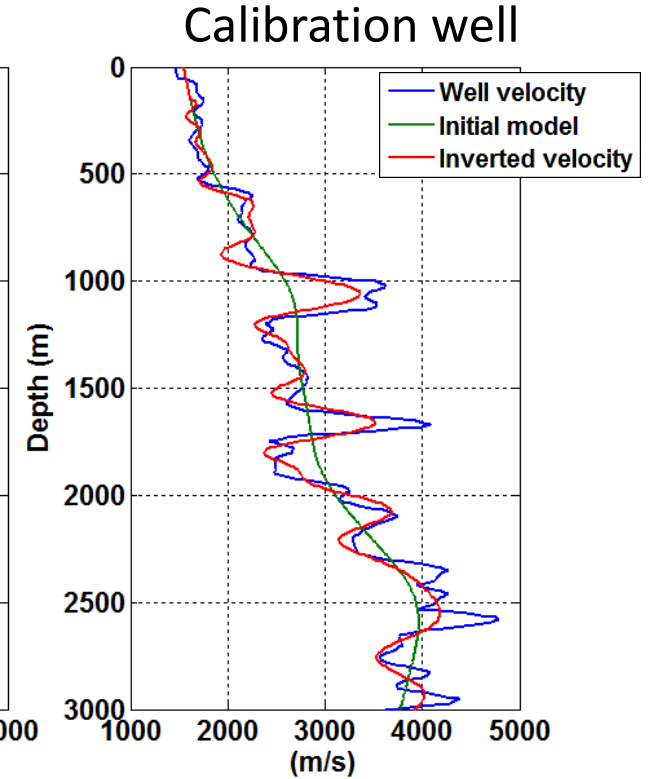
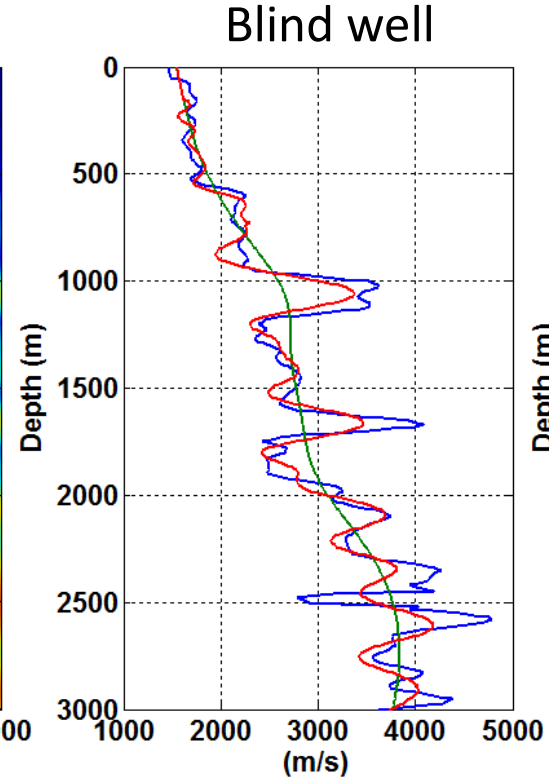
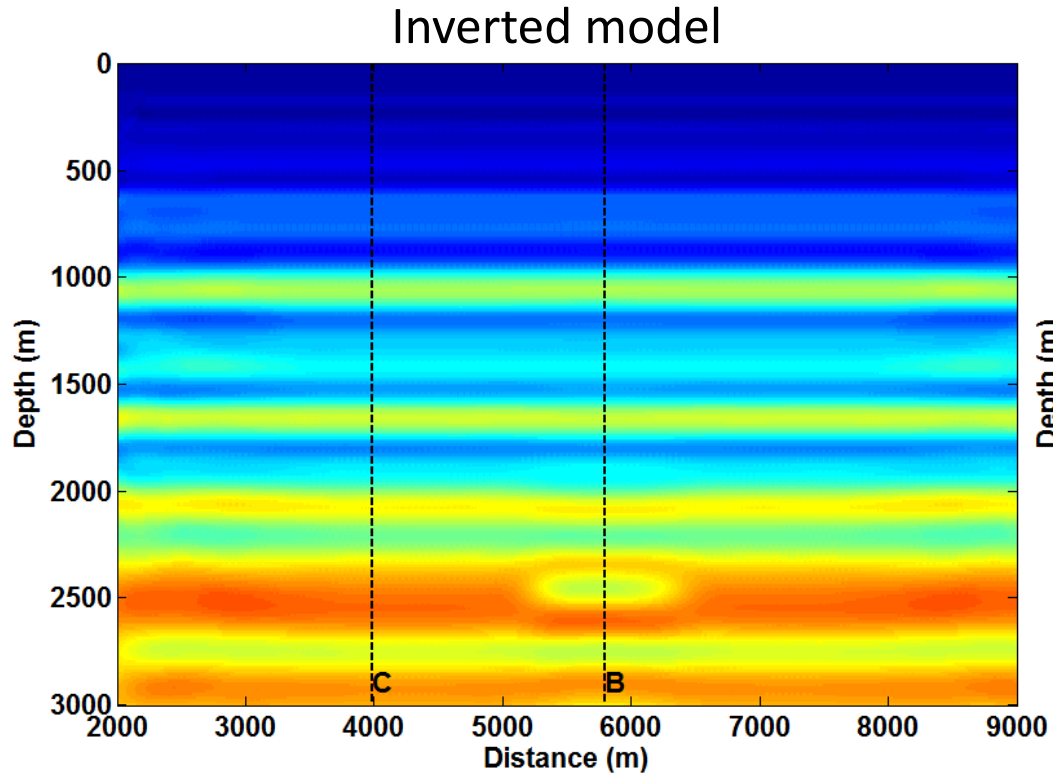
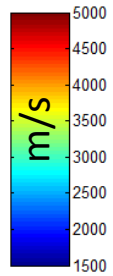
Evolution of the inverted model with more iterations

Iteration
3



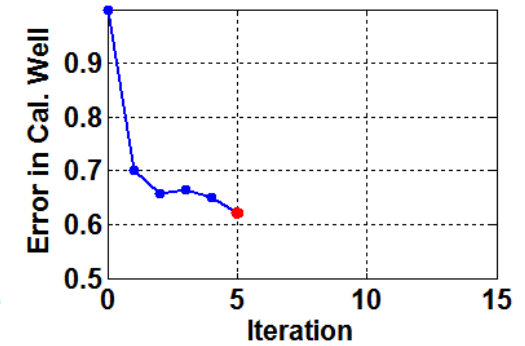
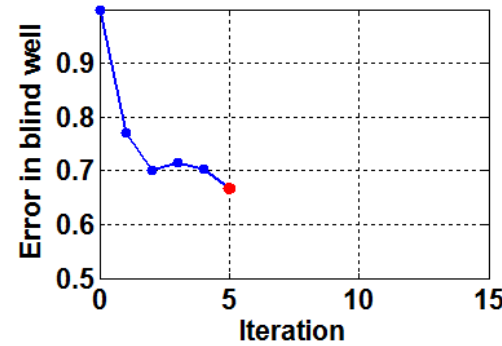
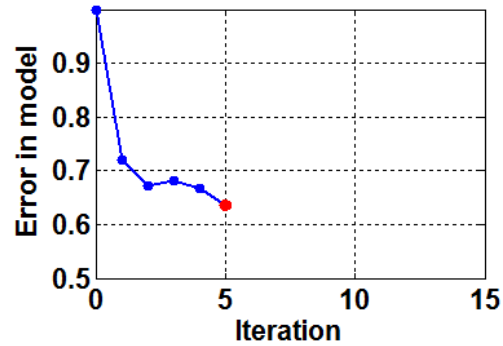
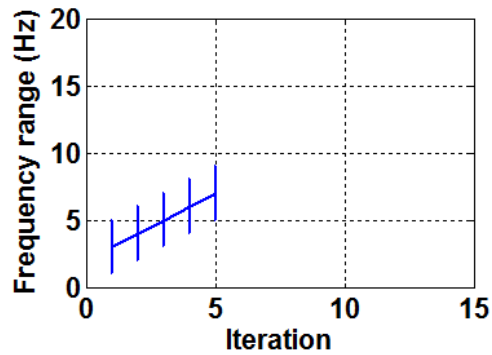
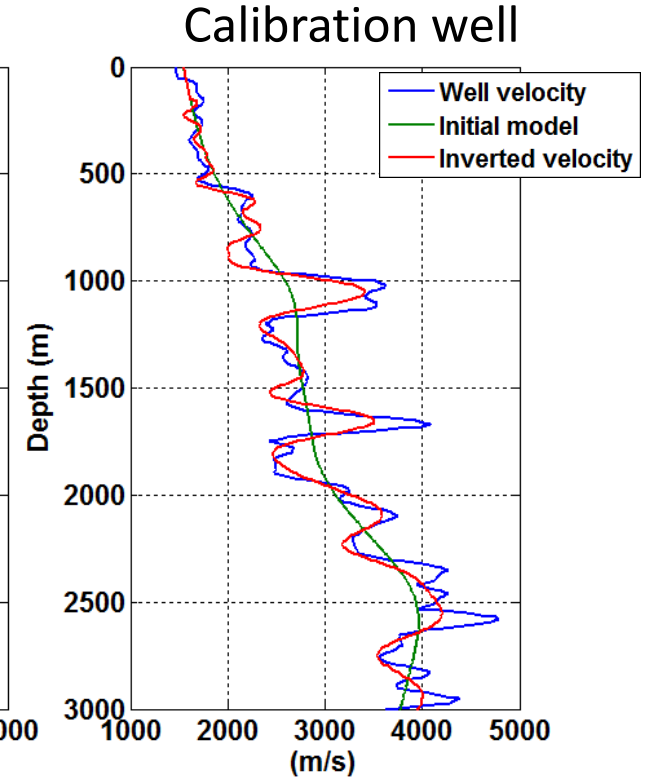
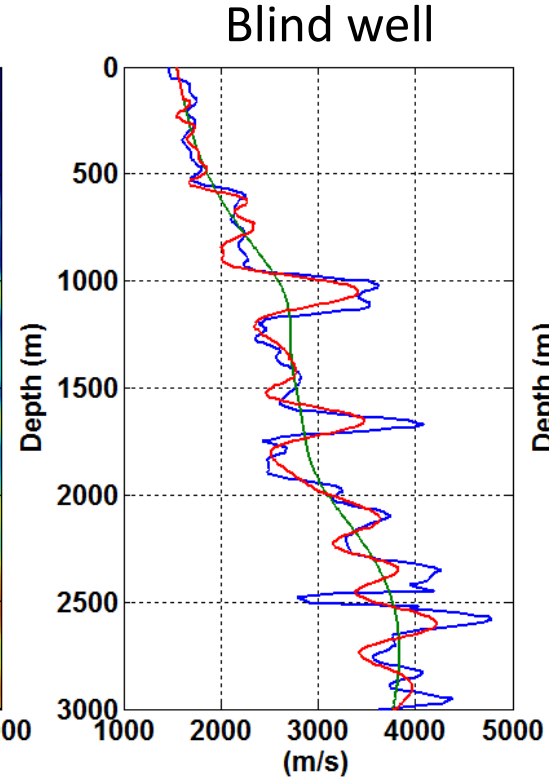
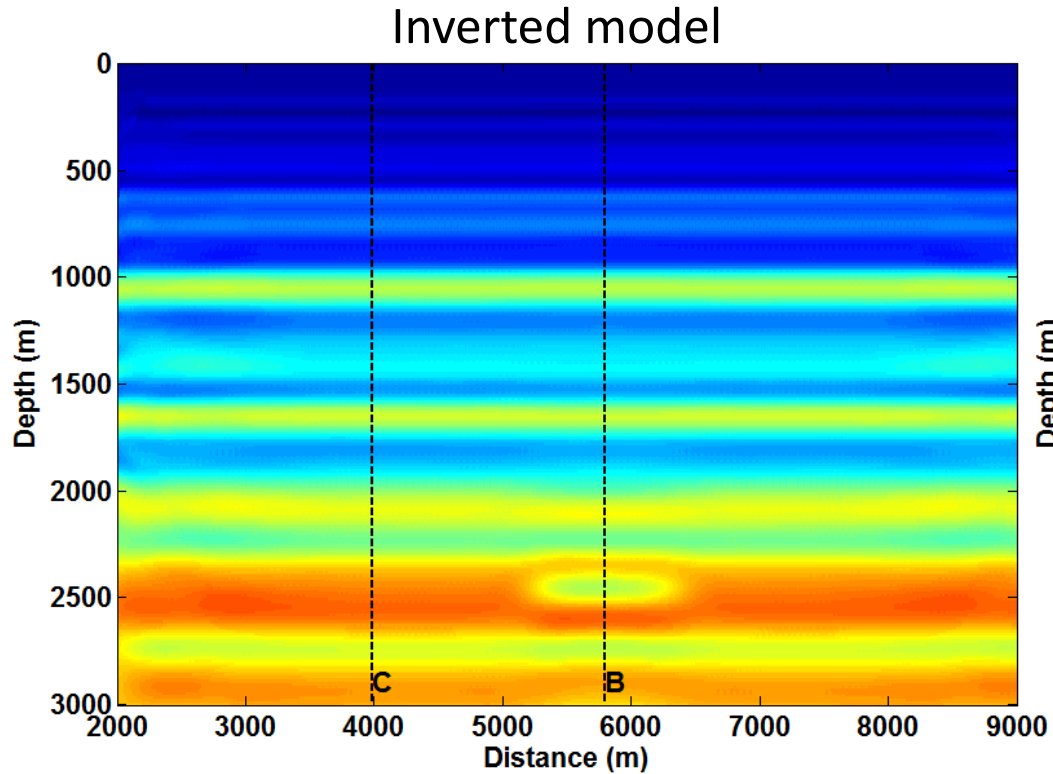
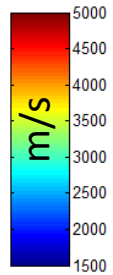
Evolution of the inverted model with more iterations

Iteration
4



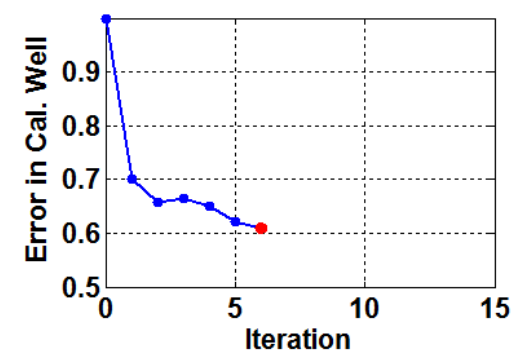
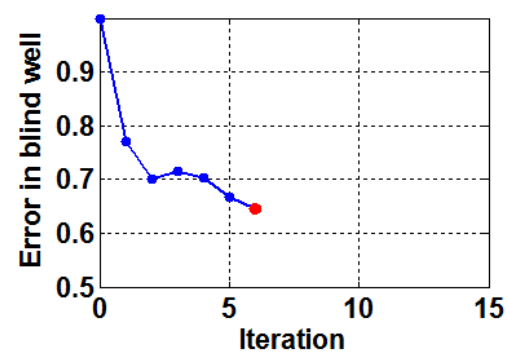
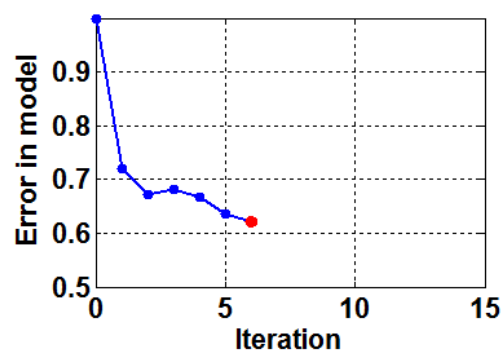
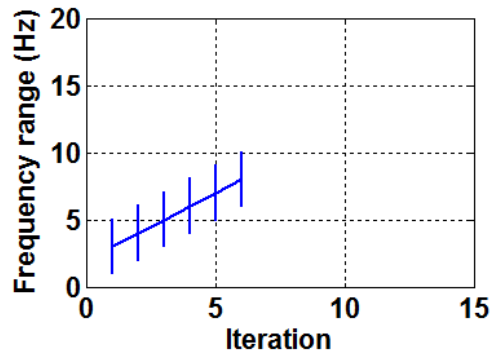
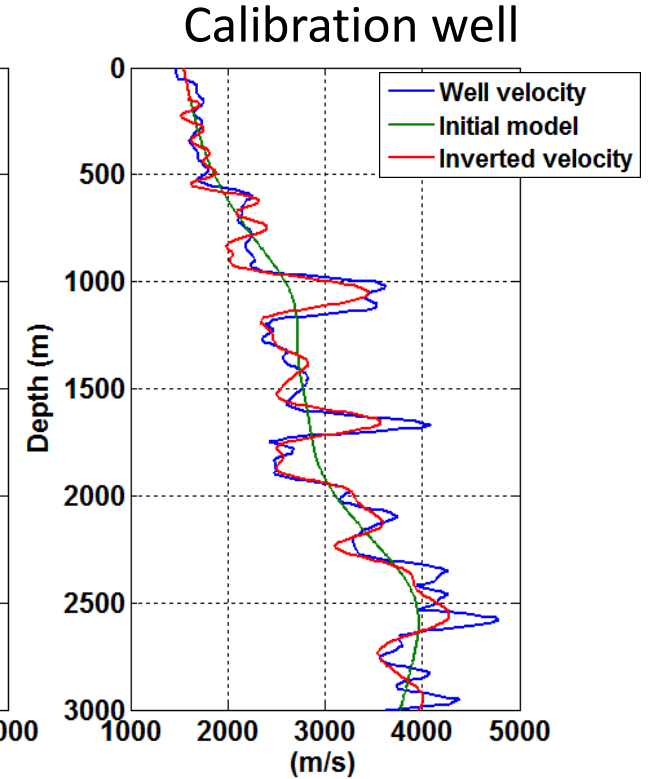
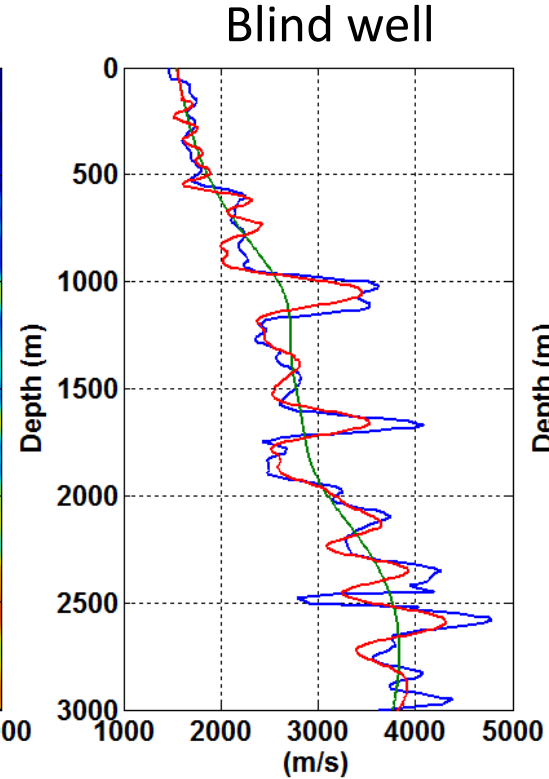
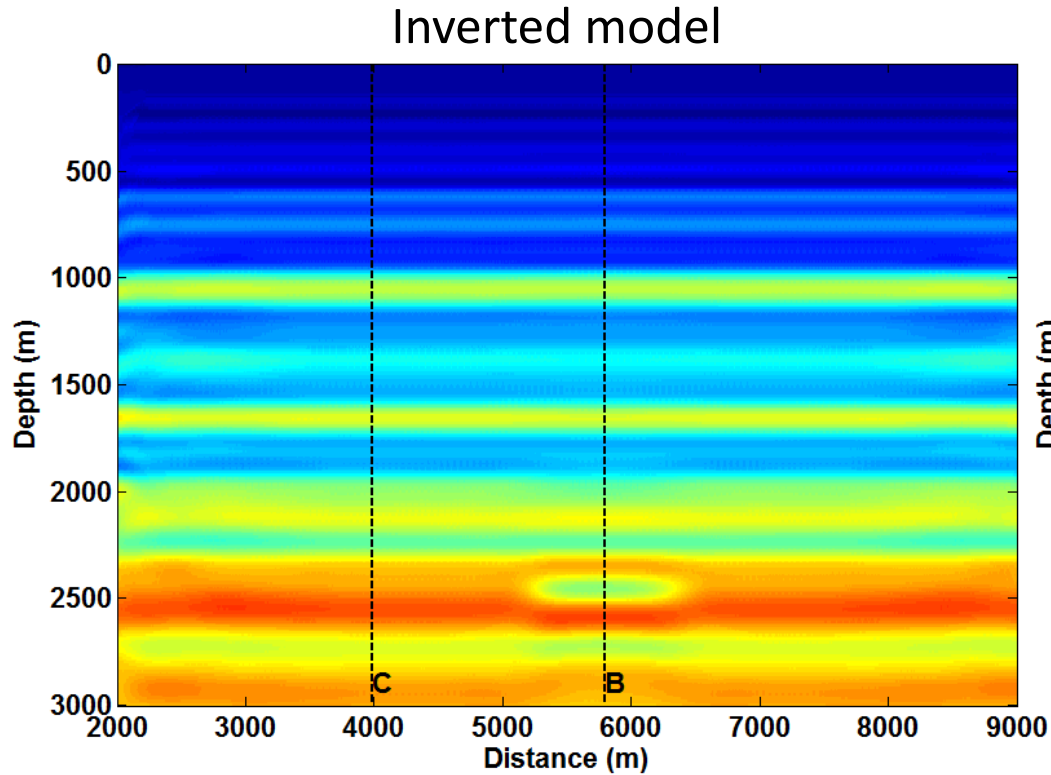
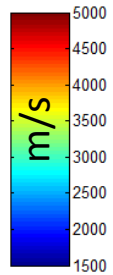
Evolution of the inverted model with more iterations

Iteration
5



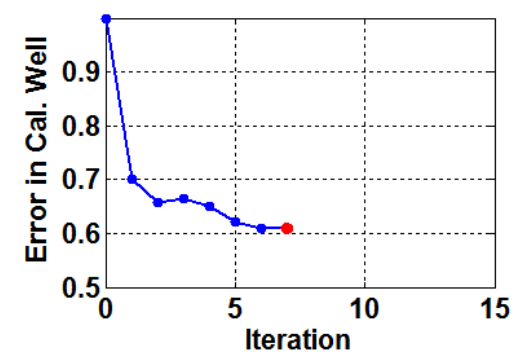
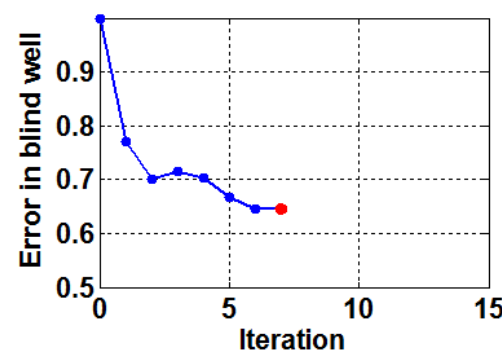
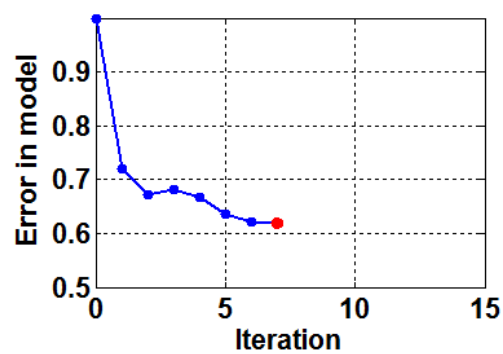
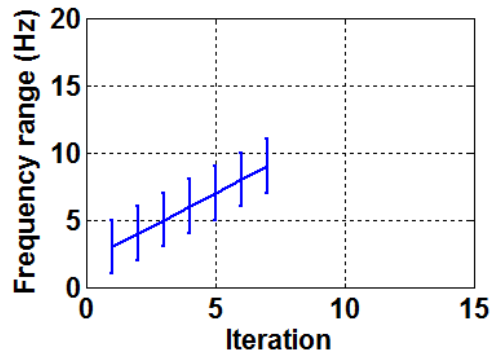
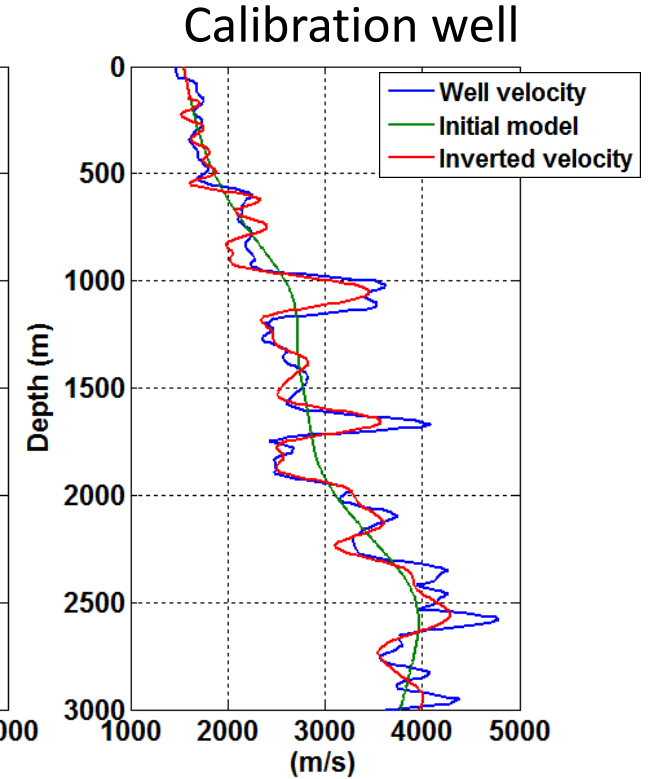
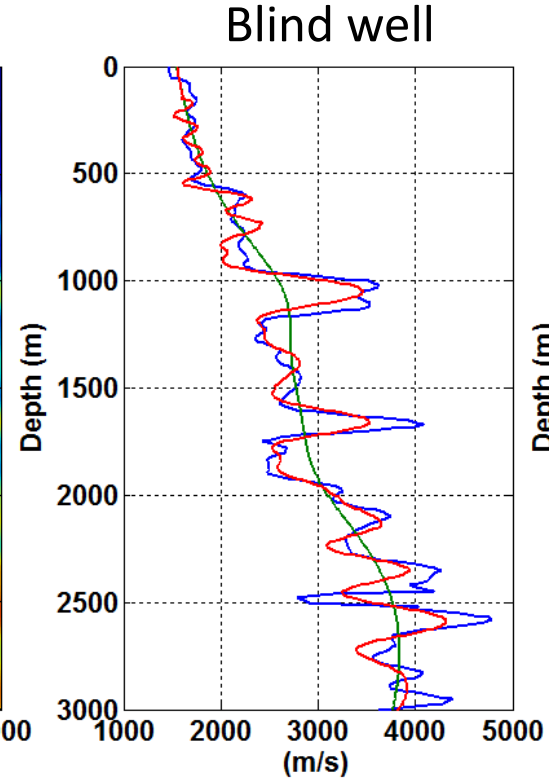
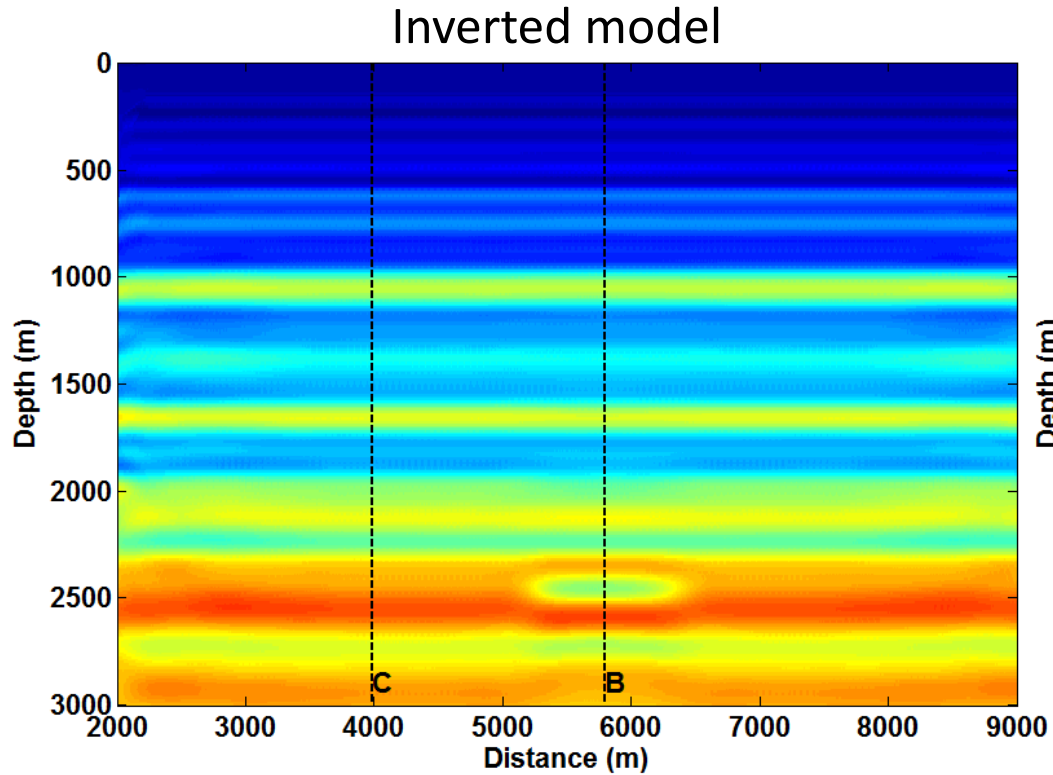
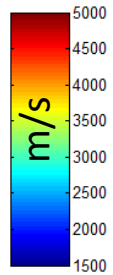
Evolution of the inverted model with more iterations

Iteration
6



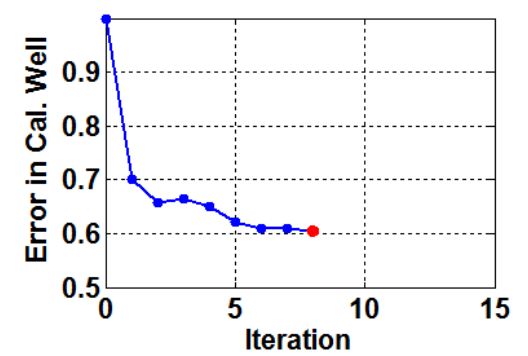
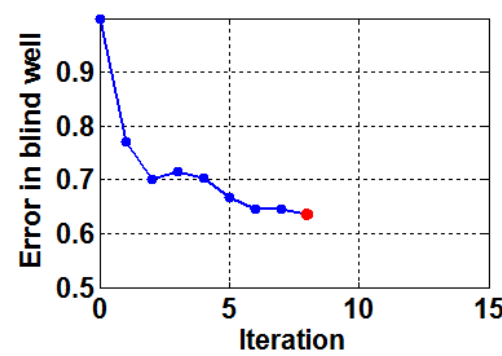
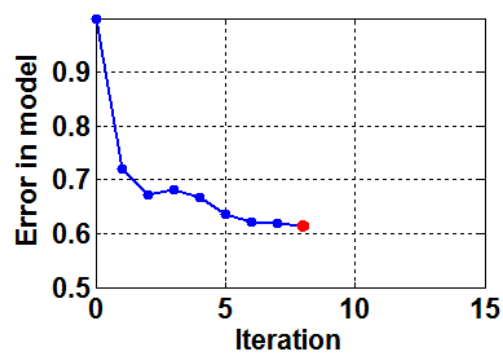
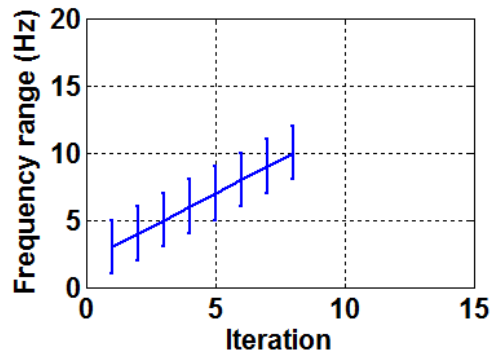
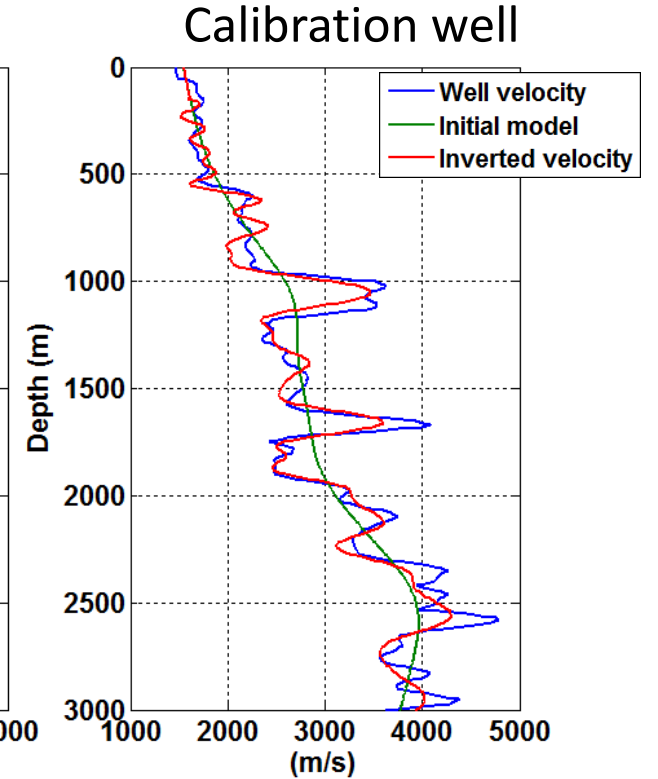
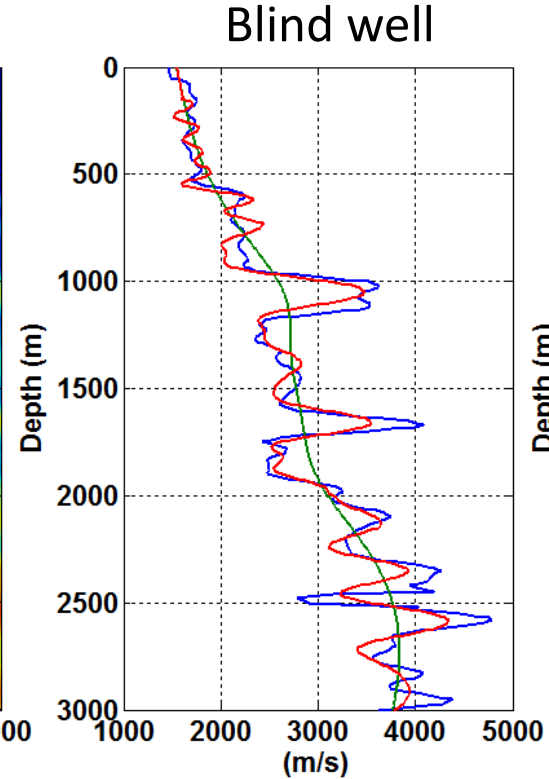
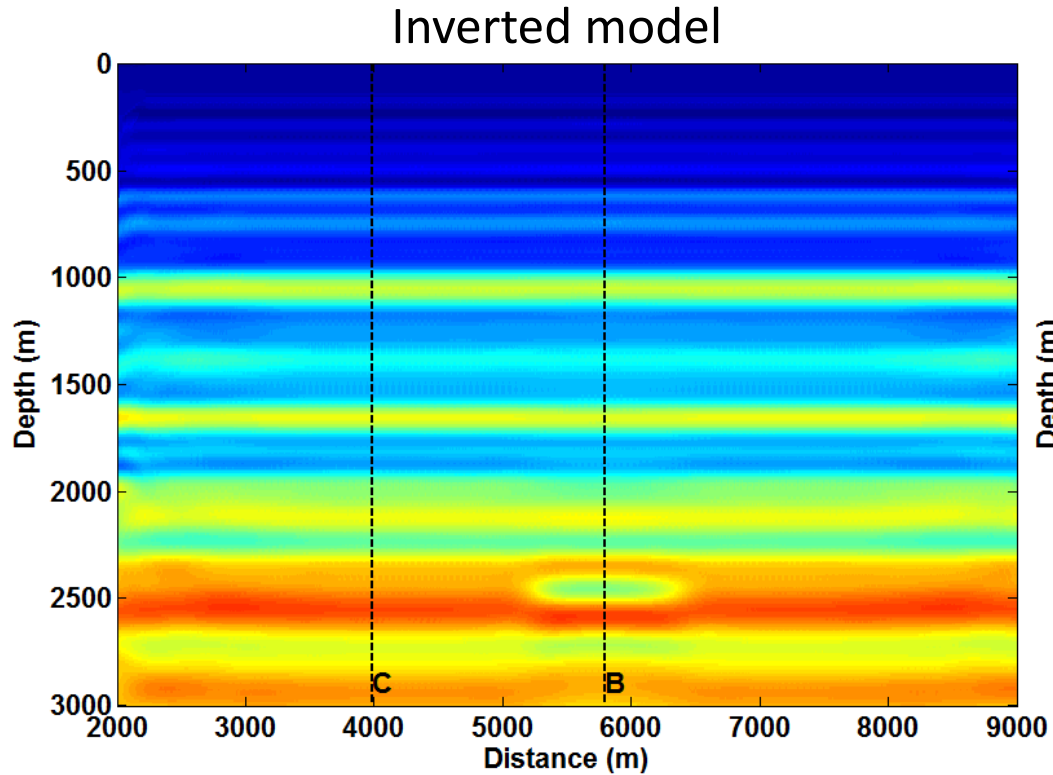
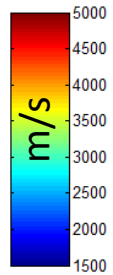
Evolution of the inverted model with more iterations

Iteration
7



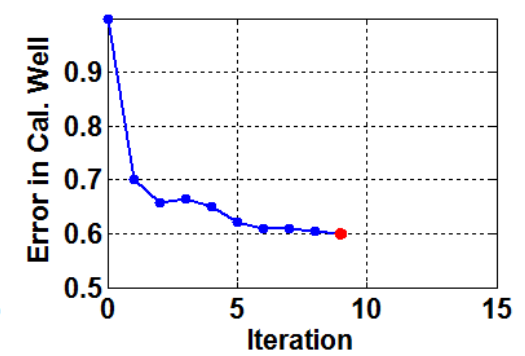
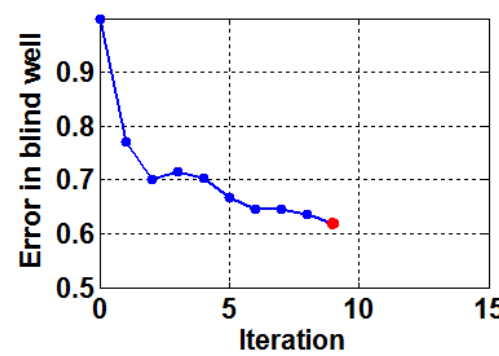
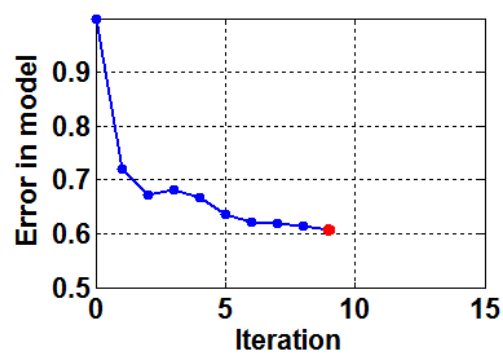
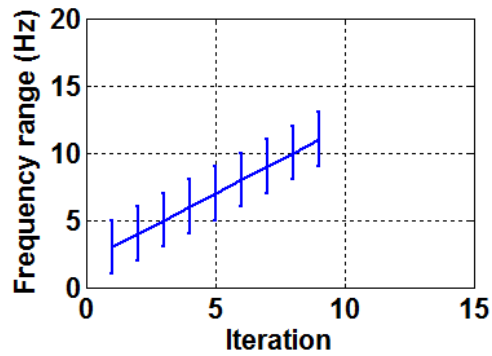
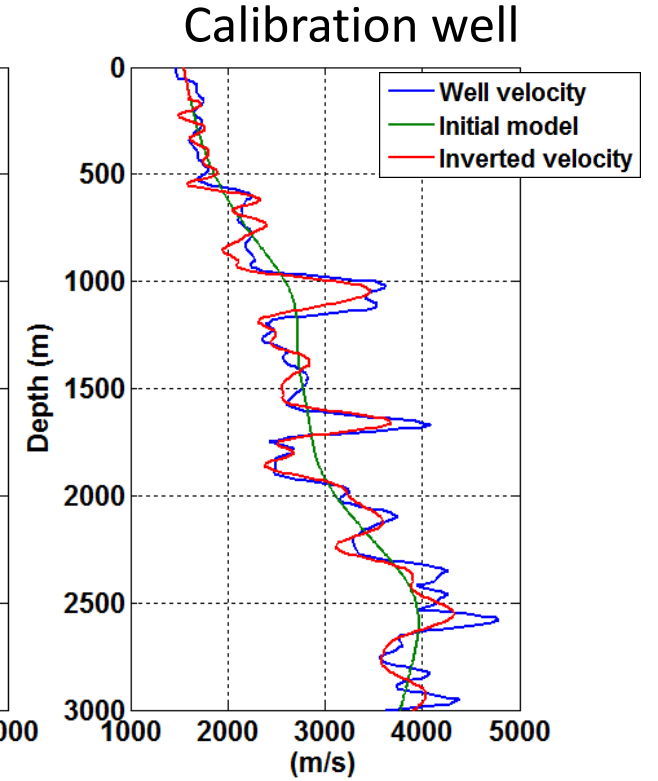
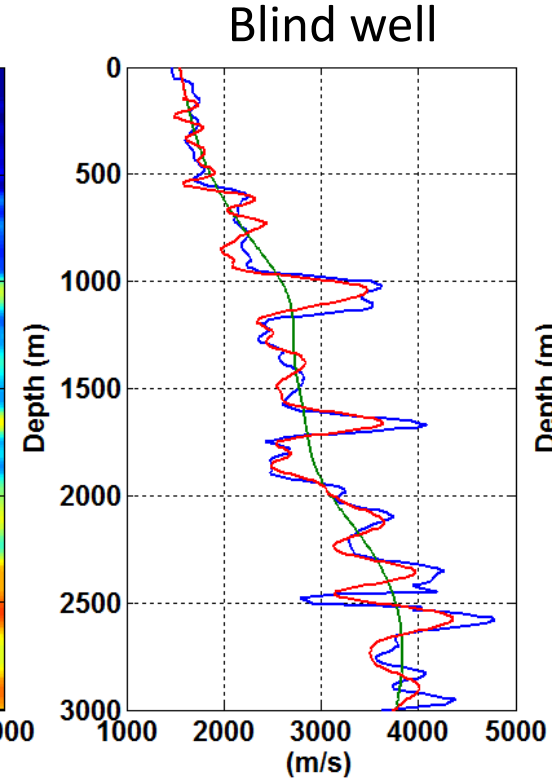
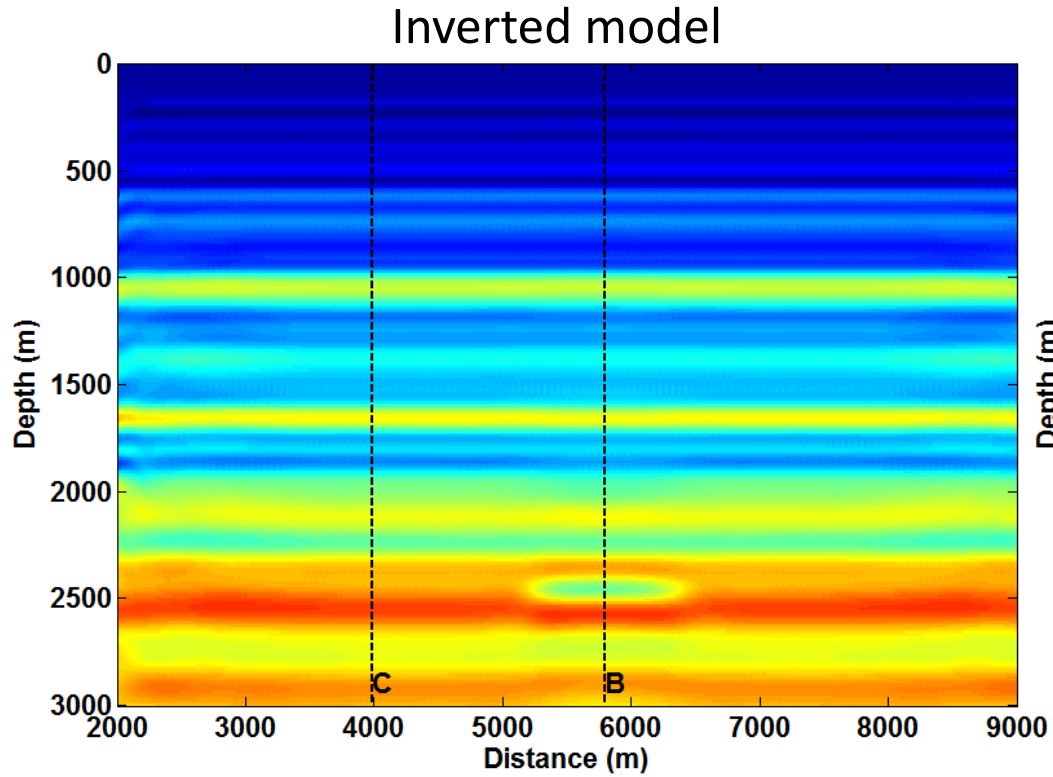
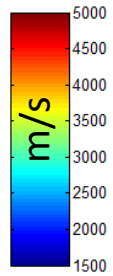
Evolution of the inverted model with more iterations

Iteration
8



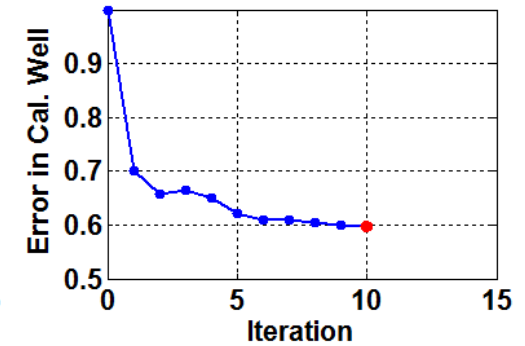
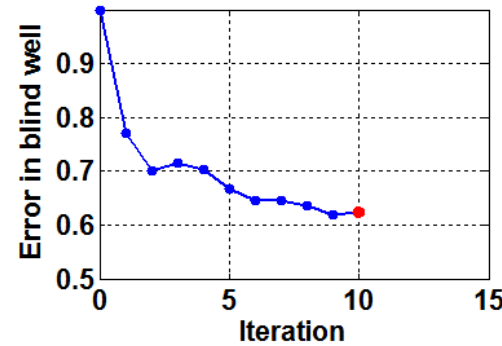
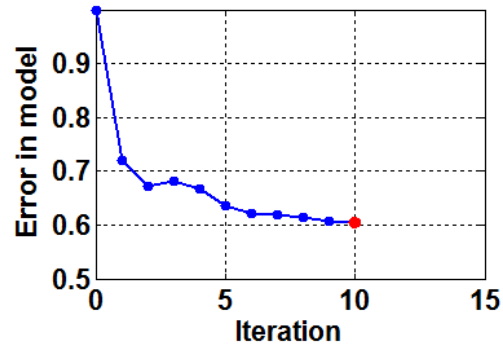
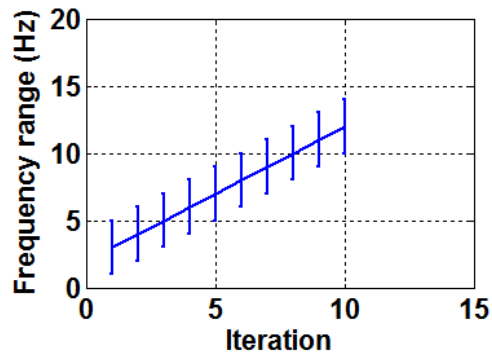
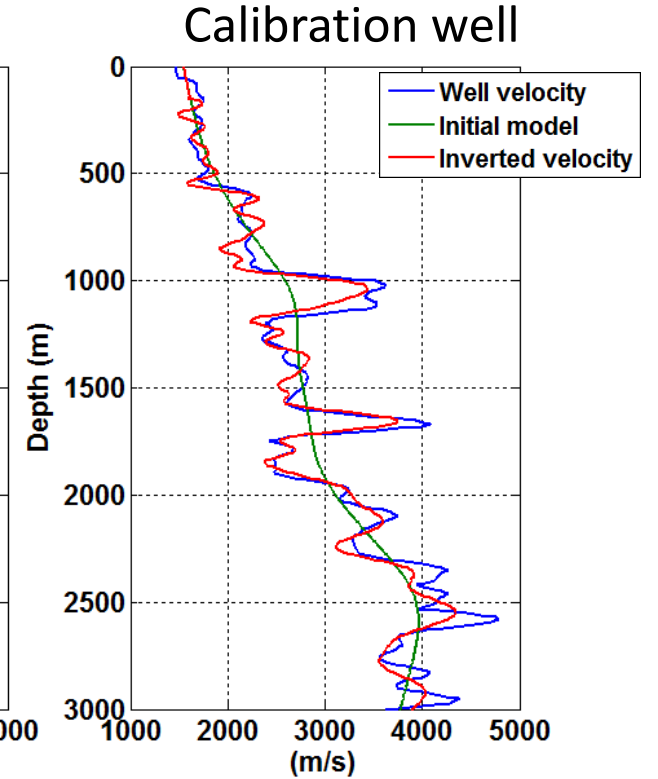
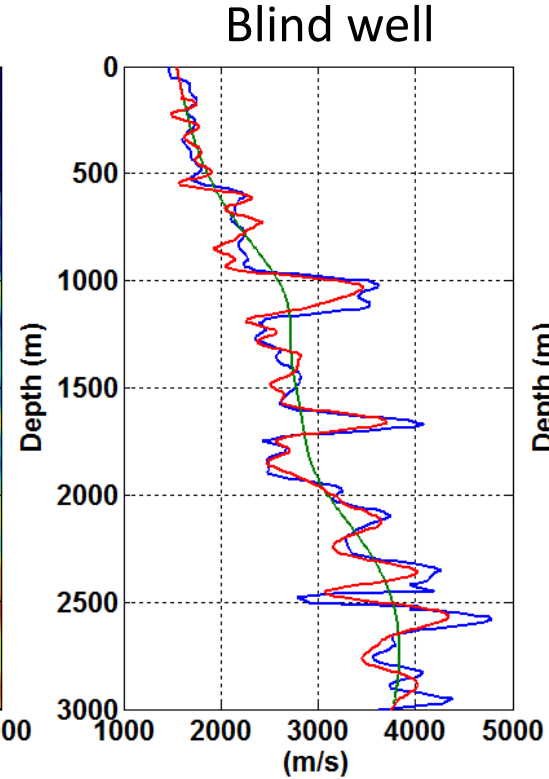
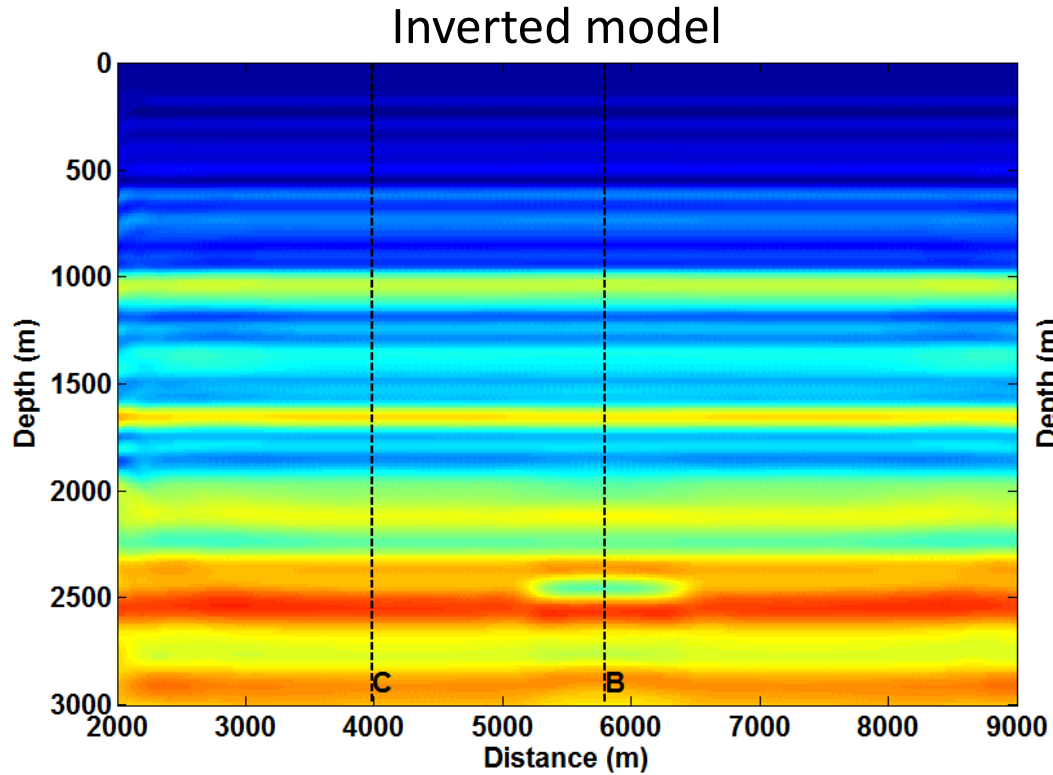
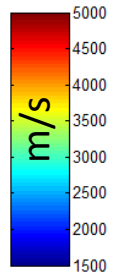
Evolution of the inverted model with more iterations

Iteration
9



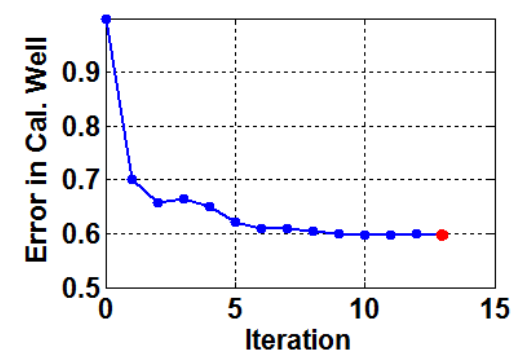
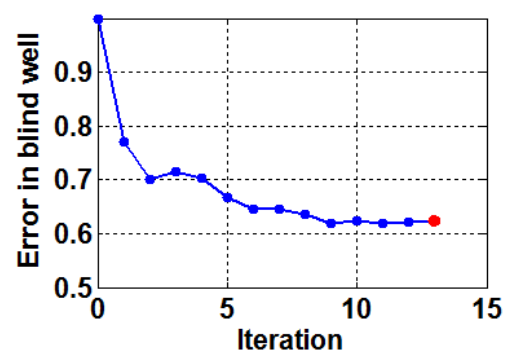
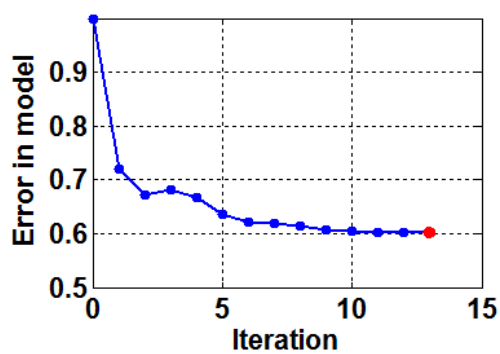
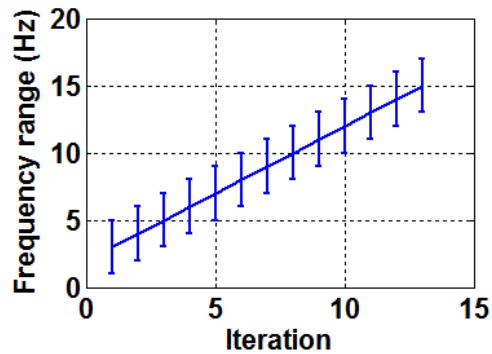
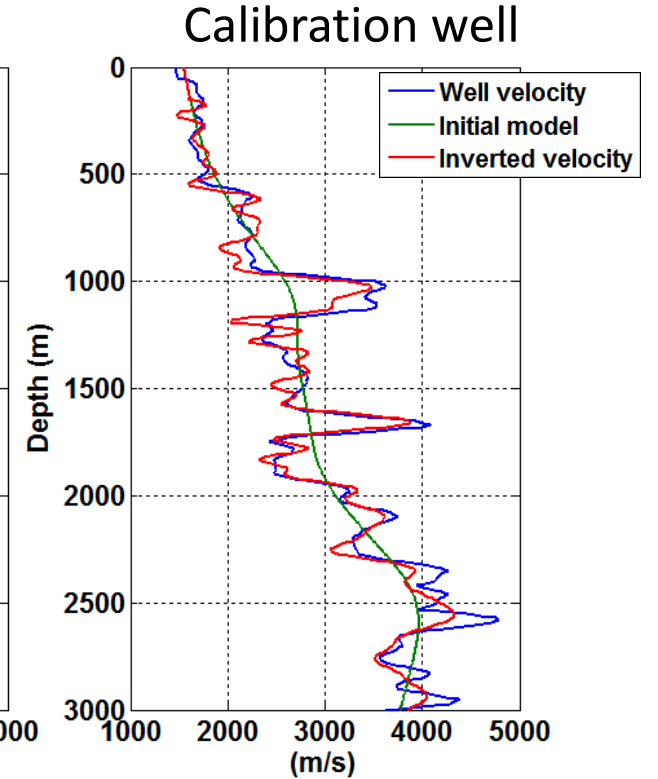
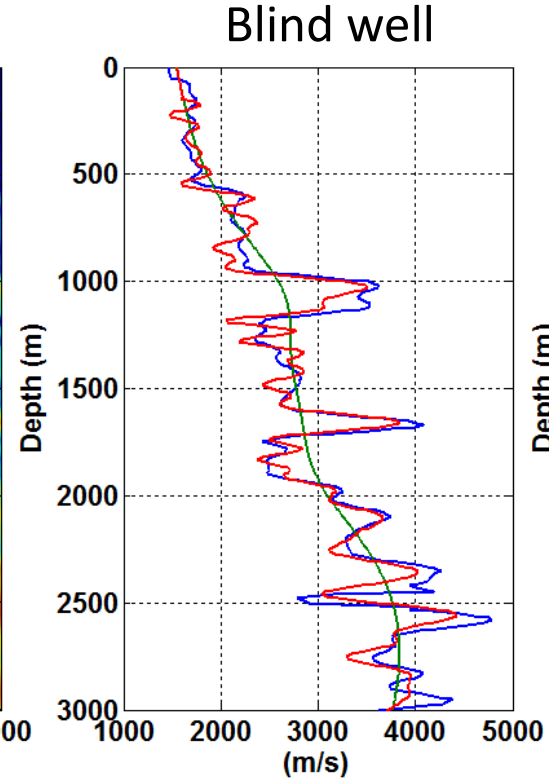
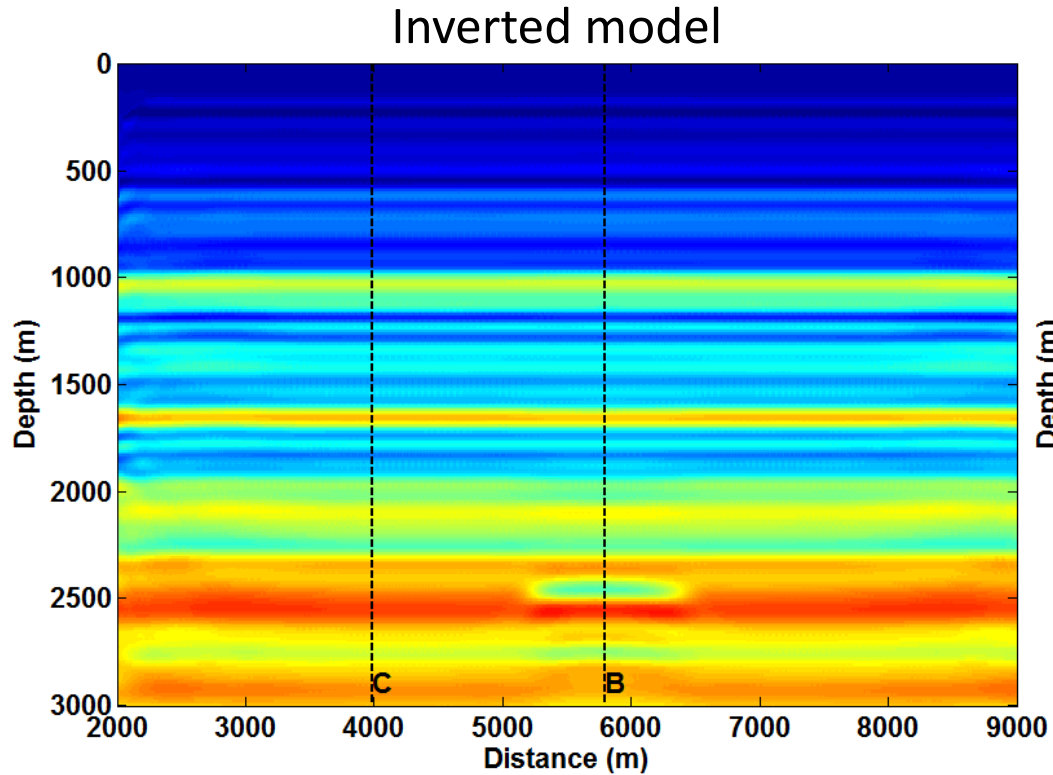
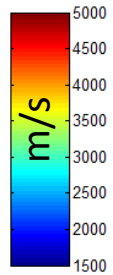
Evolution of the inverted model with more iterations

Iteration
10



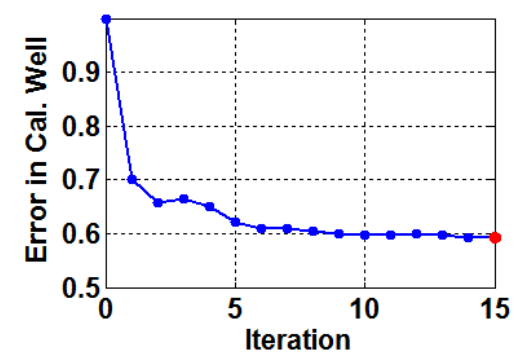
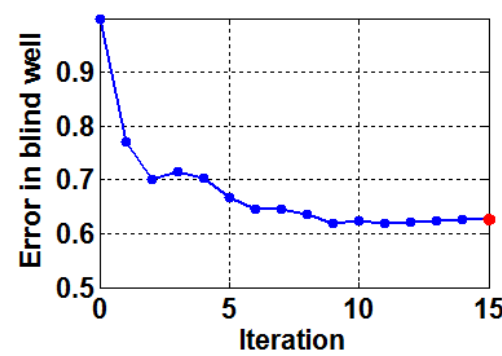
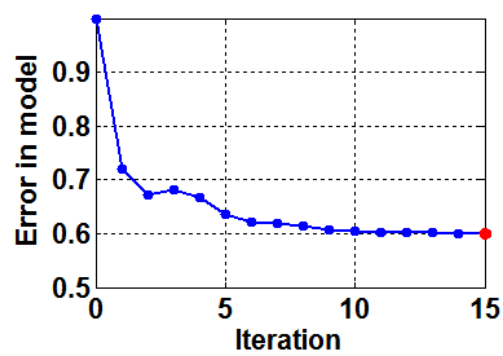
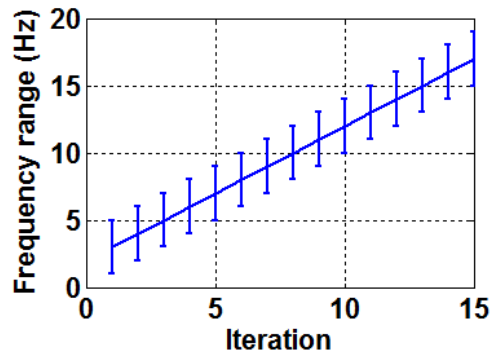
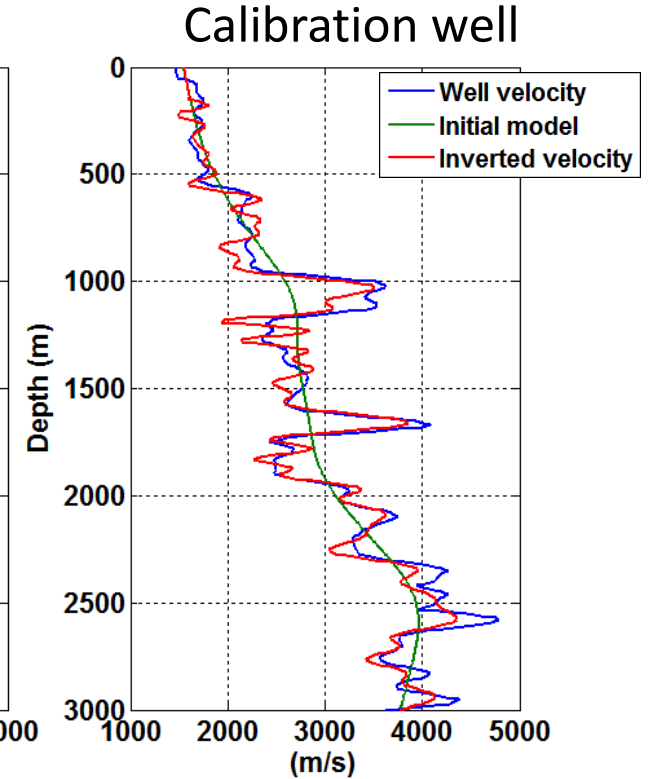
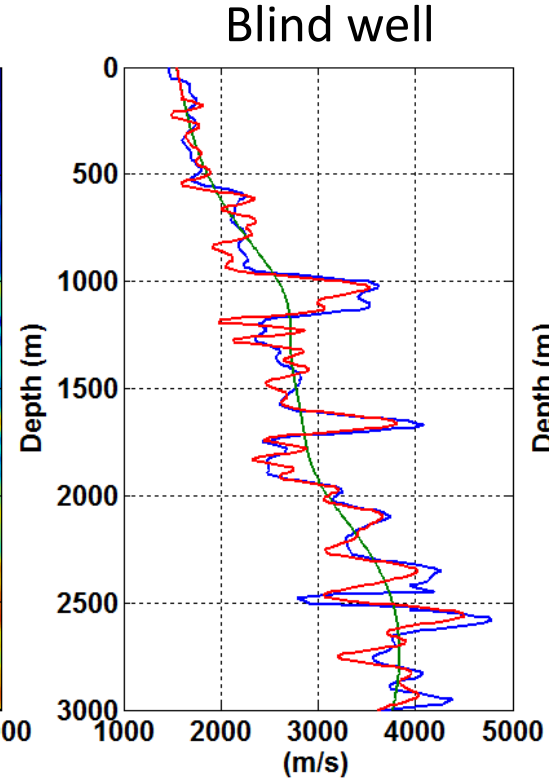
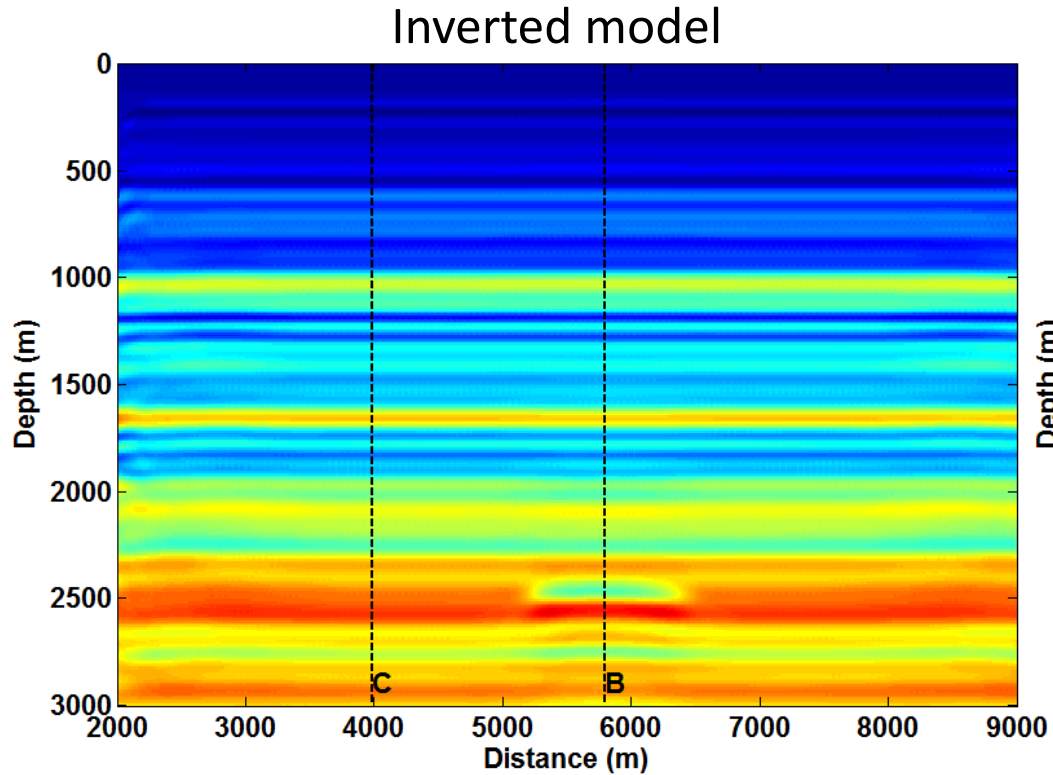
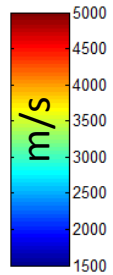
Evolution of the inverted model with more iterations

Iteration
13



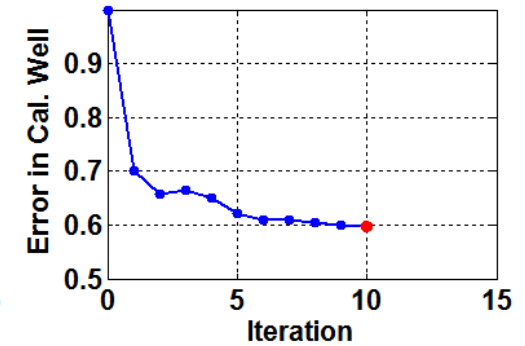
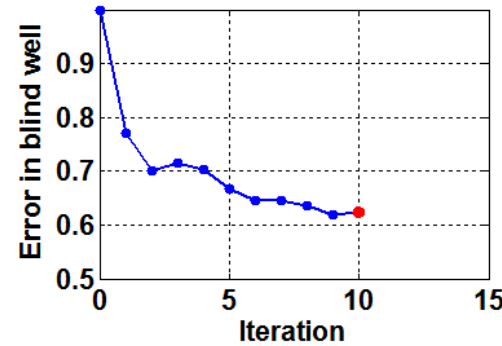
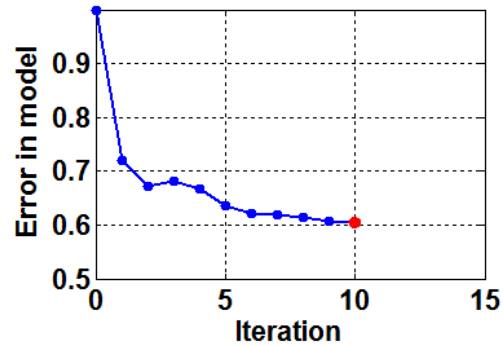
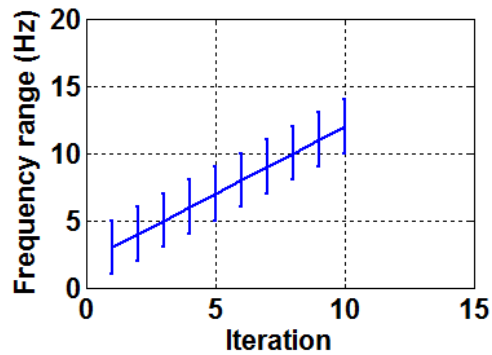
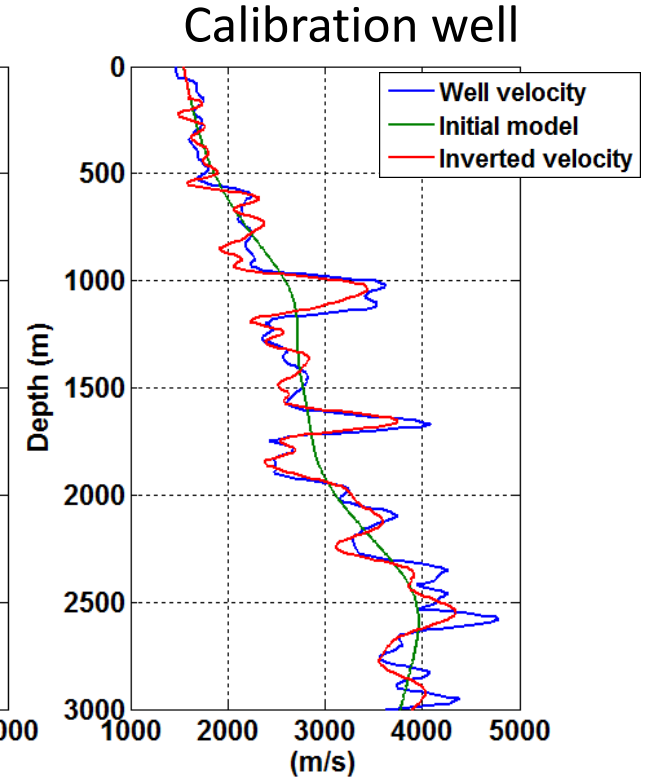
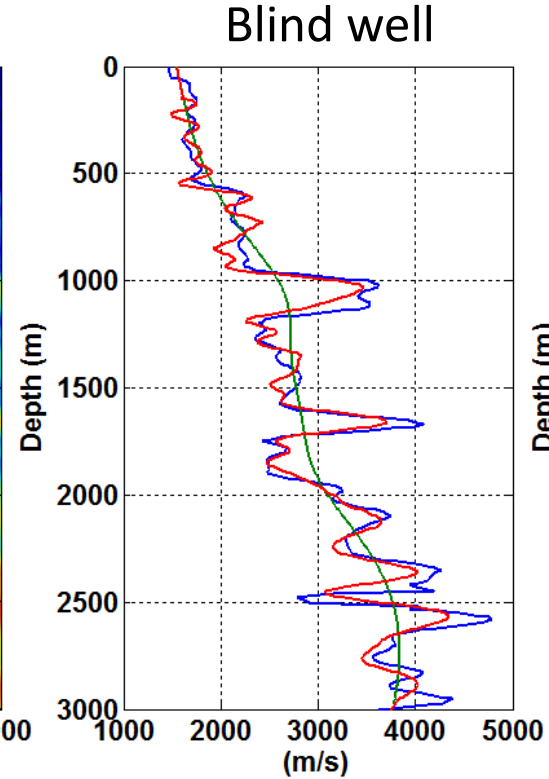
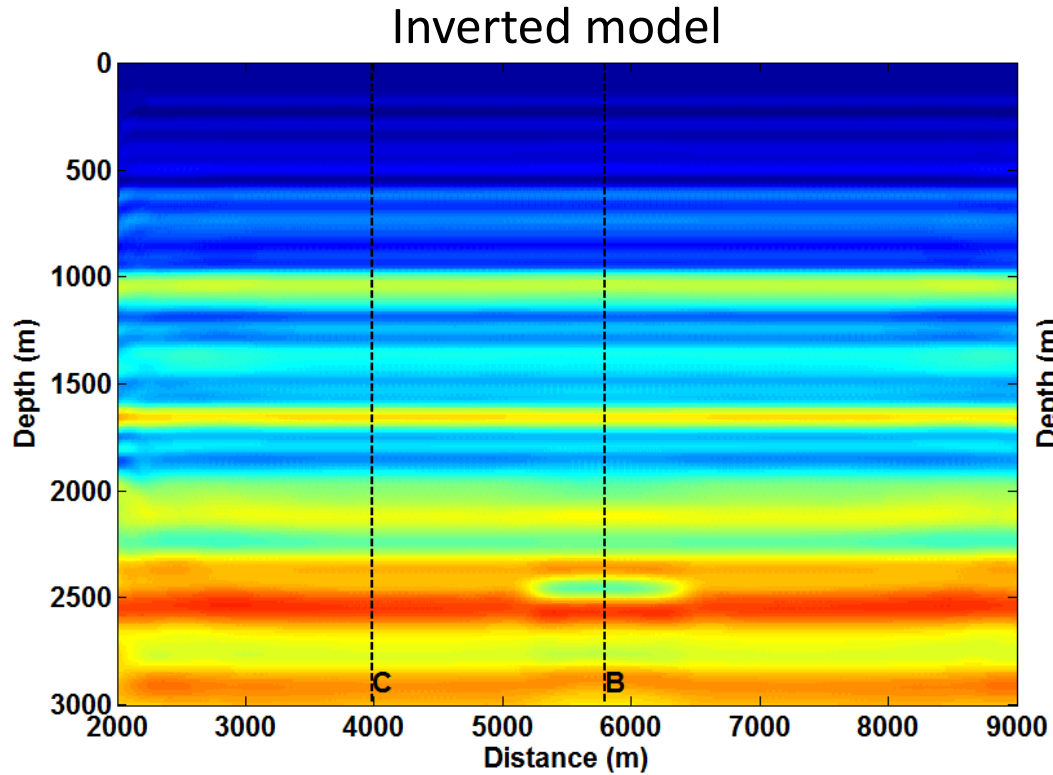
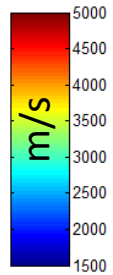
Evolution of the inverted model with more iterations

Iteration
15



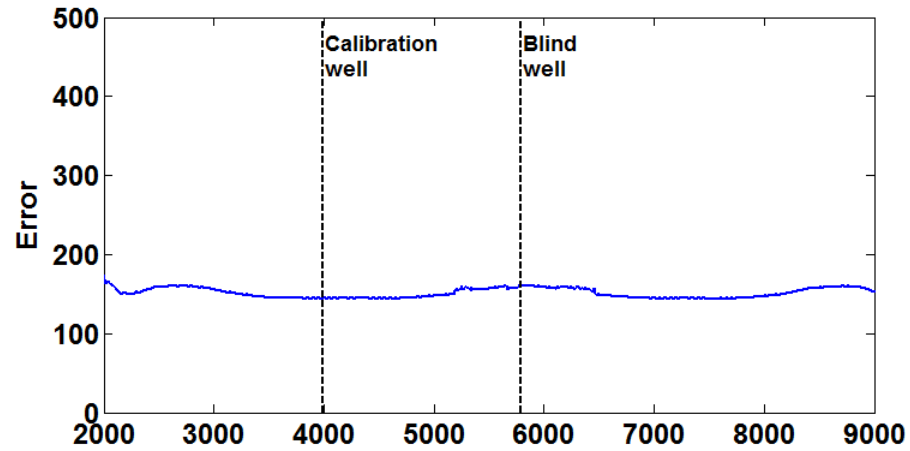
Evolution of the inverted model with more iterations

Iteration
10

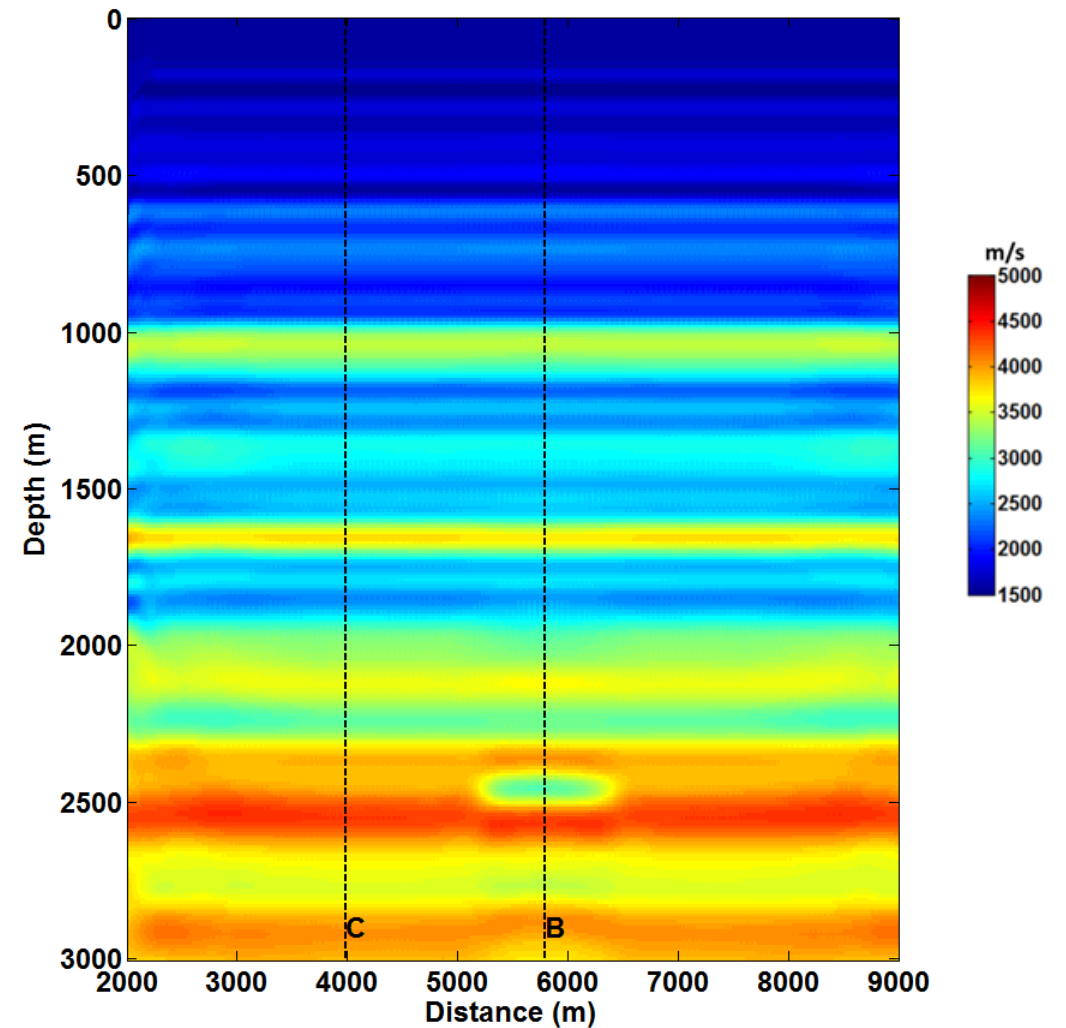


Spatial distribution of the error

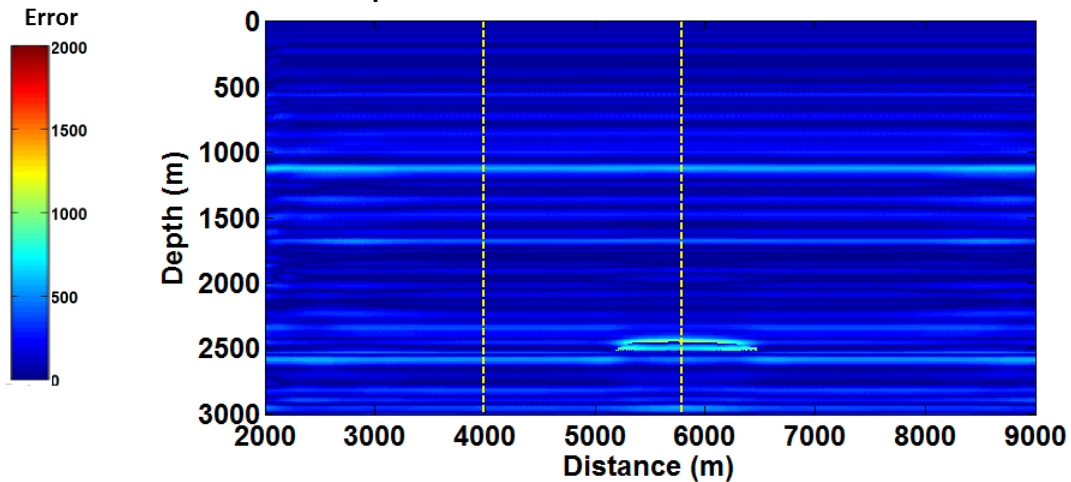
Horizontal distribution of the error



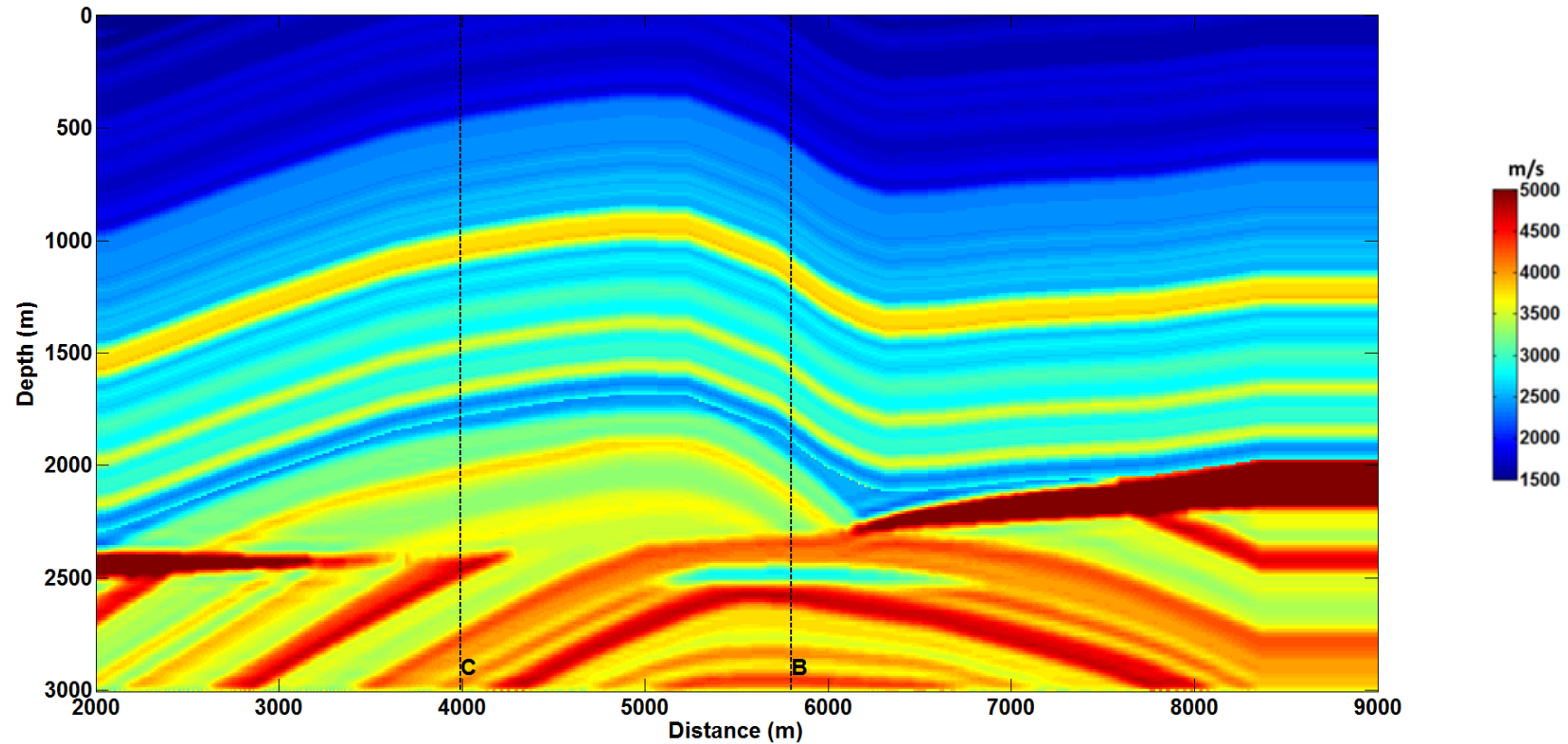
Inverted velocity model



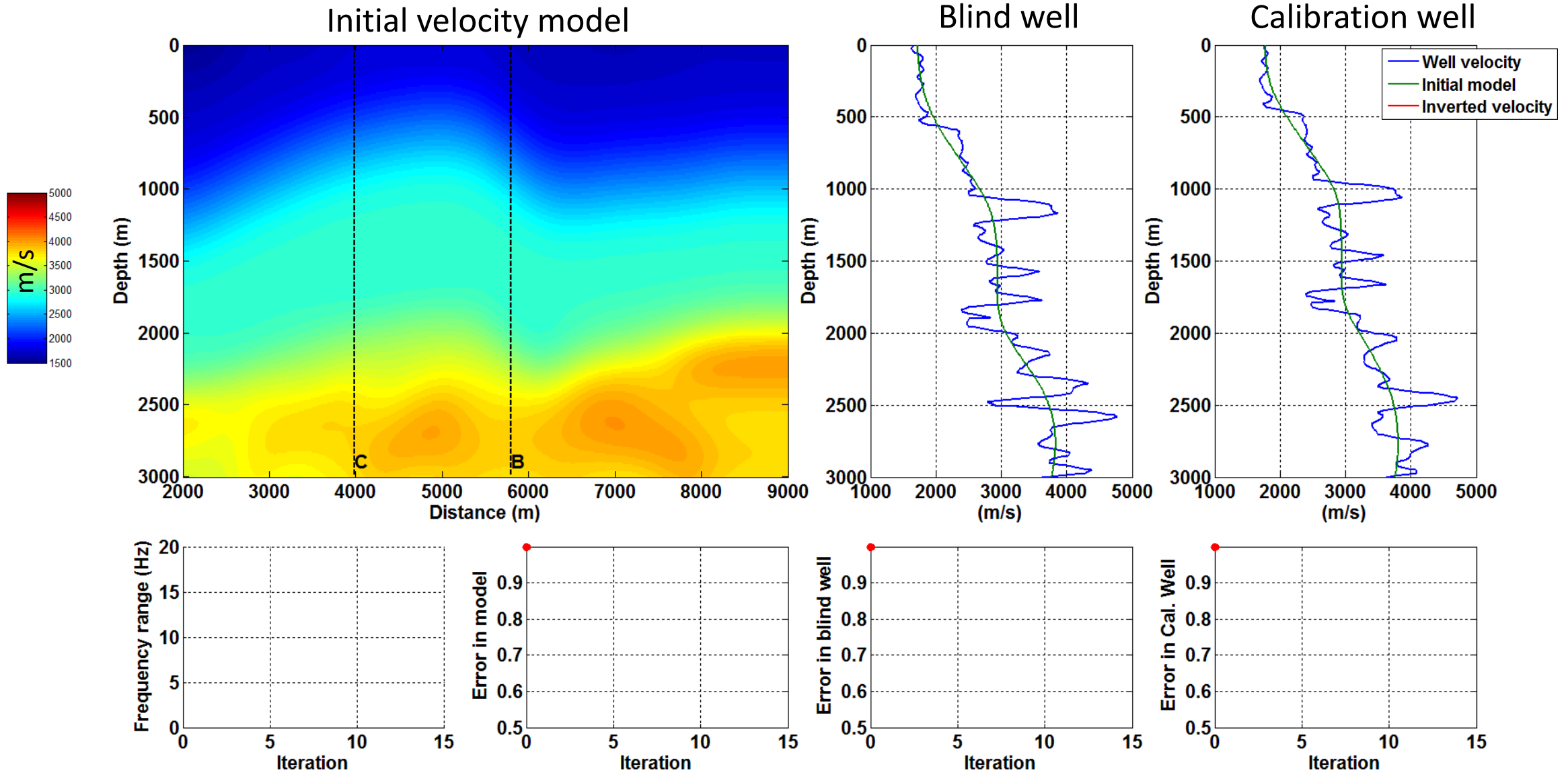
Spatial distribution of the error



Model 2

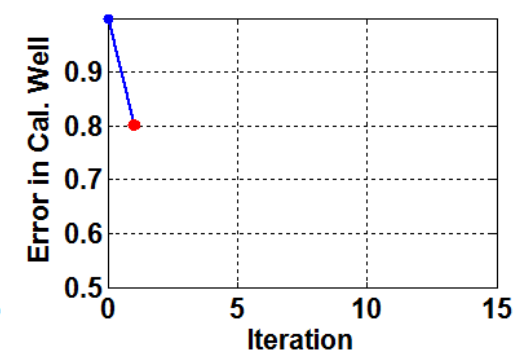
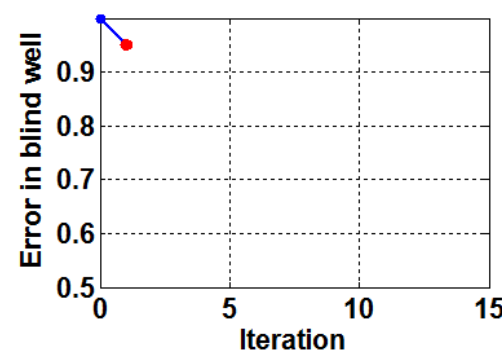
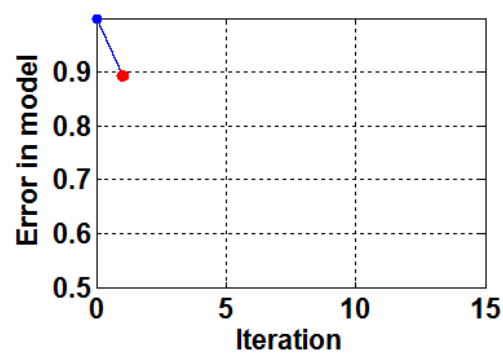
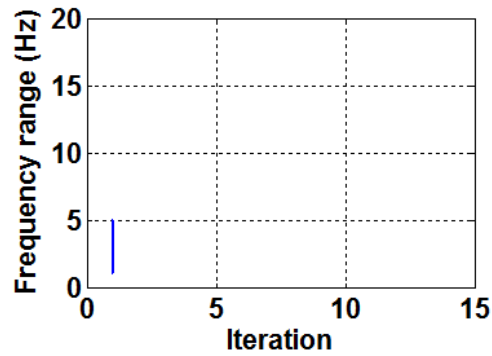
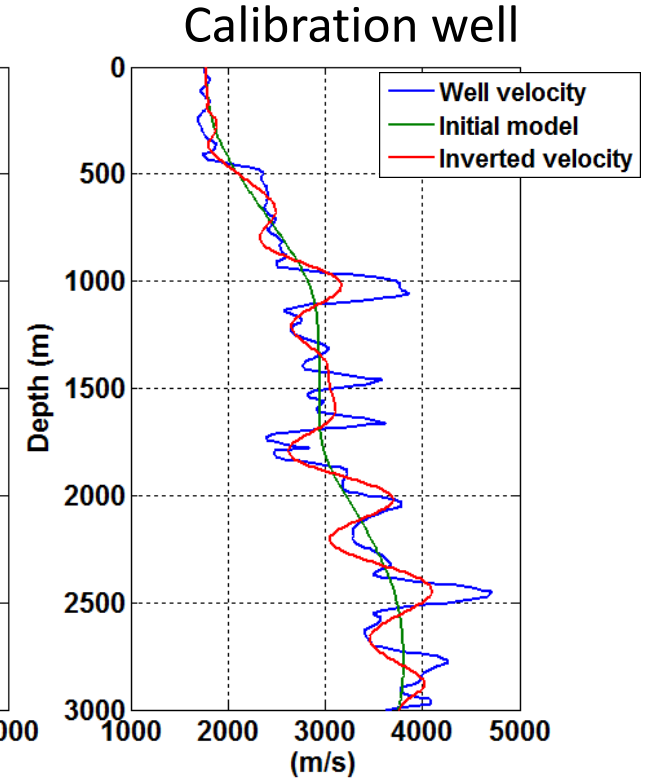
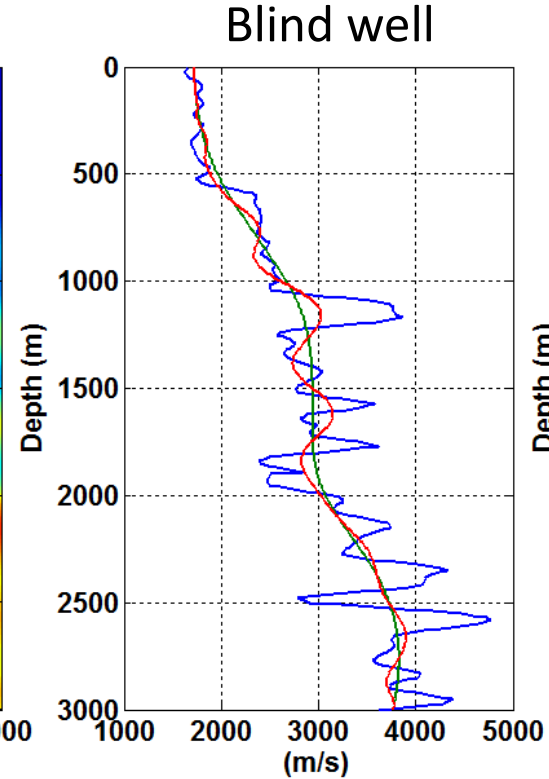
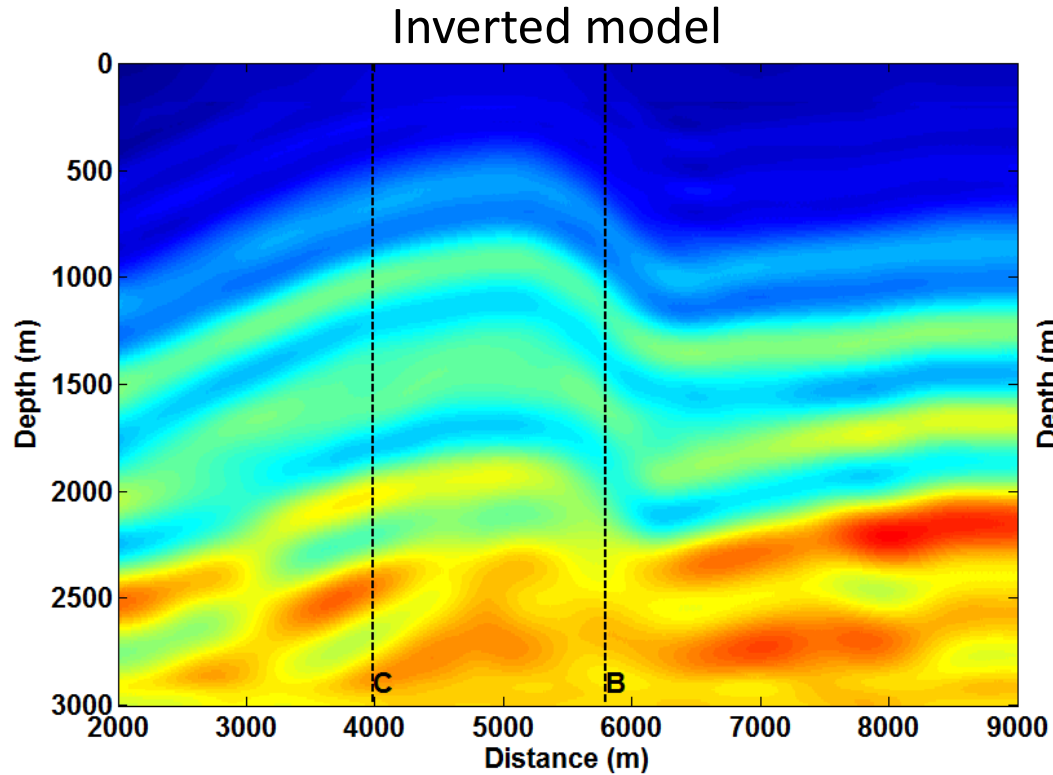
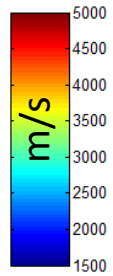


Evolution of the inverted model with more iterations



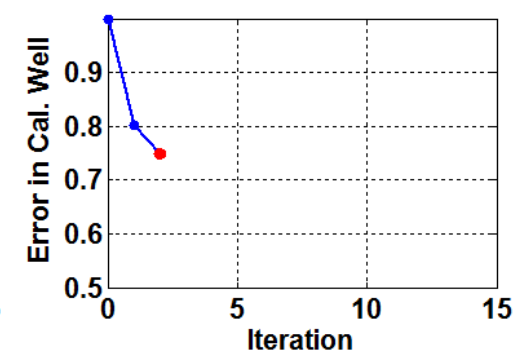
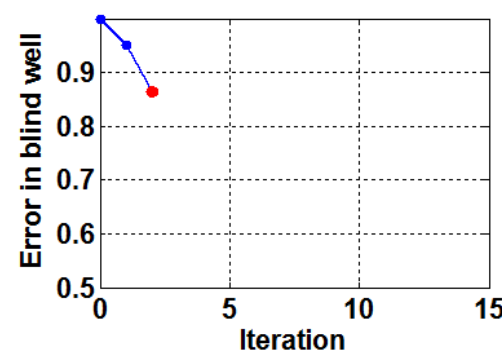
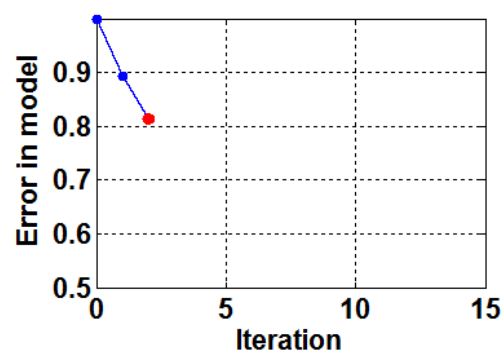
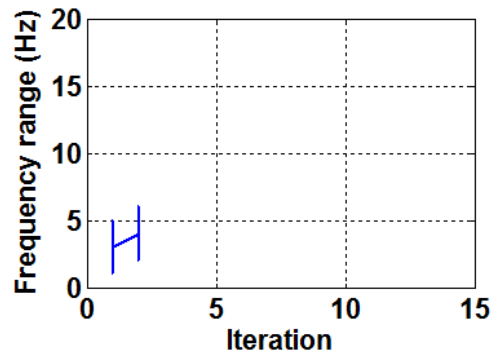
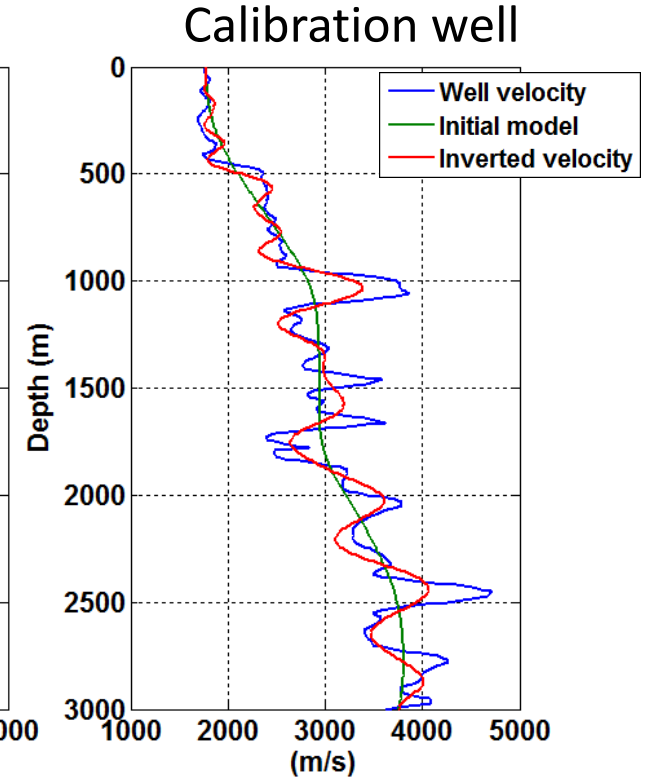
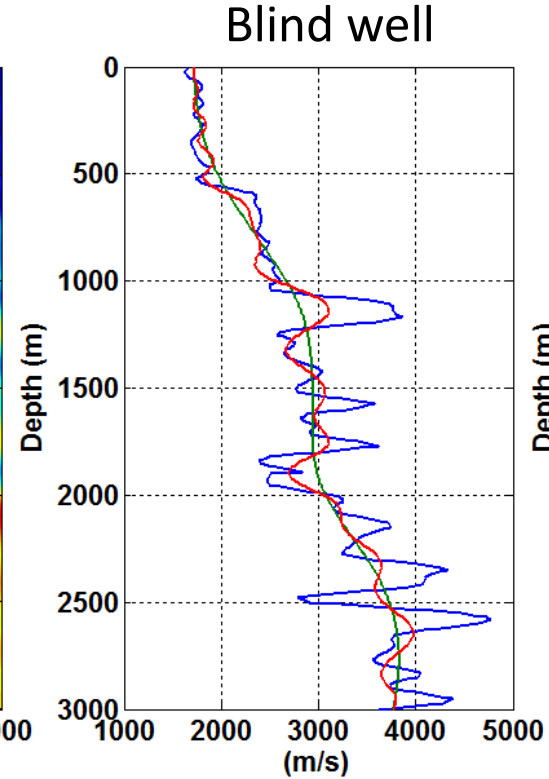
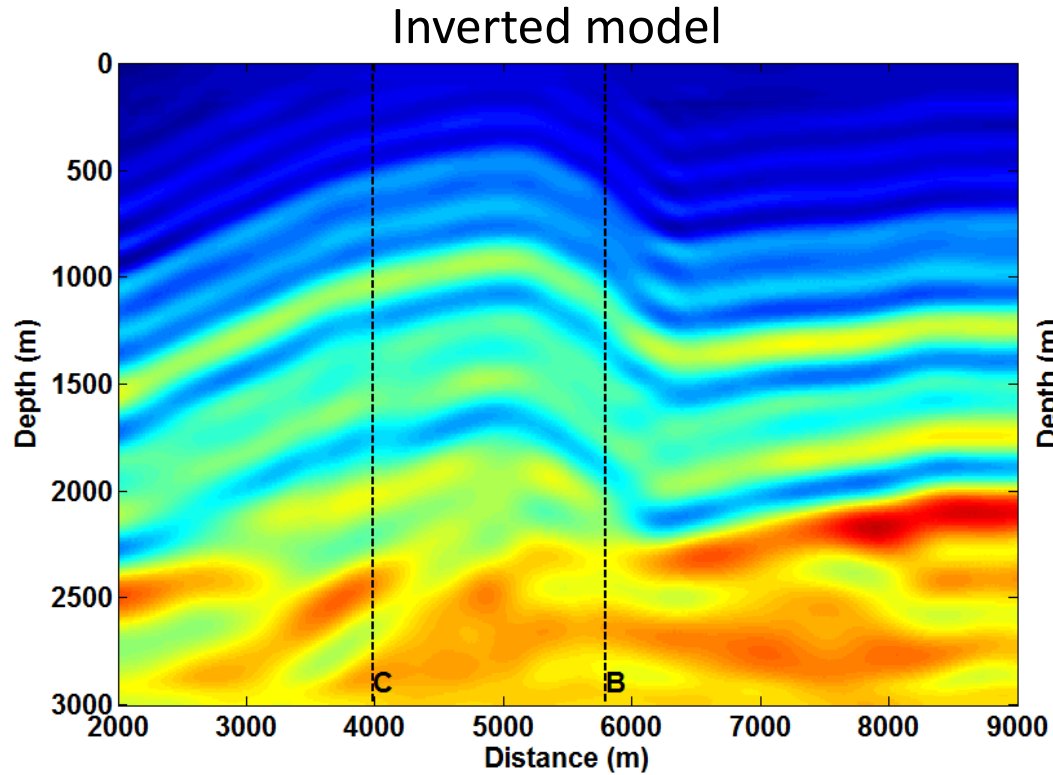
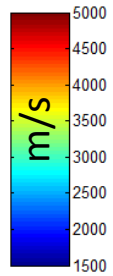
Evolution of the inverted model with more iterations

Iteration
1



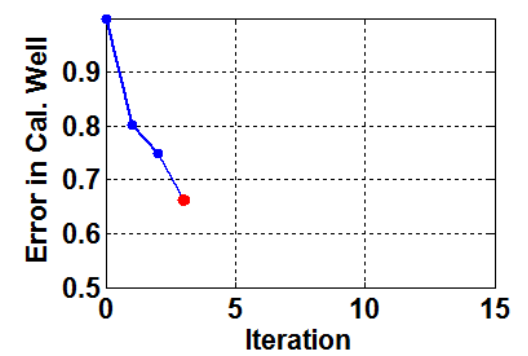
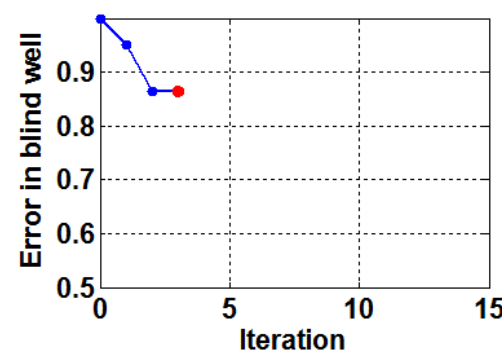
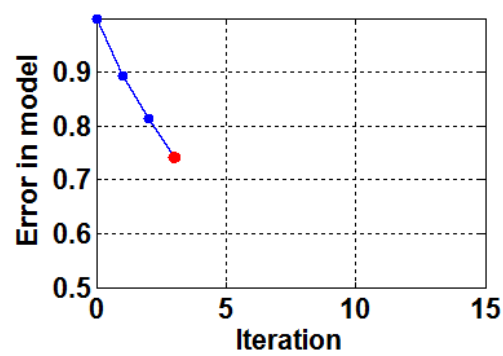
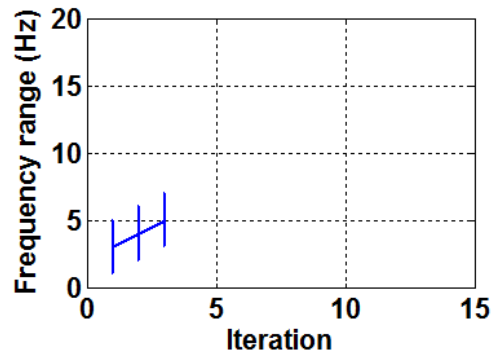
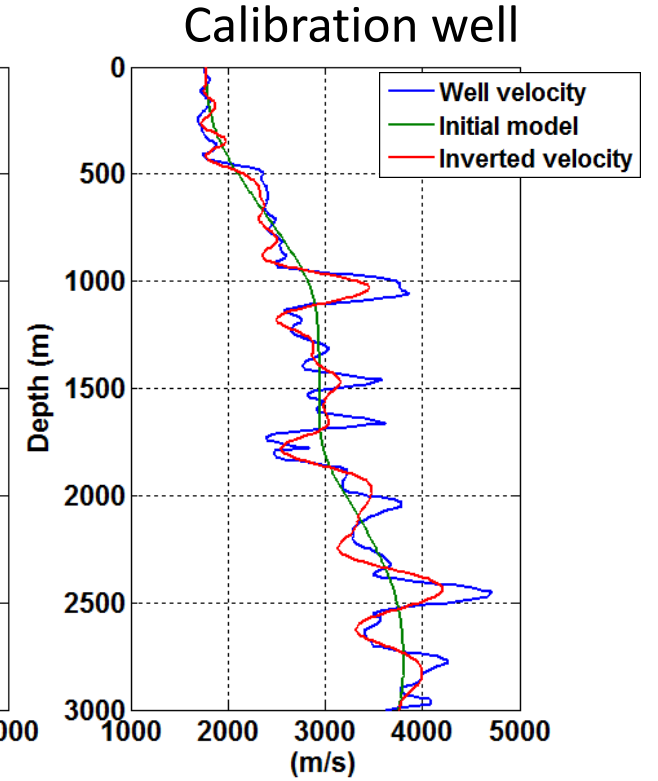
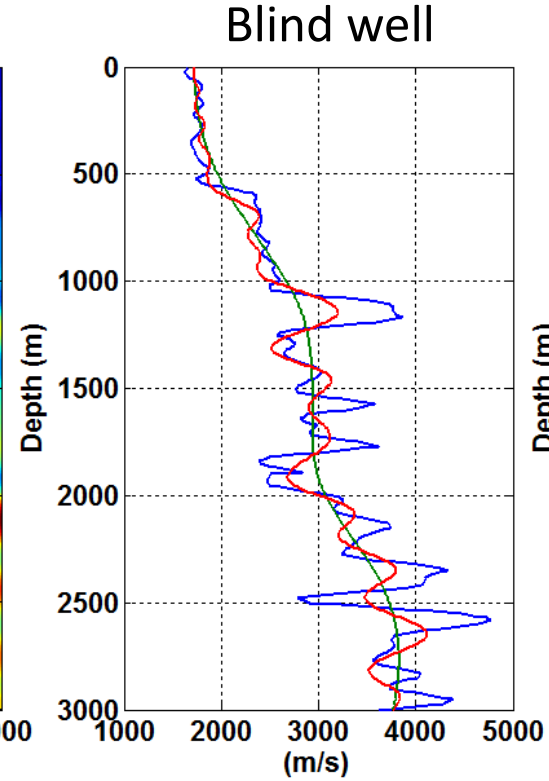
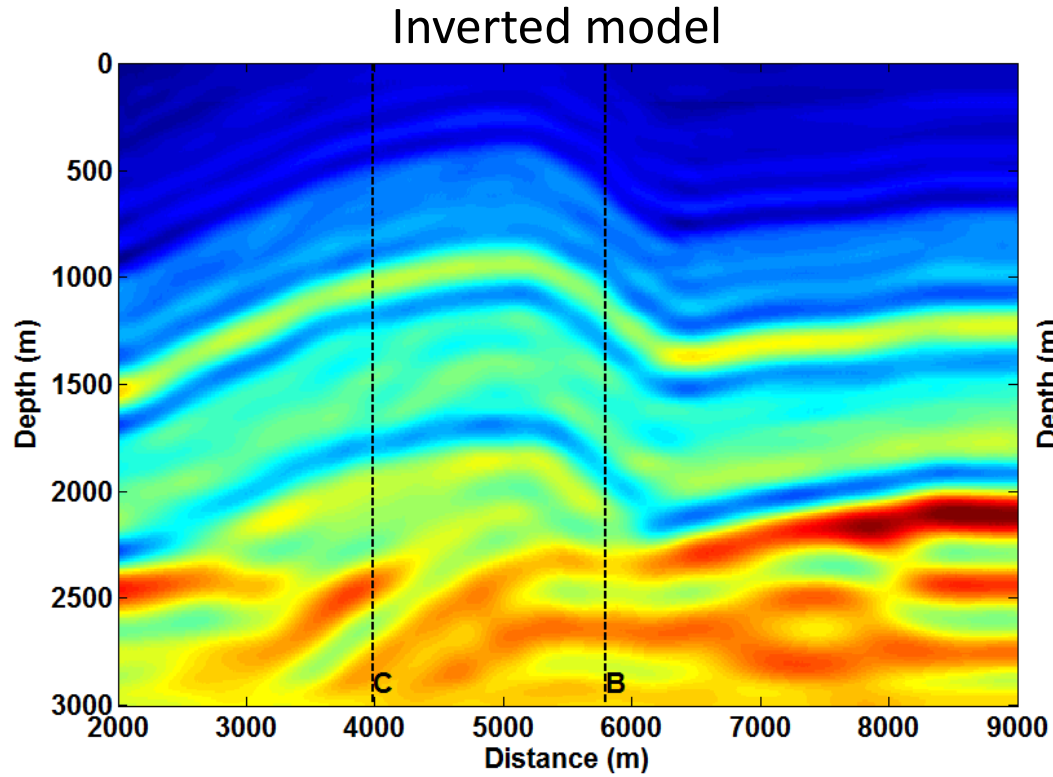
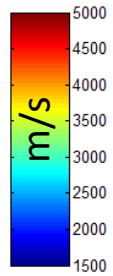
Evolution of the inverted model with more iterations

Iteration
2



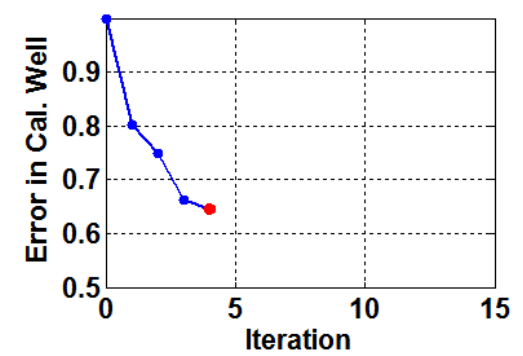
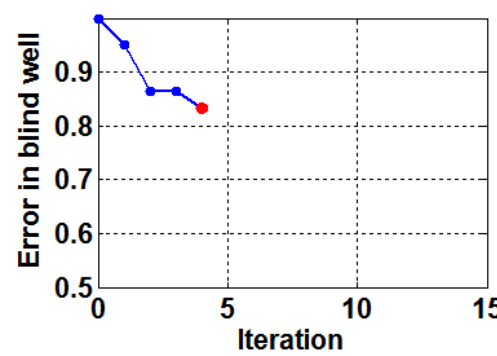
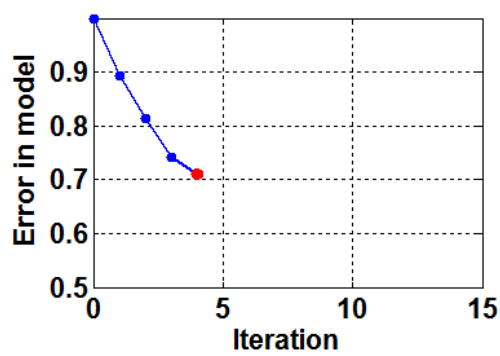
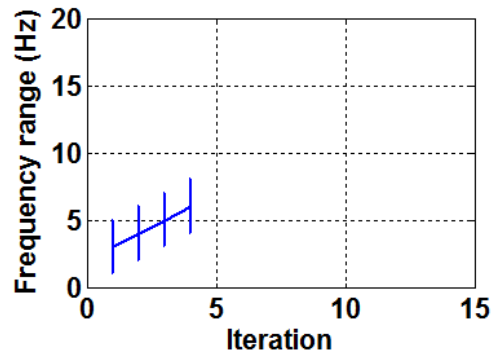
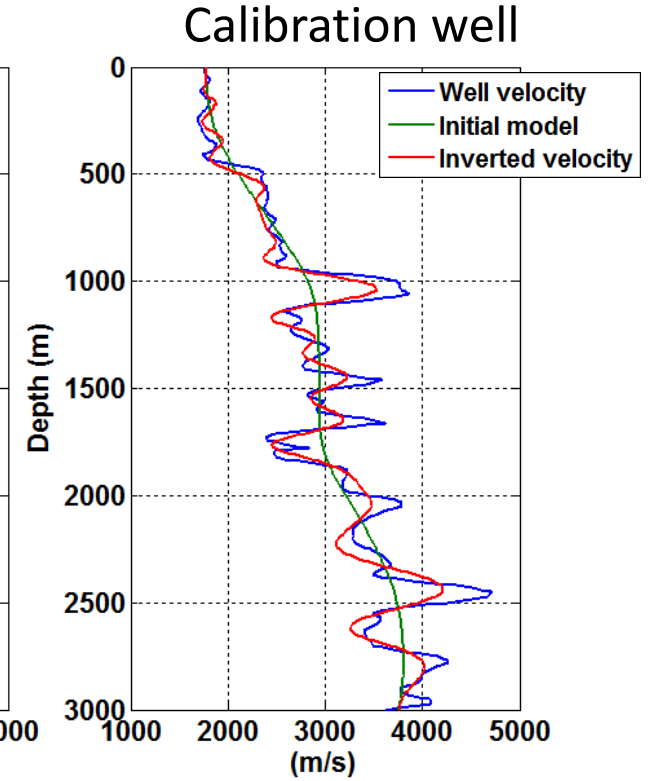
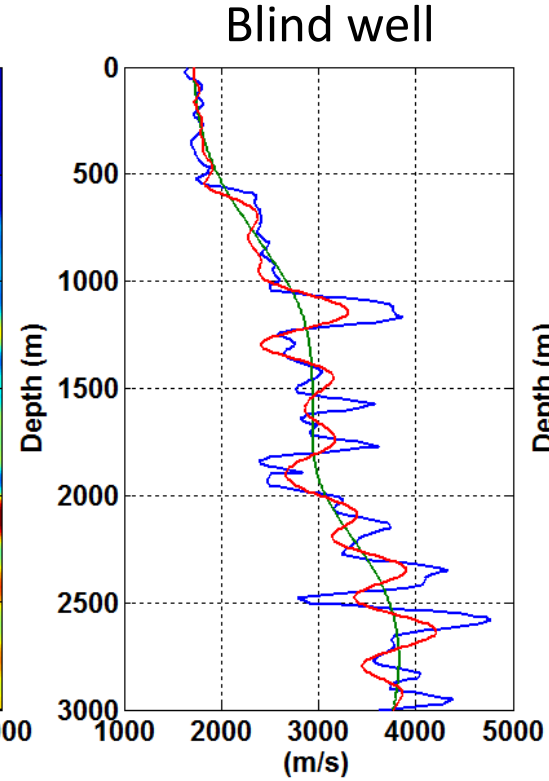
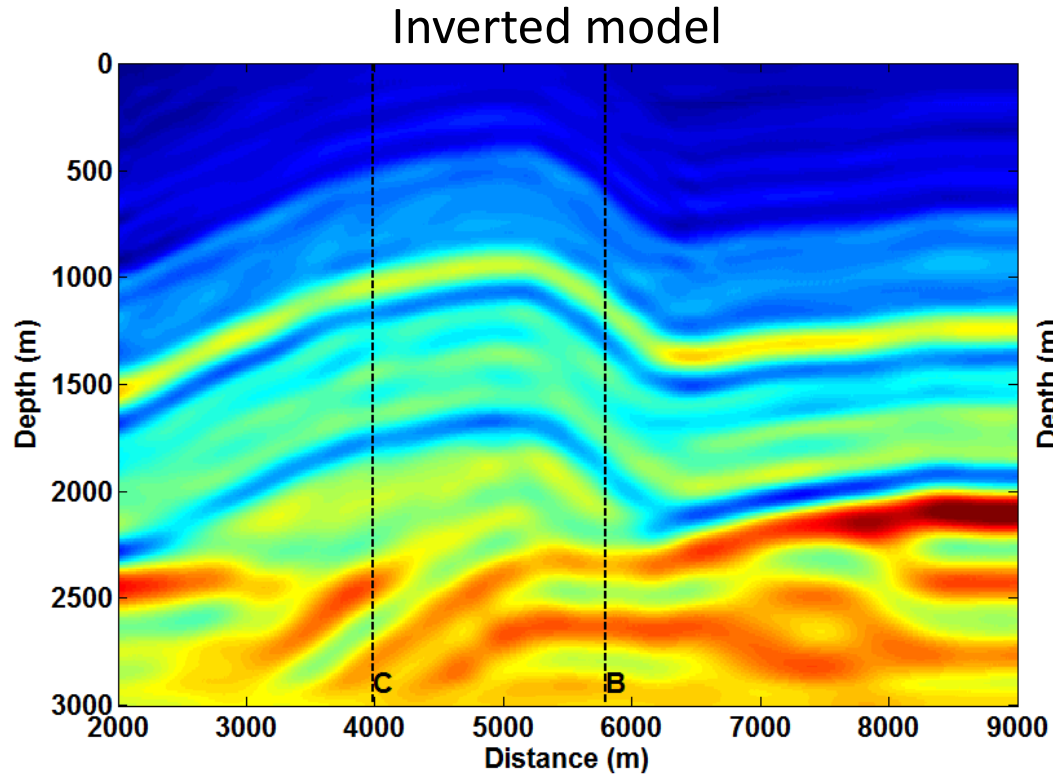
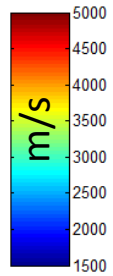
Evolution of the inverted model with more iterations

Iteration
3



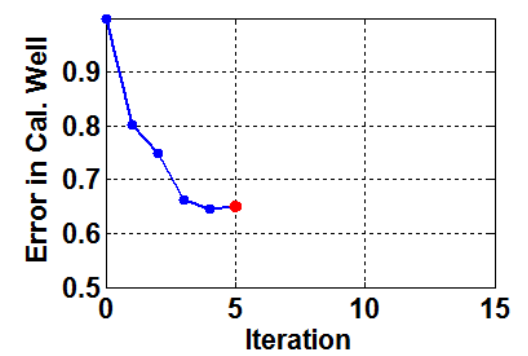
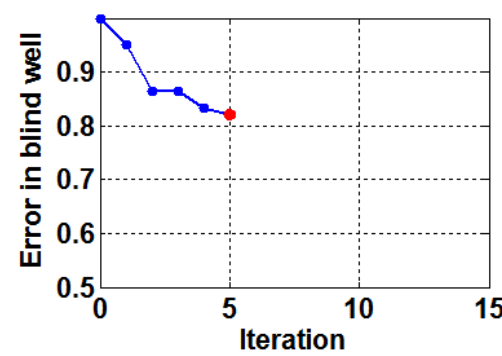
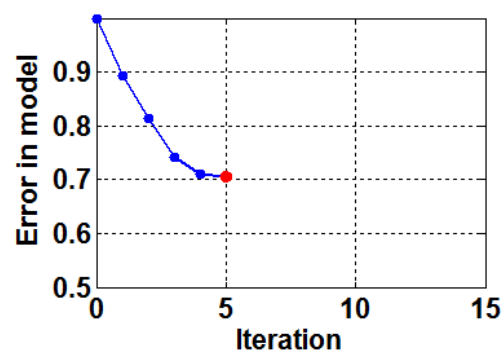
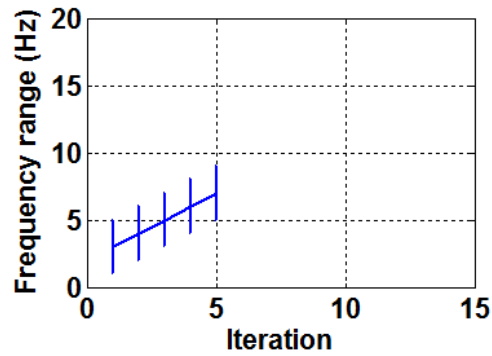
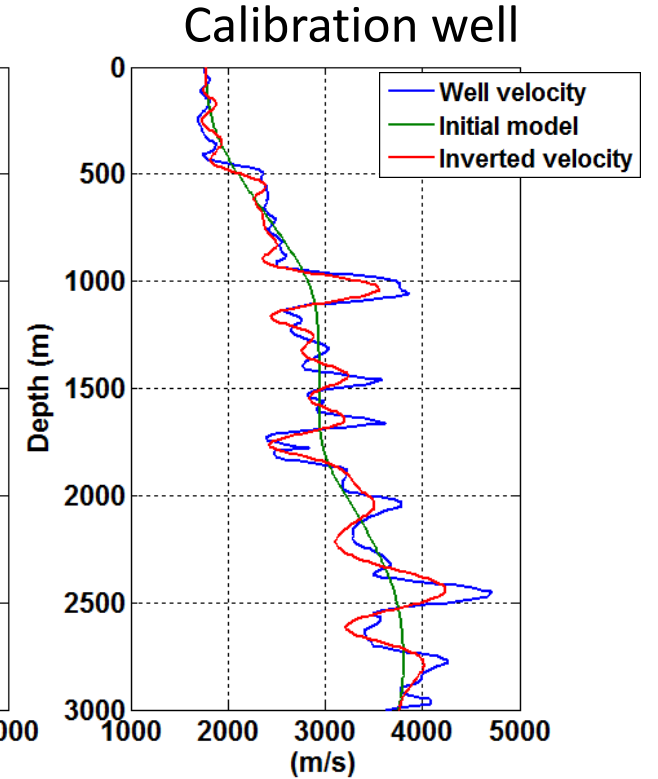
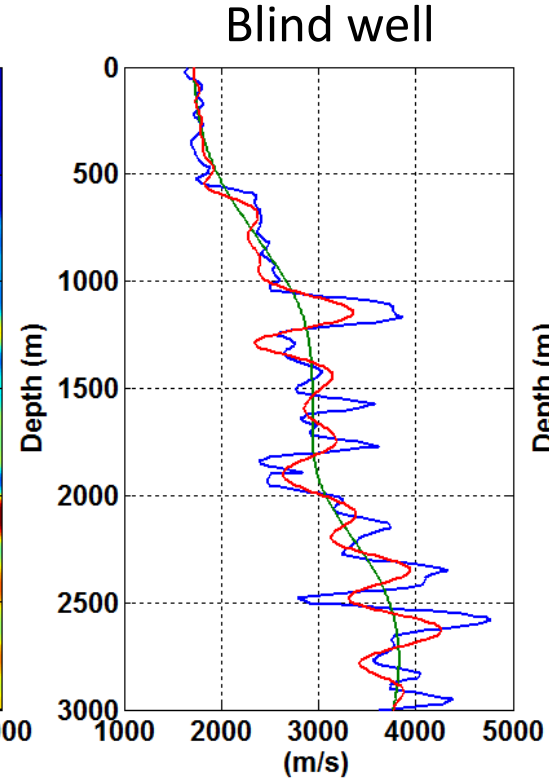
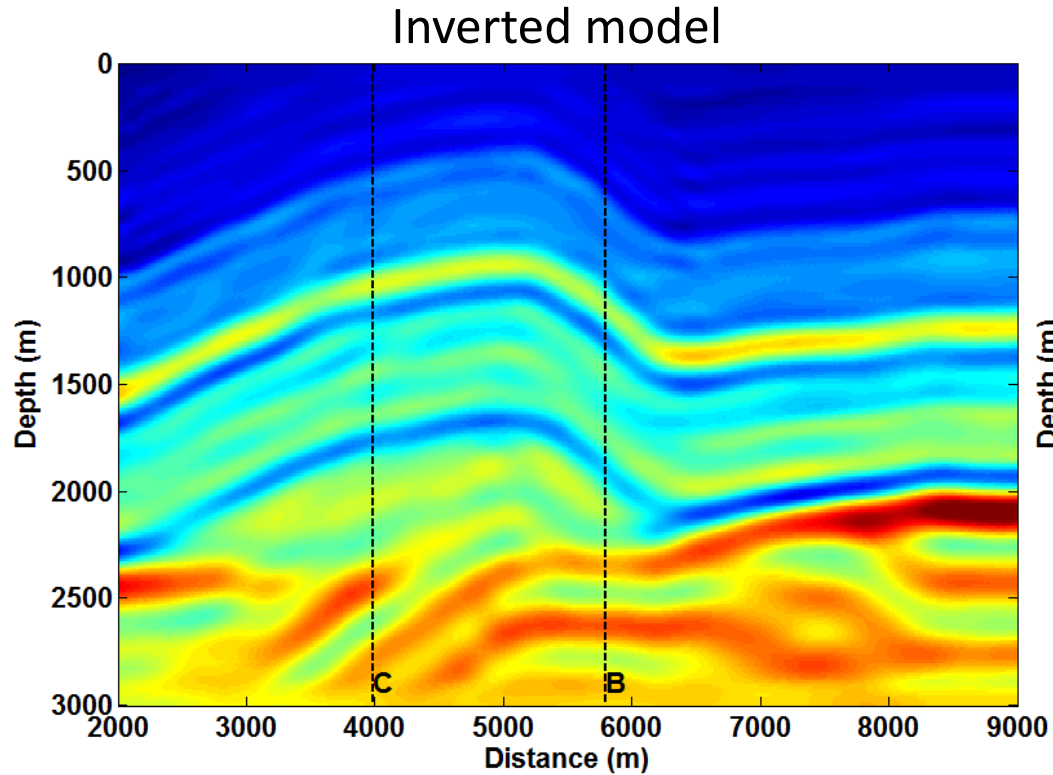
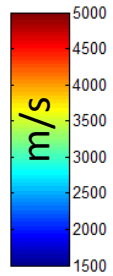
Evolution of the inverted model with more iterations

Iteration
4



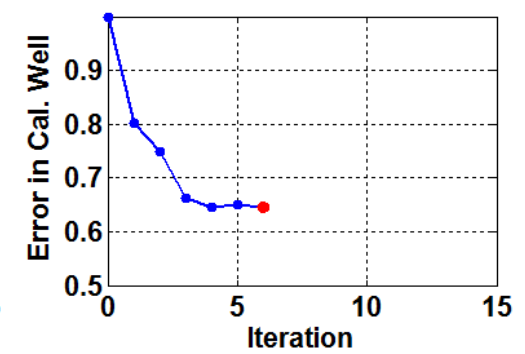
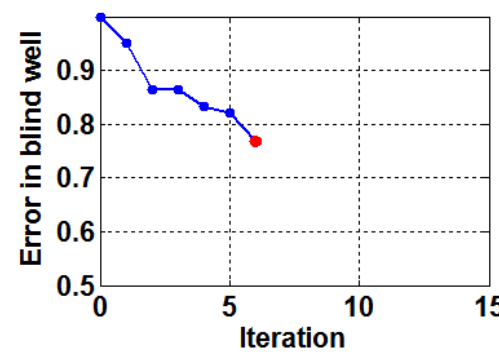
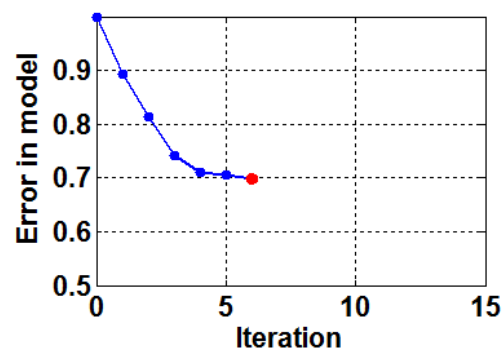
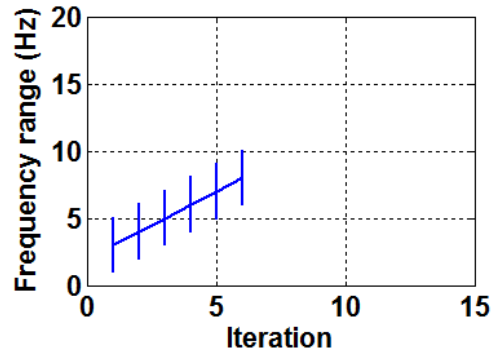
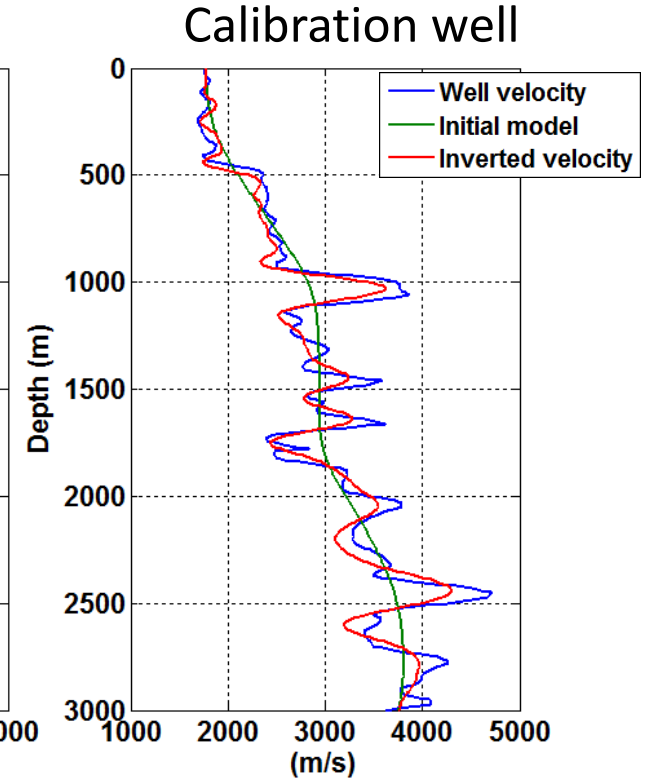
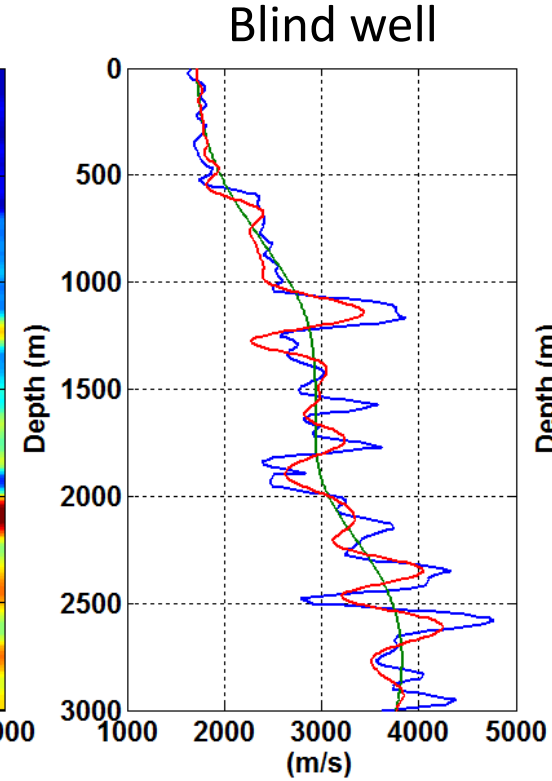
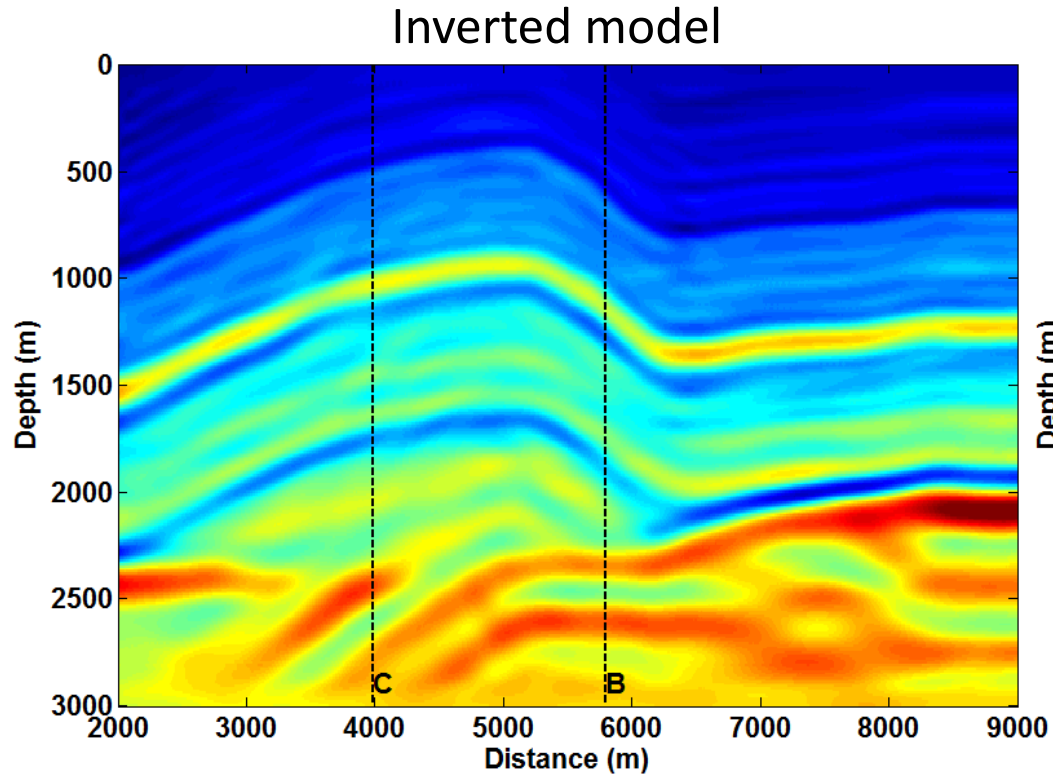
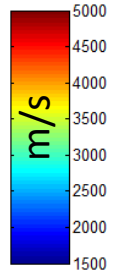
Evolution of the inverted model with more iterations

Iteration
5



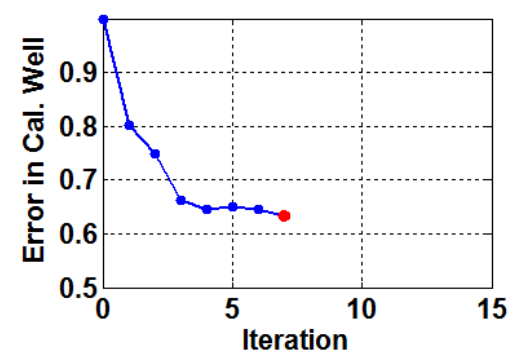
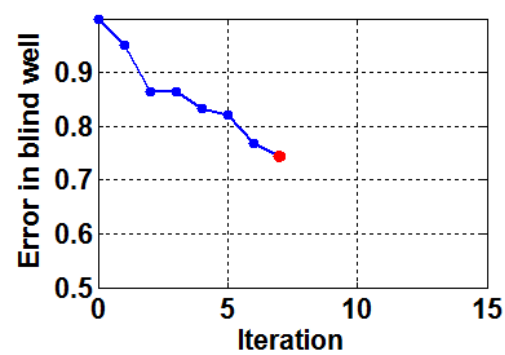
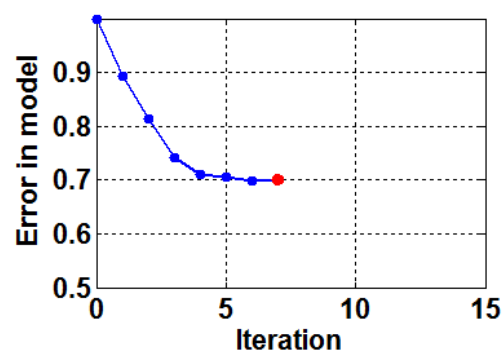
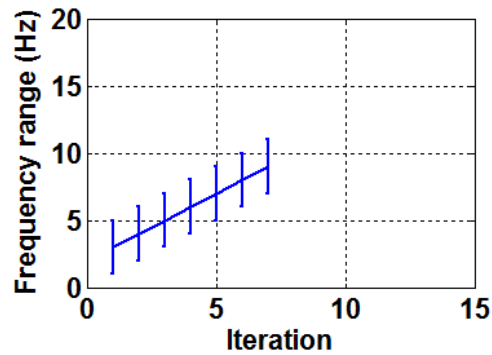
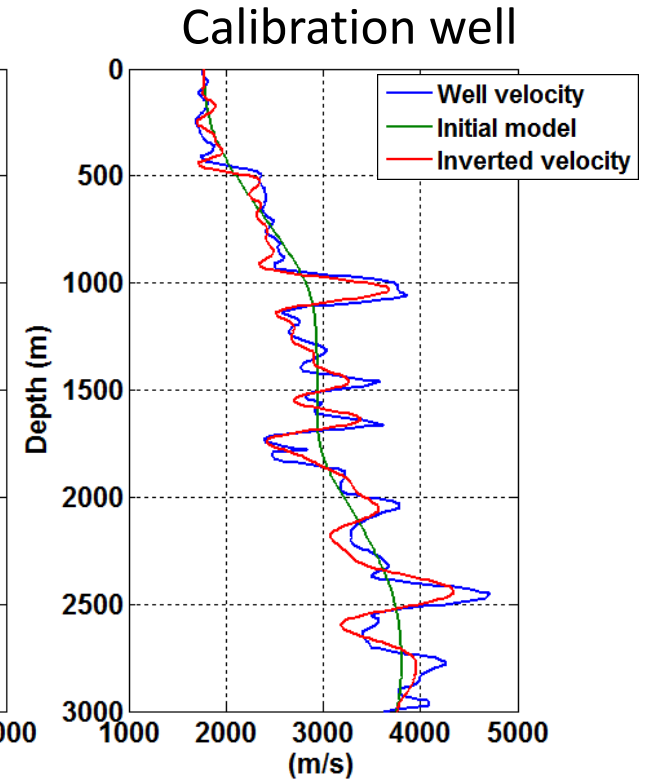
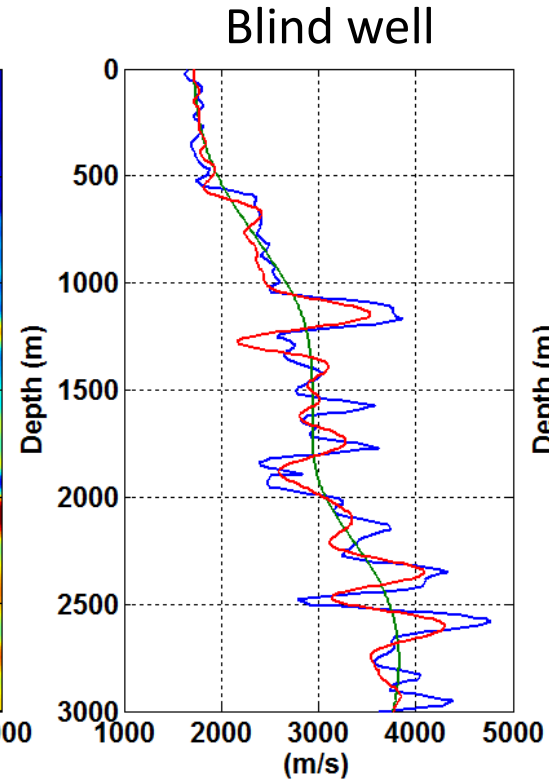
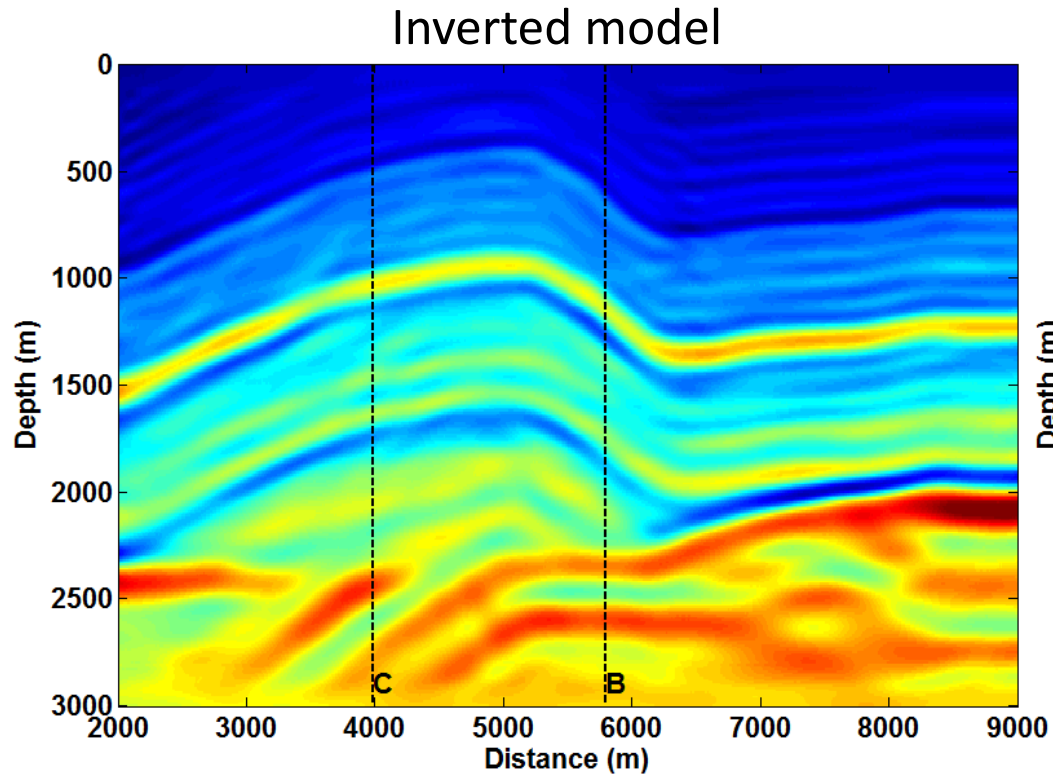
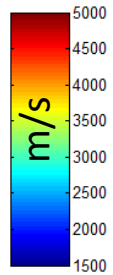
Evolution of the inverted model with more iterations

Iteration
6



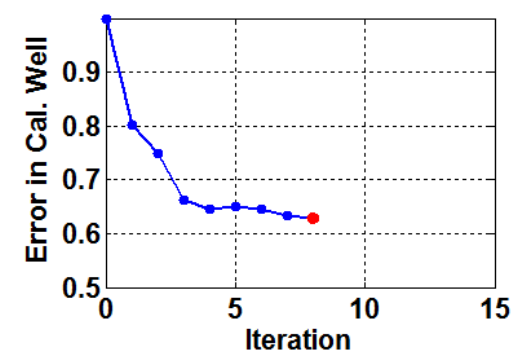
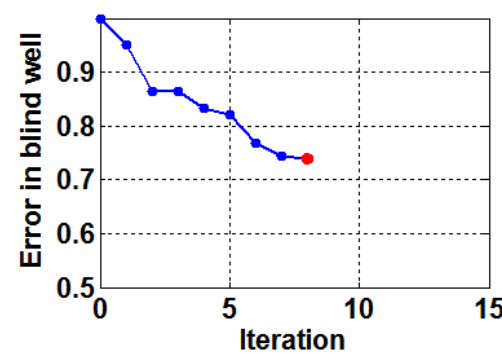
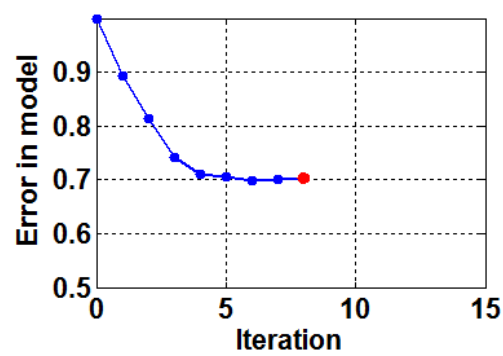
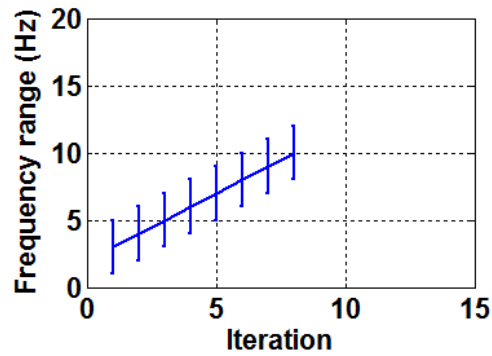
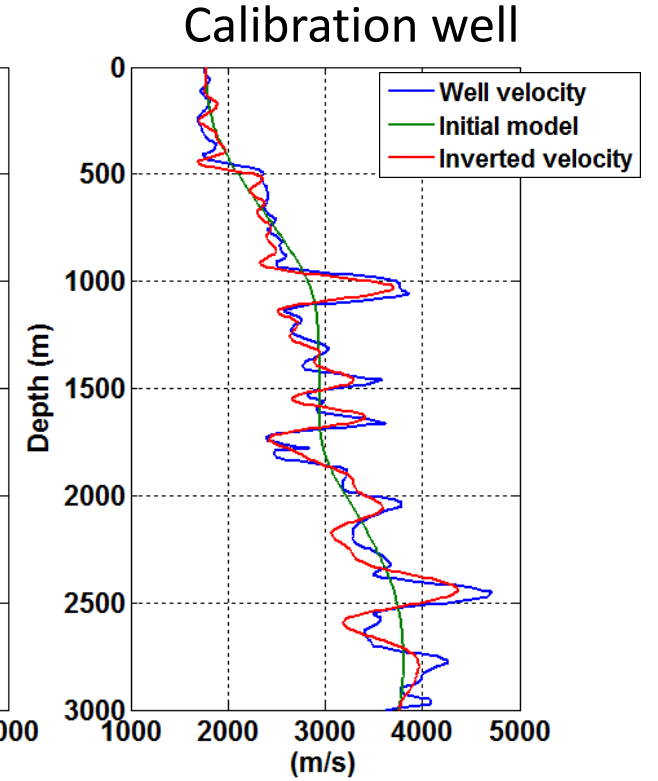
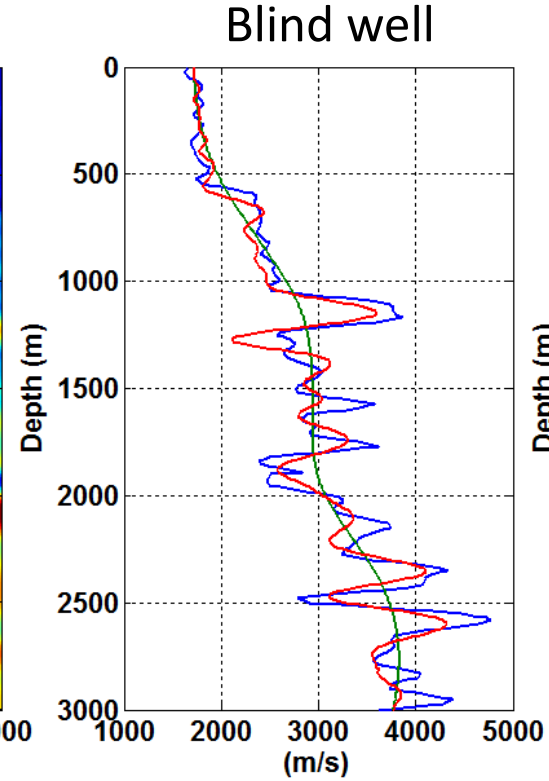
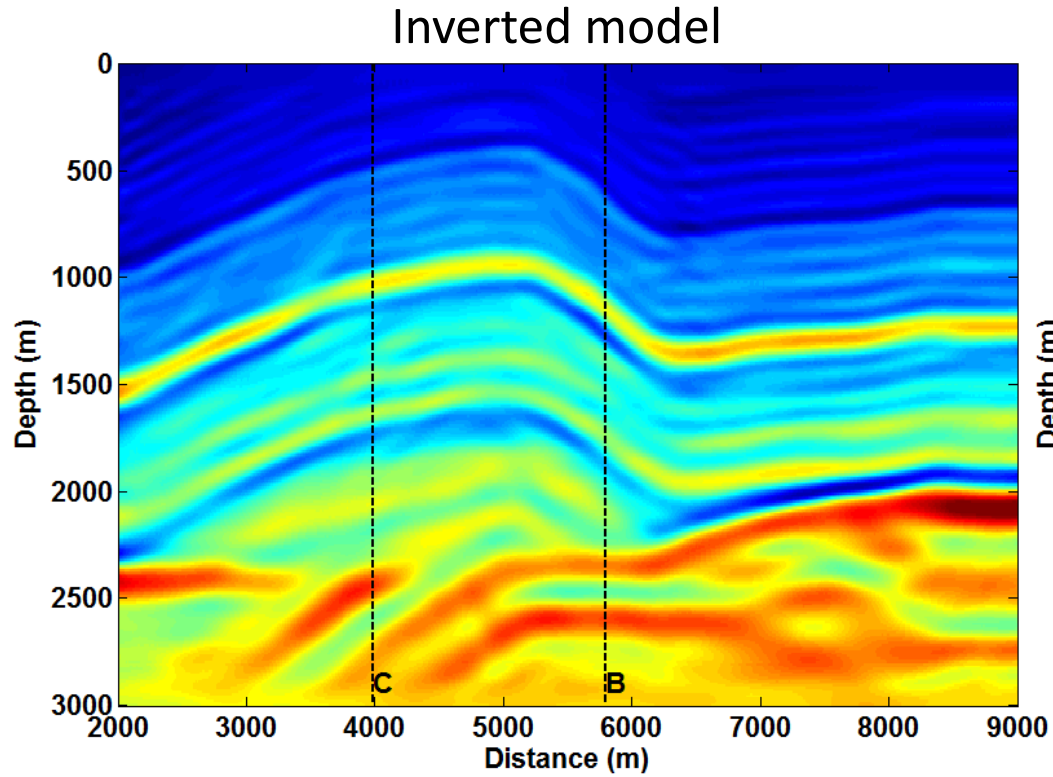
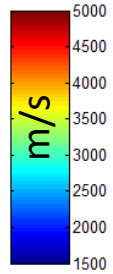
Evolution of the inverted model with more iterations

Iteration
7



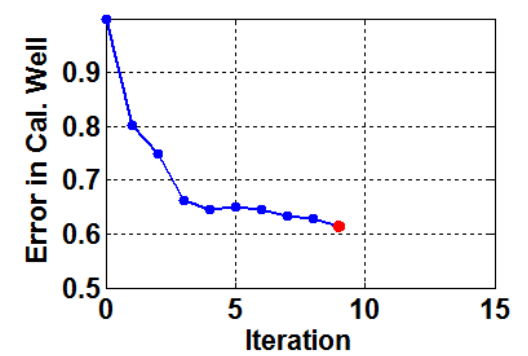
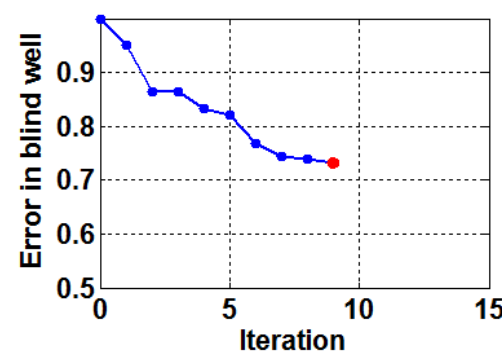
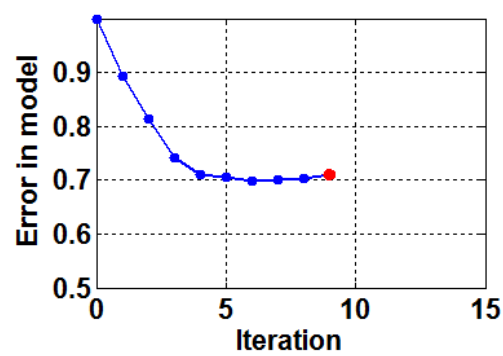
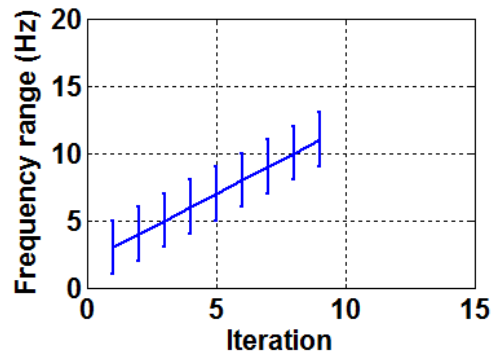
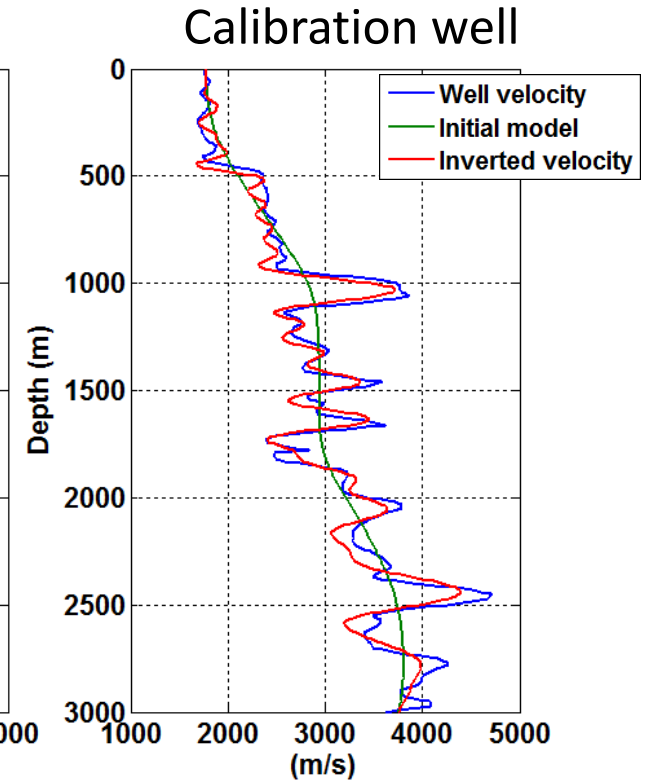
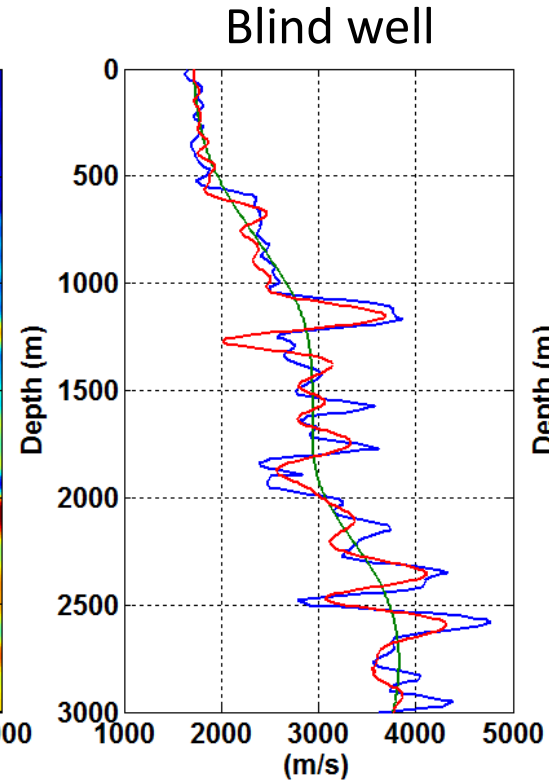
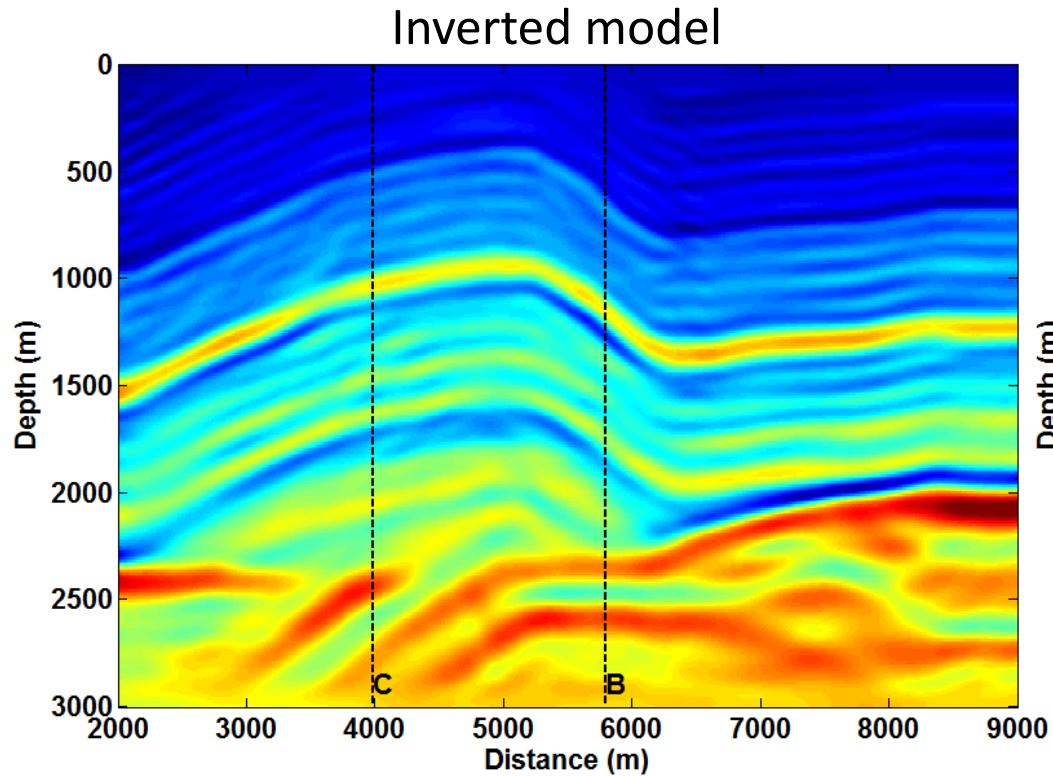
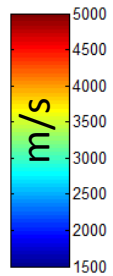
Evolution of the inverted model with more iterations

Iteration
8



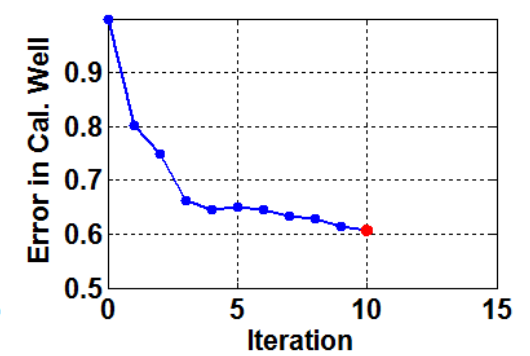
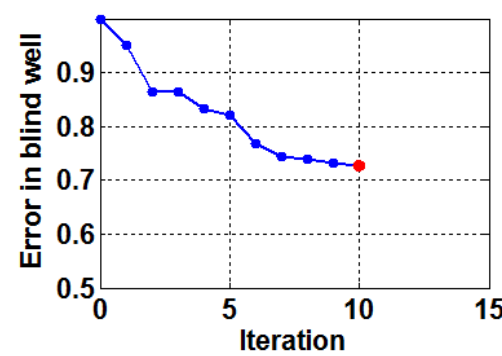
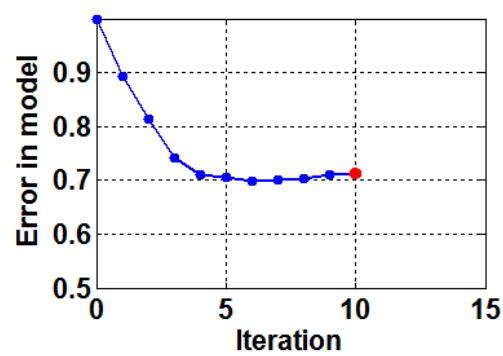
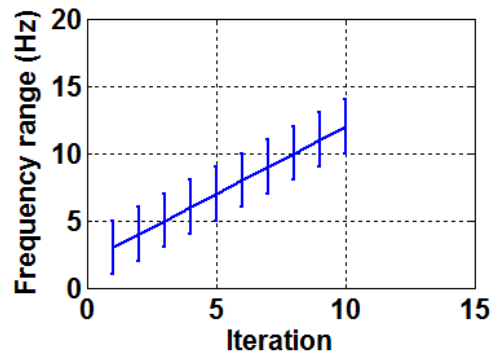
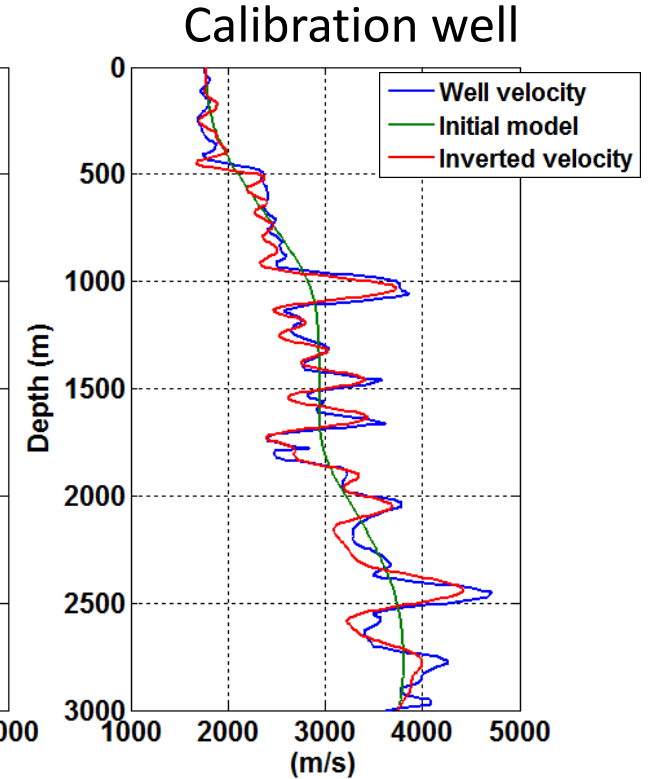
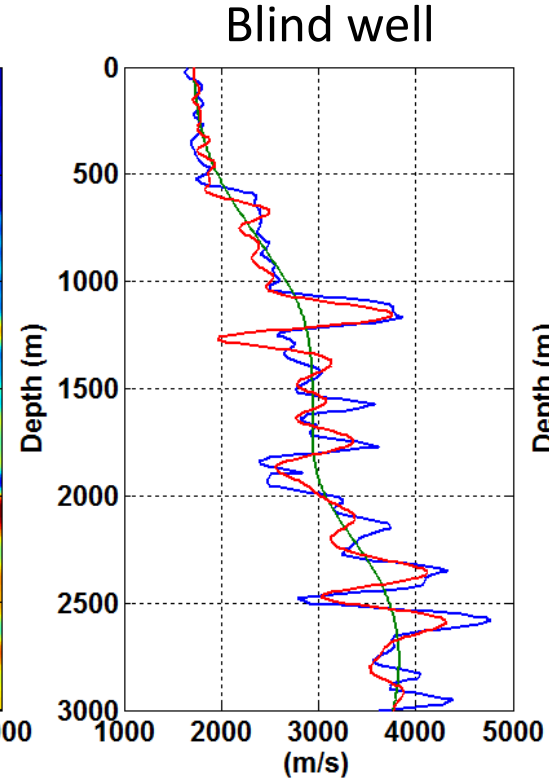
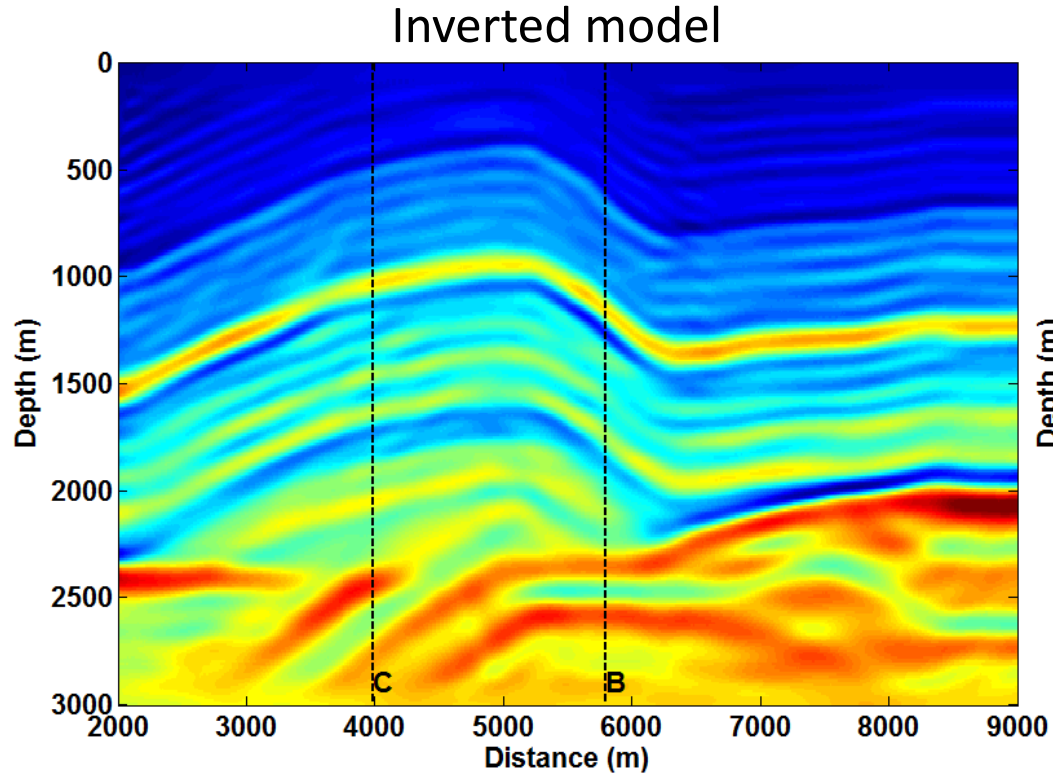
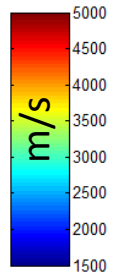
Evolution of the inverted model with more iterations

Iteration
9



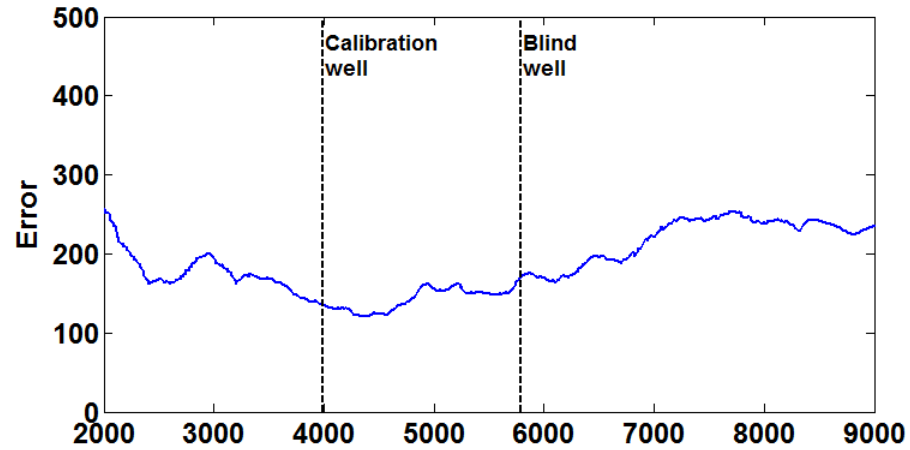
Evolution of the inverted model with more iterations

Iteration
10

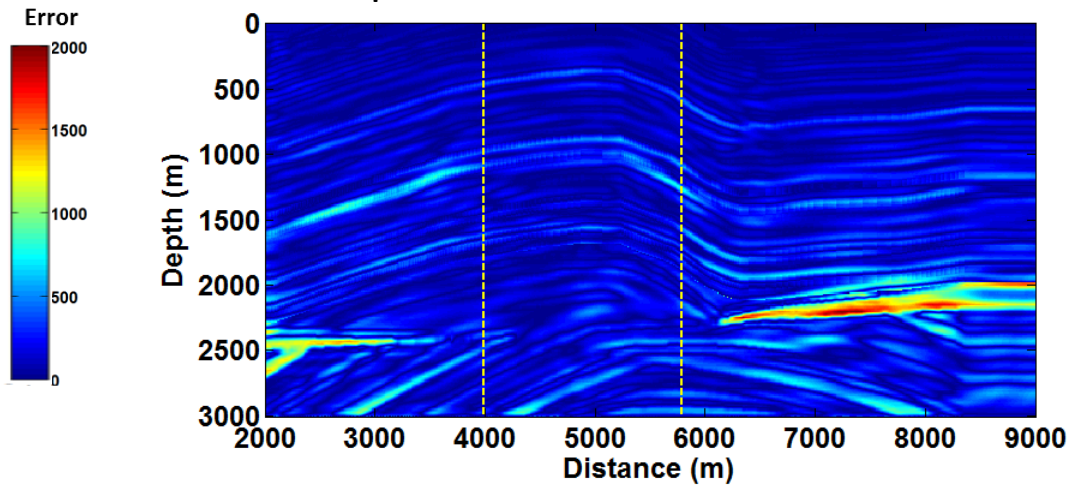


Spatial distribution of the error

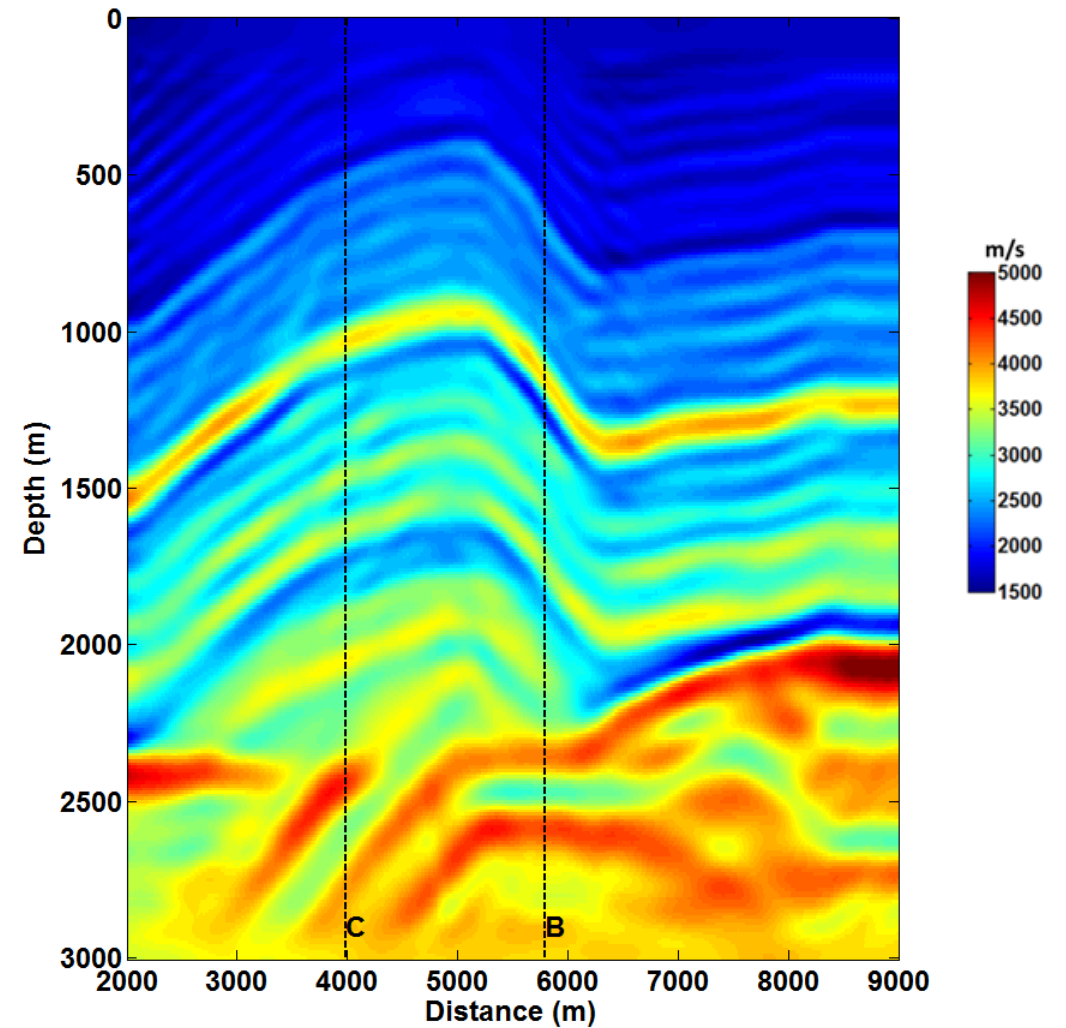
Horizontal distribution of the error



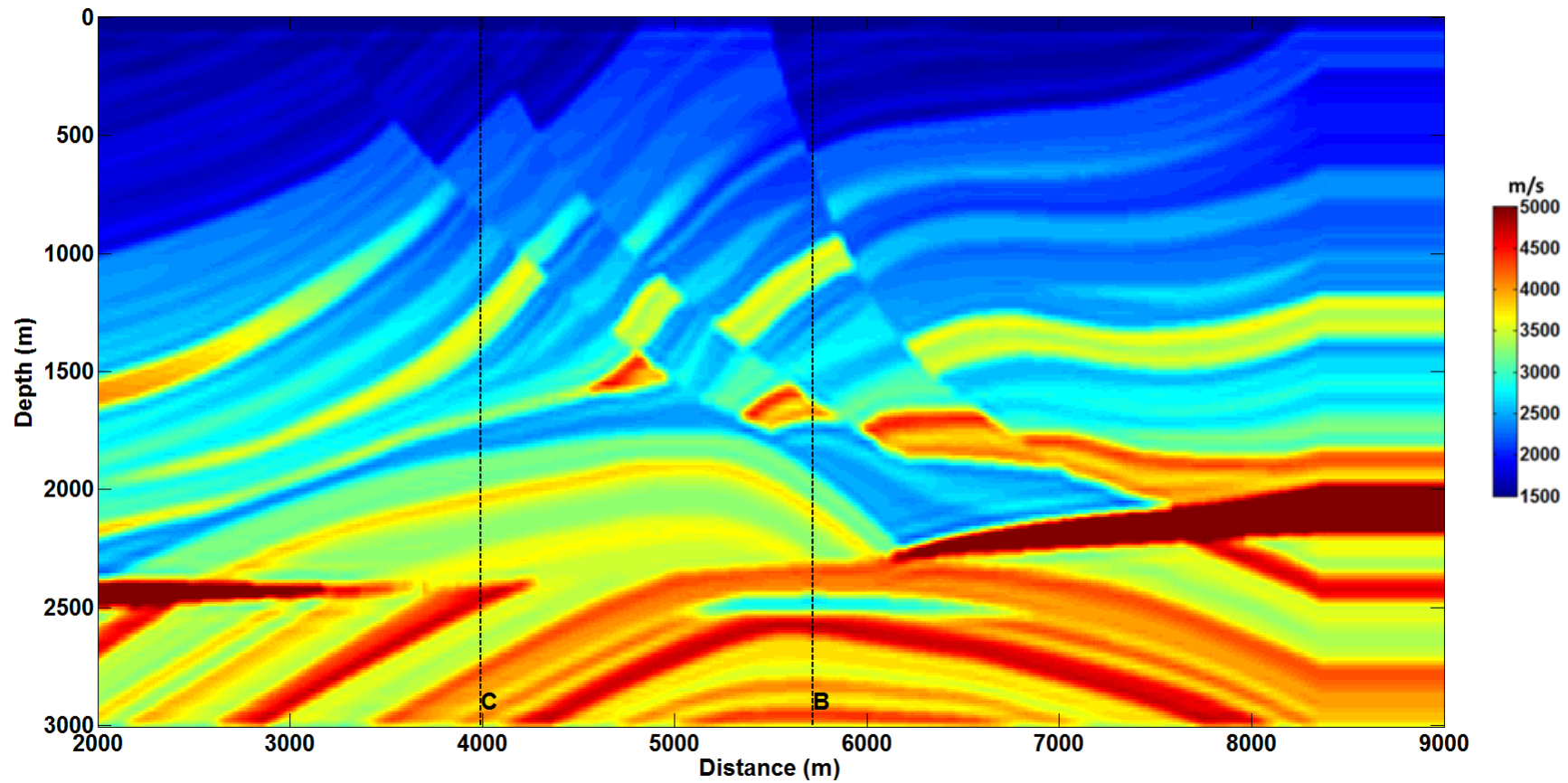
Spatial distribution of the error



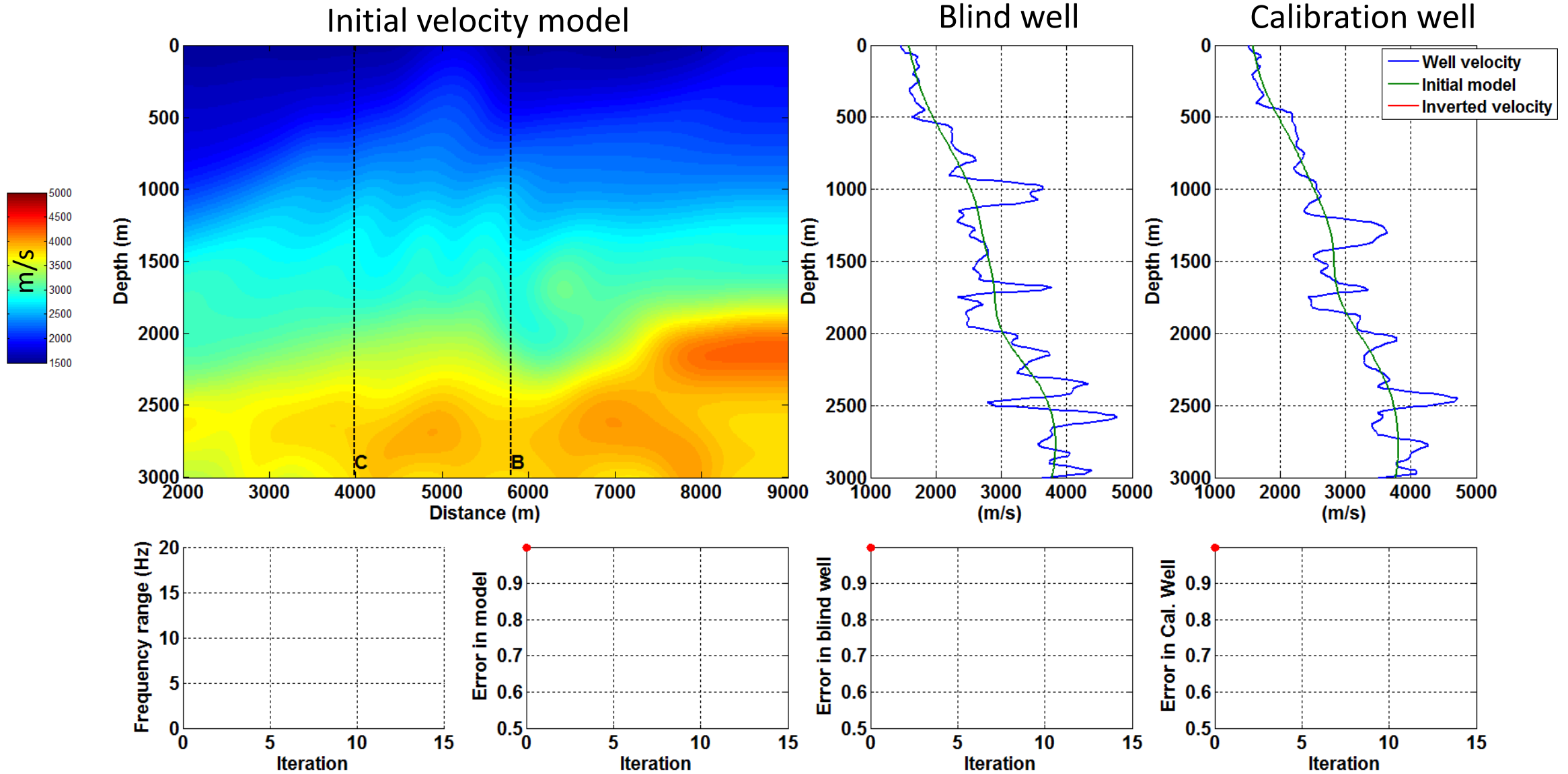
Inverted velocity model



Model 3

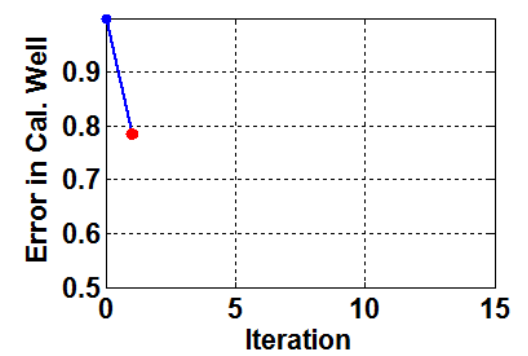
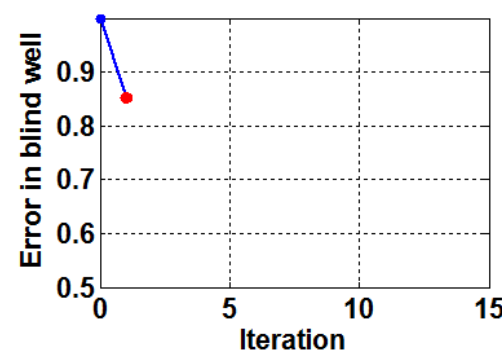
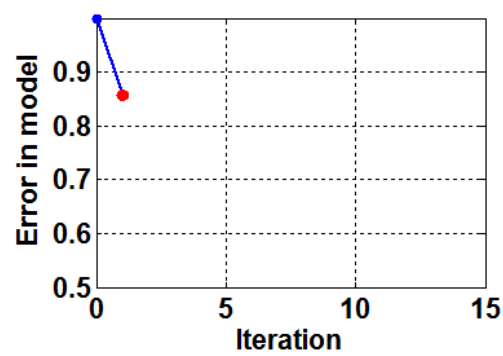
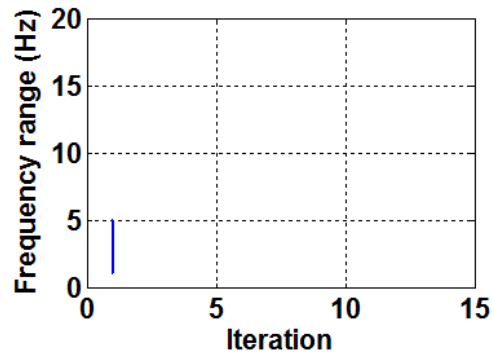
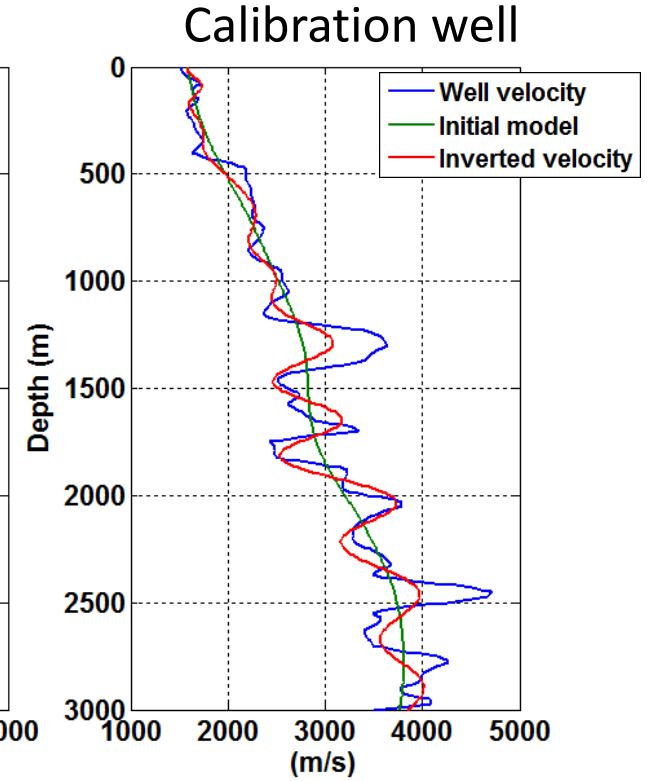
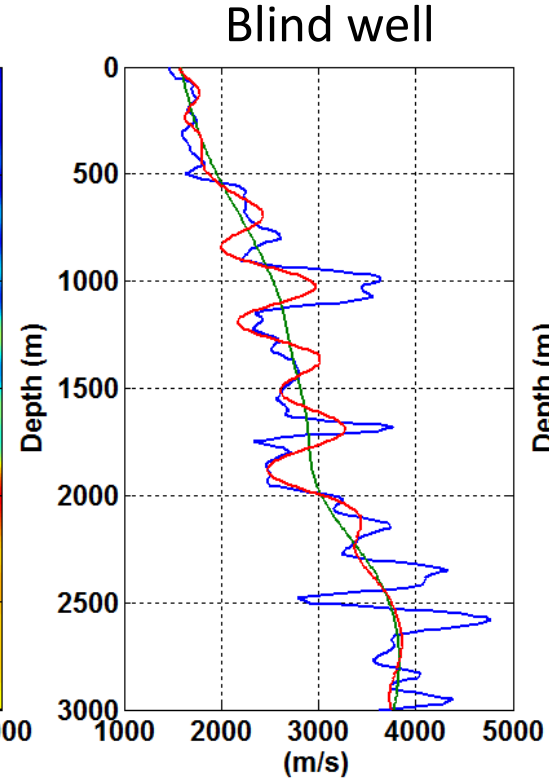
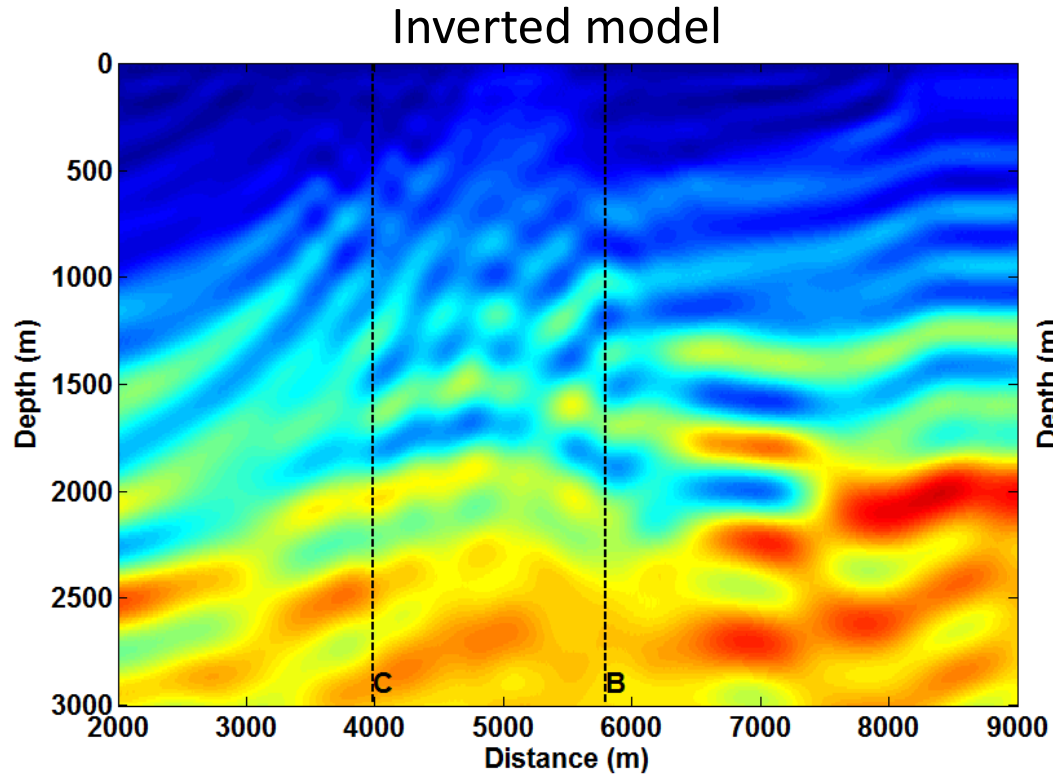
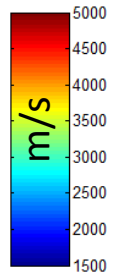


Evolution of the inverted model with more iterations



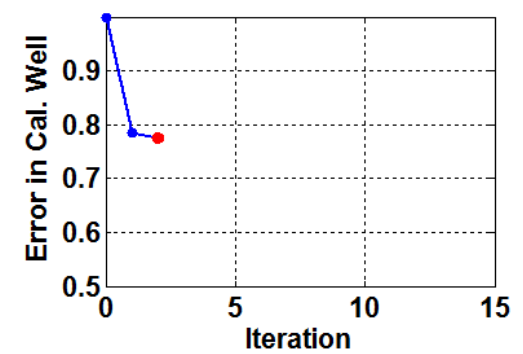
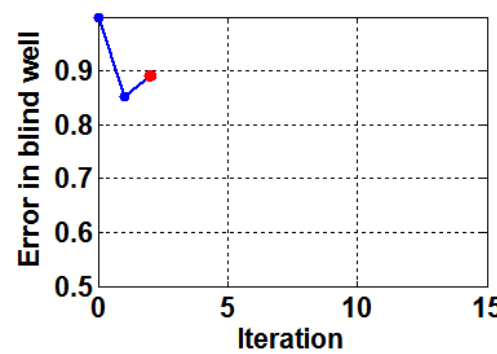
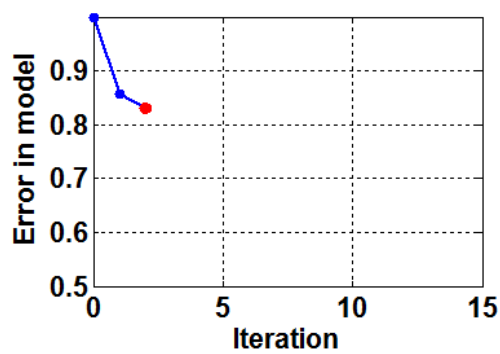
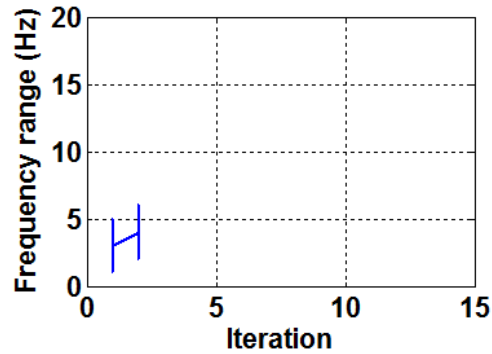
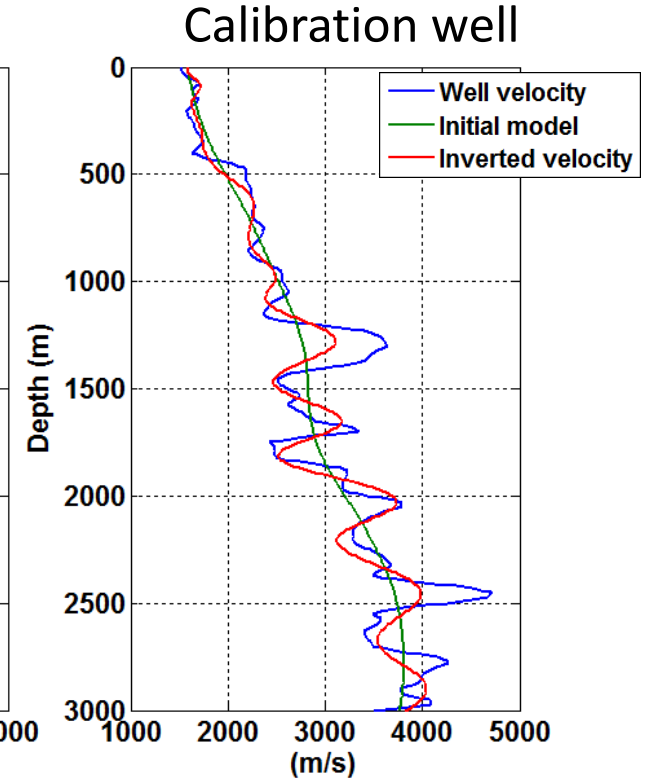
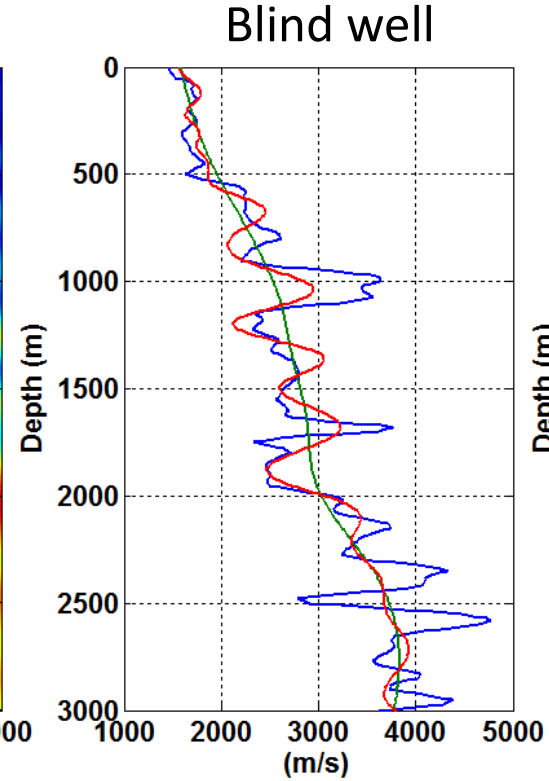
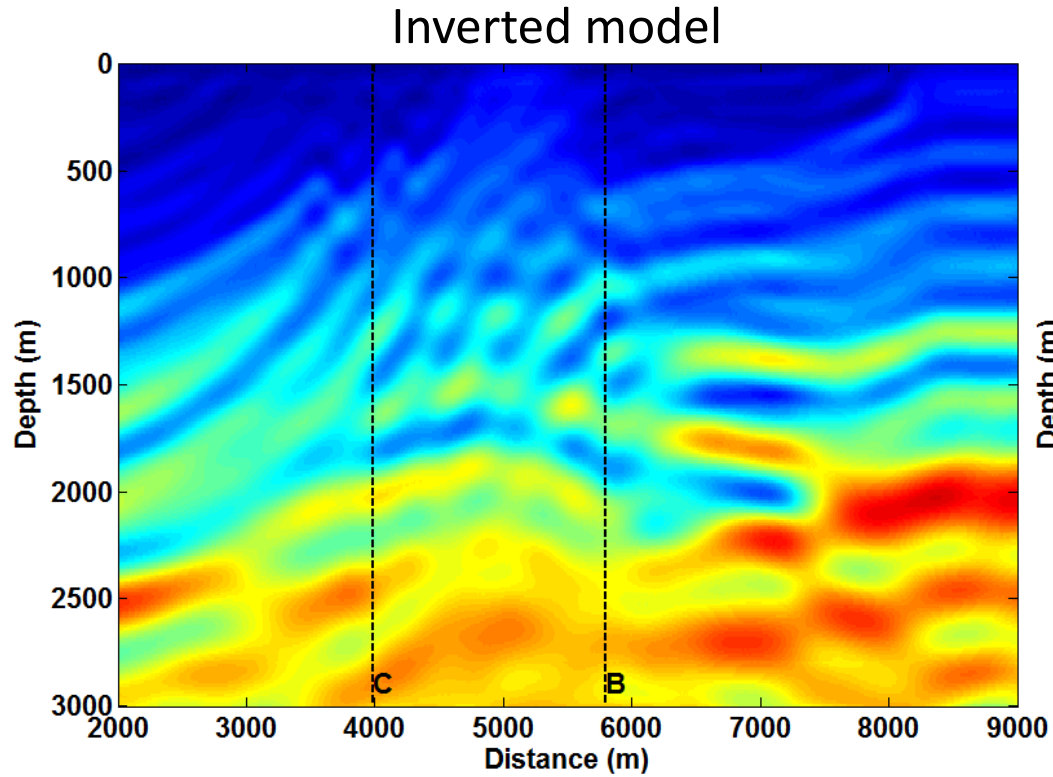
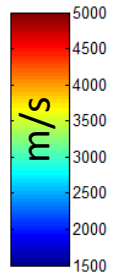
Evolution of the inverted model with more iterations

Iteration
1



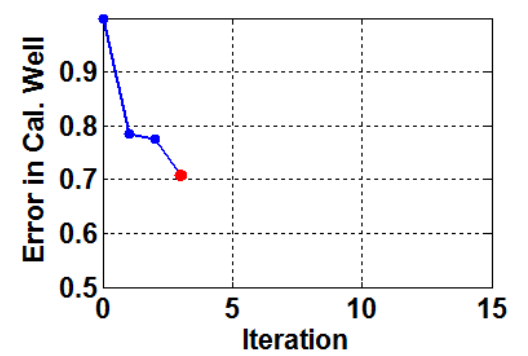
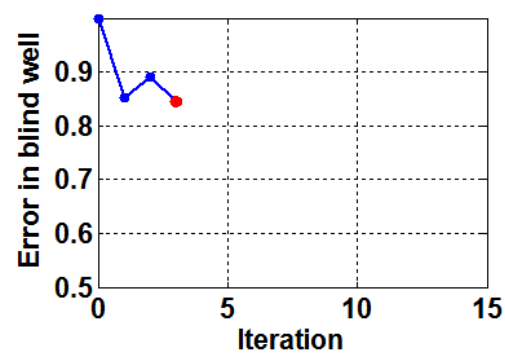
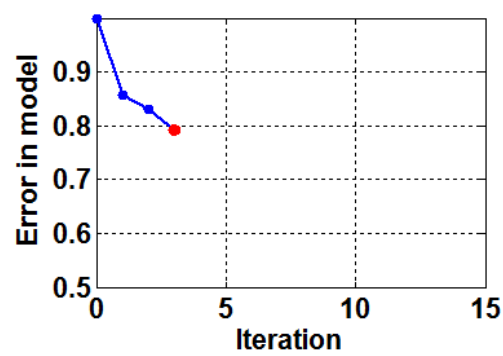
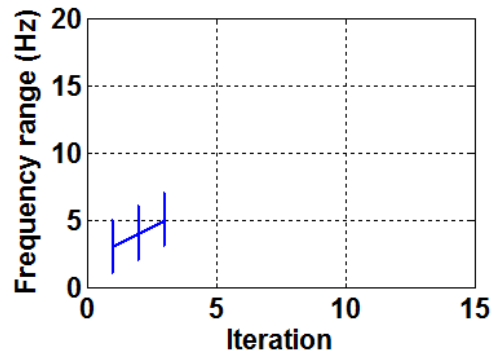
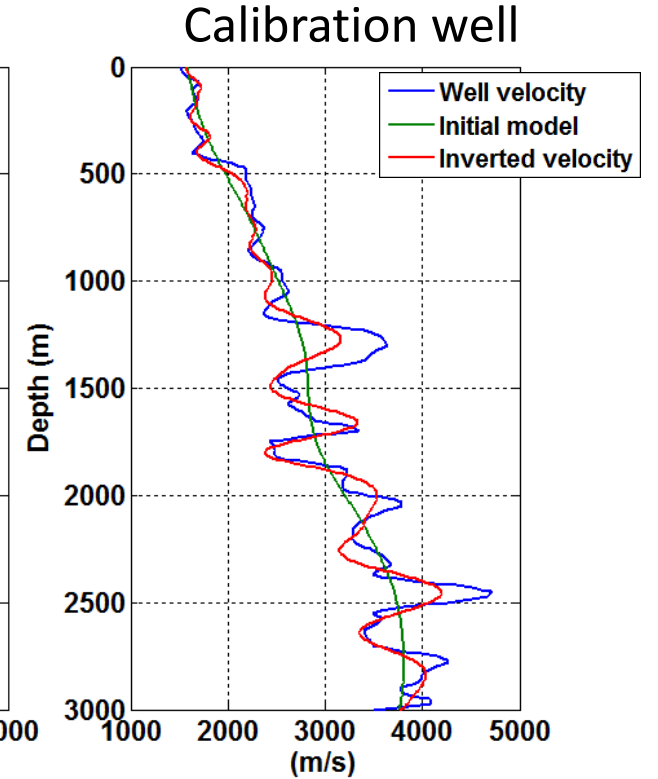
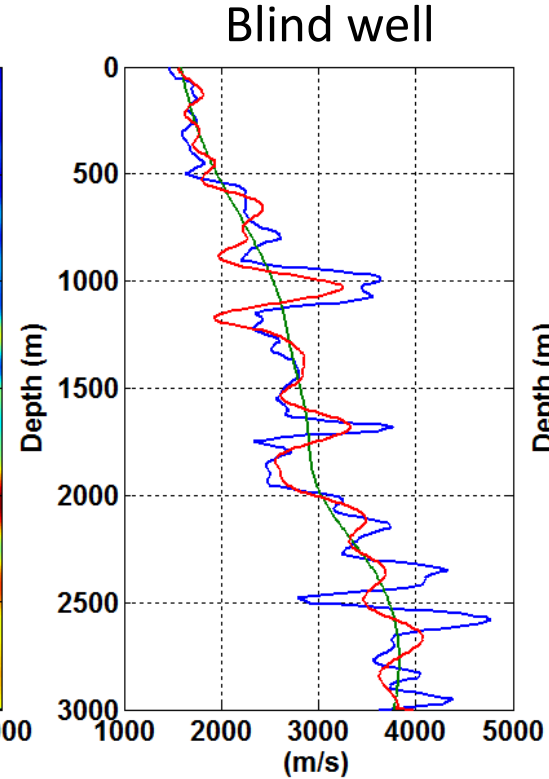
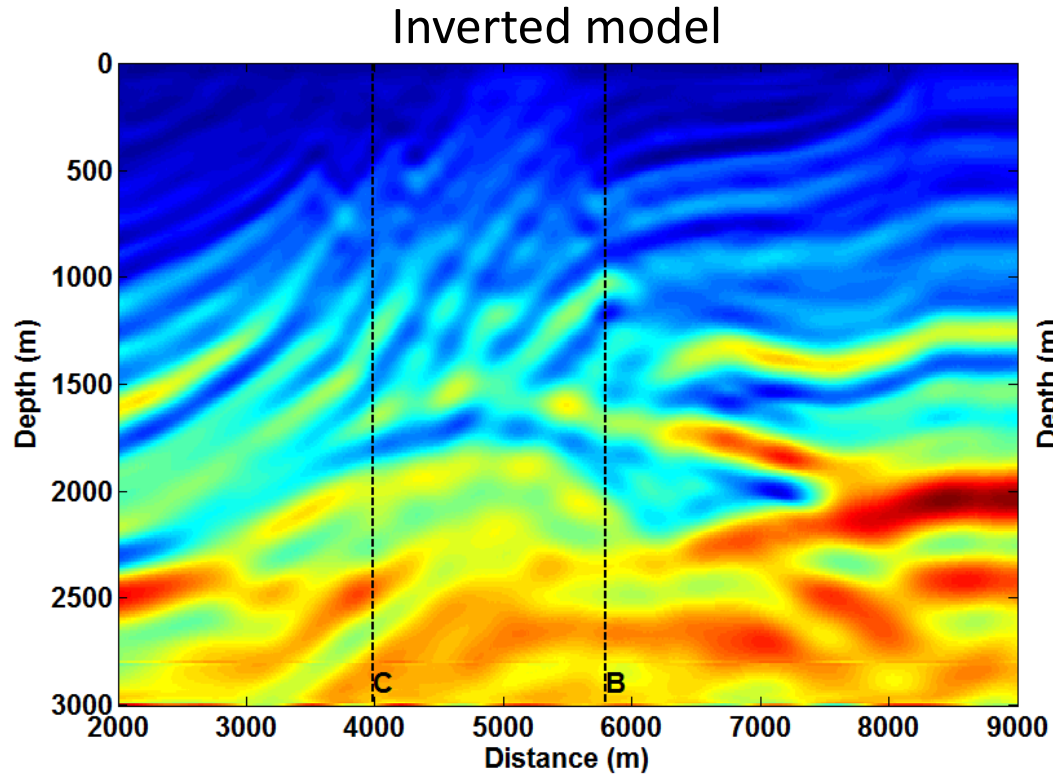
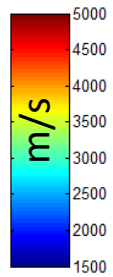
Evolution of the inverted model with more iterations

Iteration
2



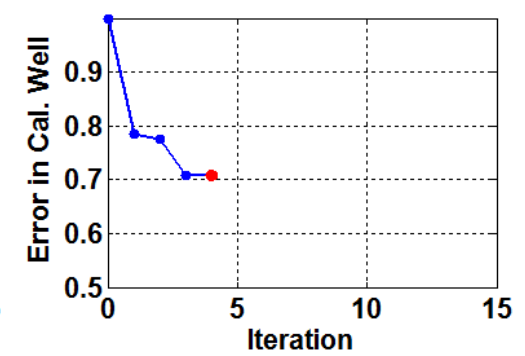
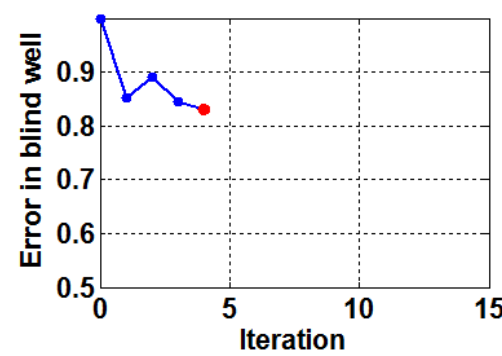
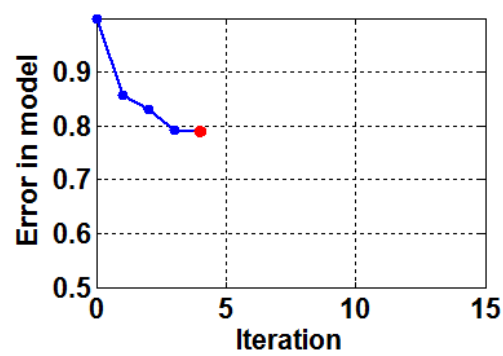
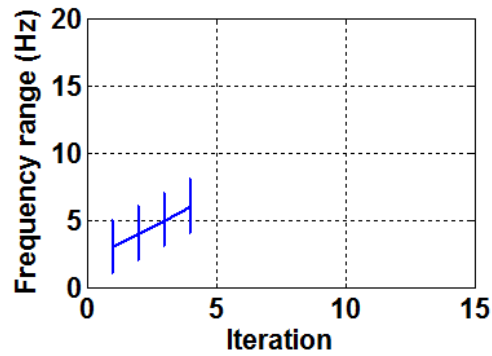
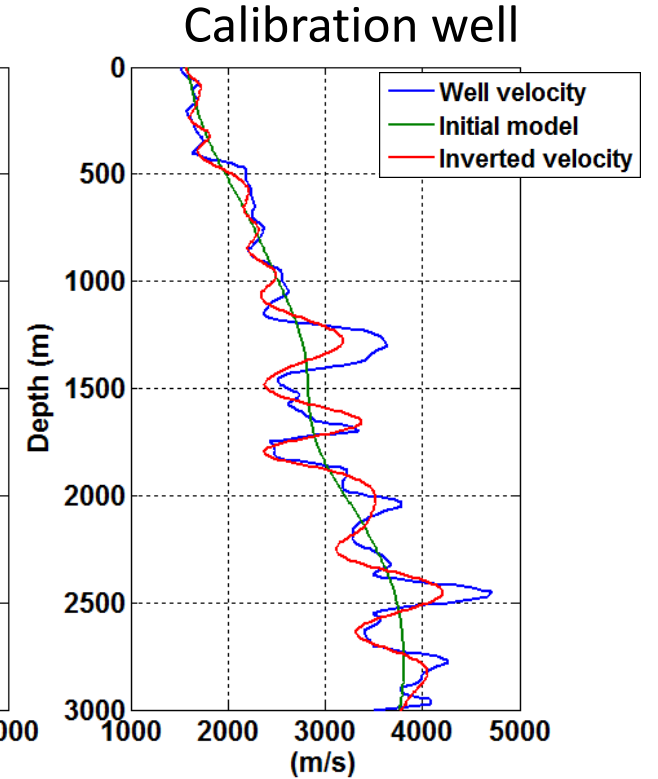
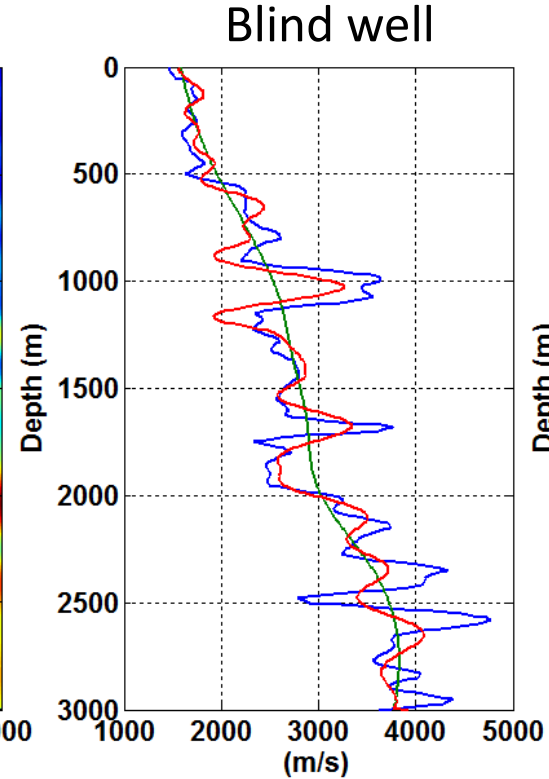
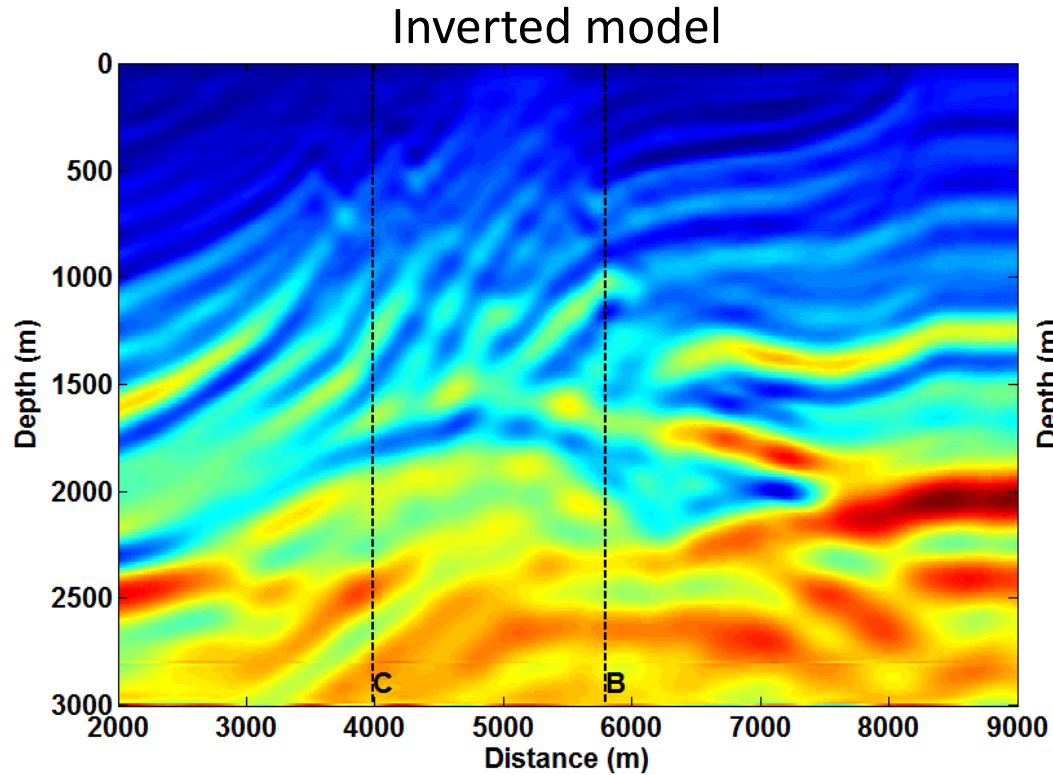
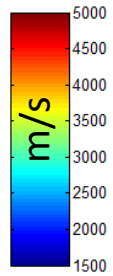
Evolution of the inverted model with more iterations

Iteration
3



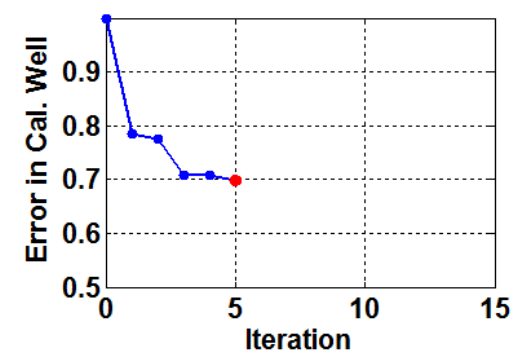
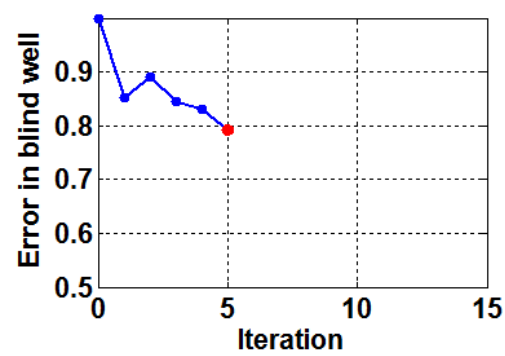
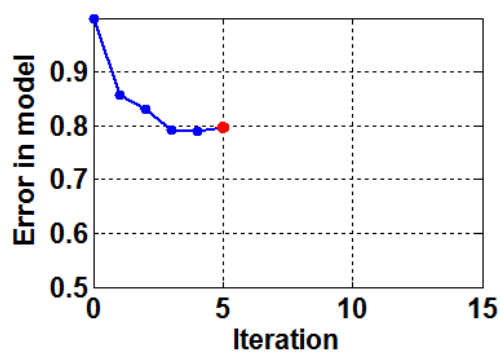
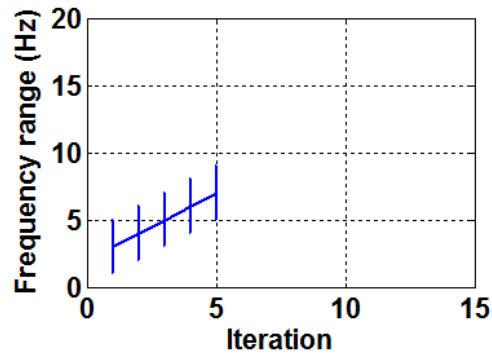
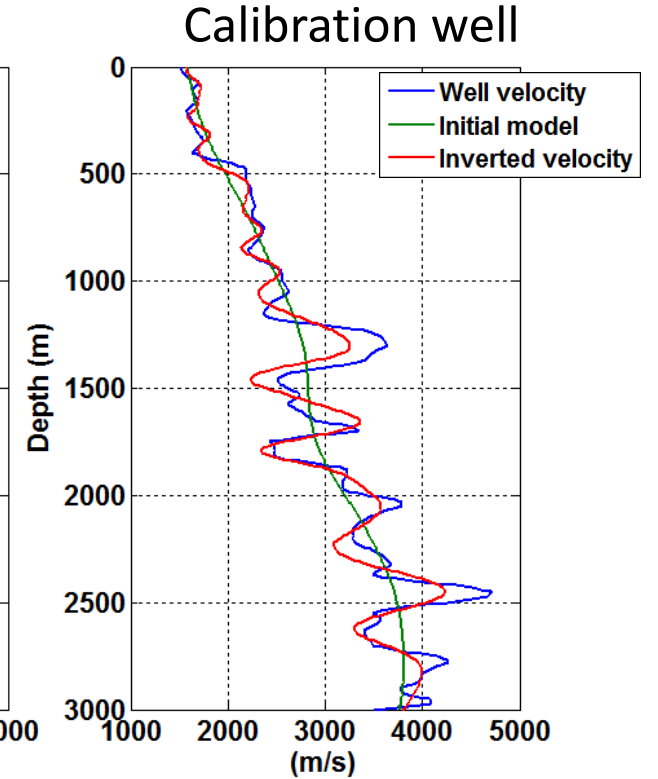
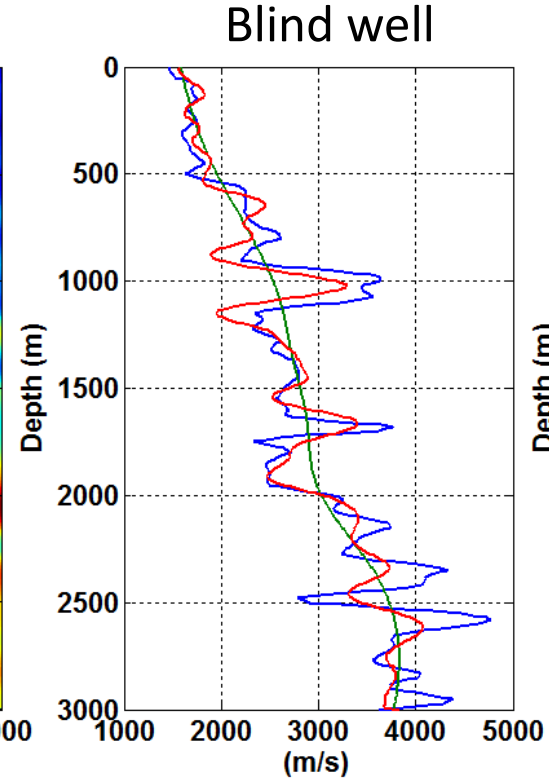
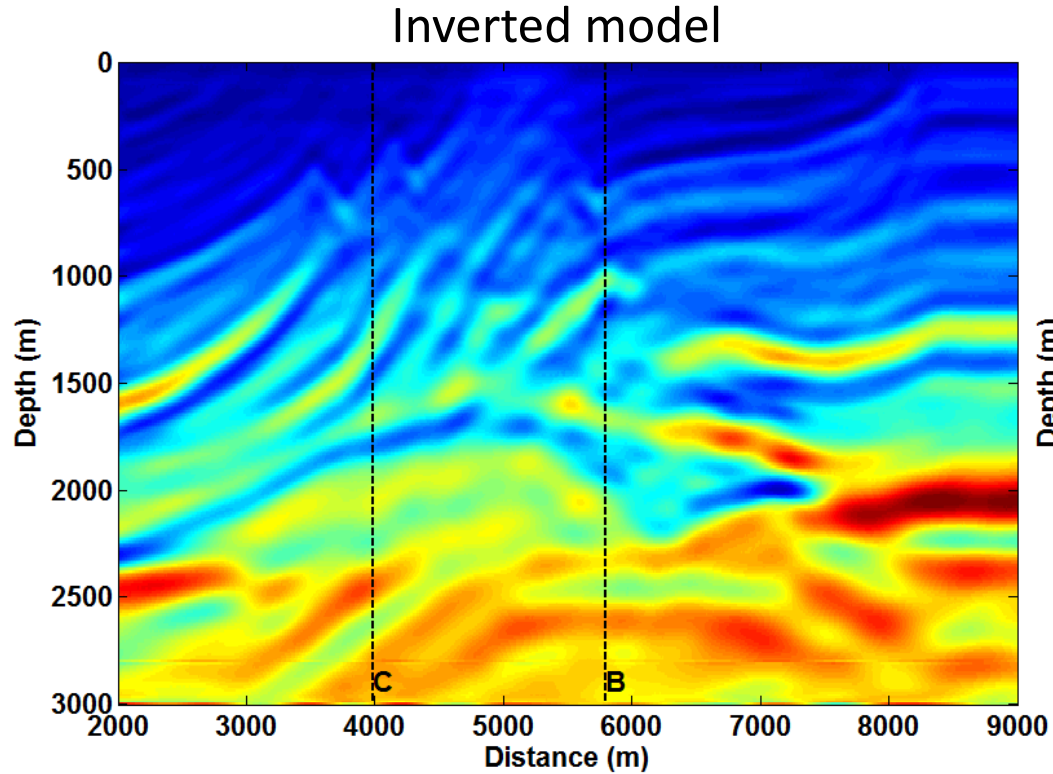
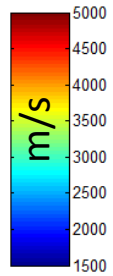
Evolution of the inverted model with more iterations

Iteration
4



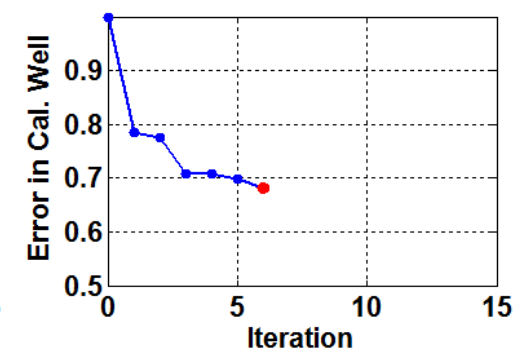
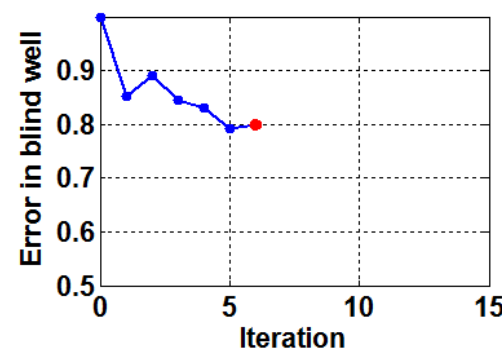
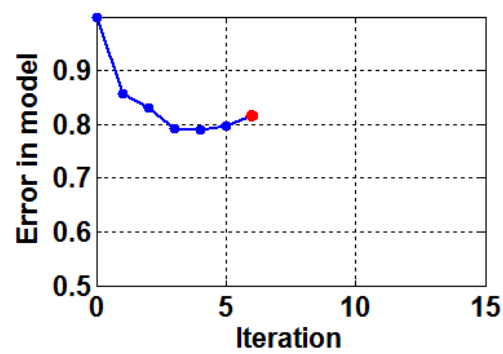
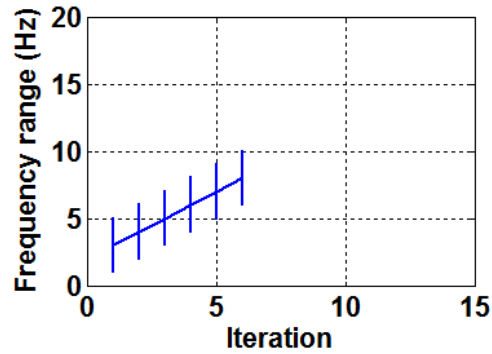
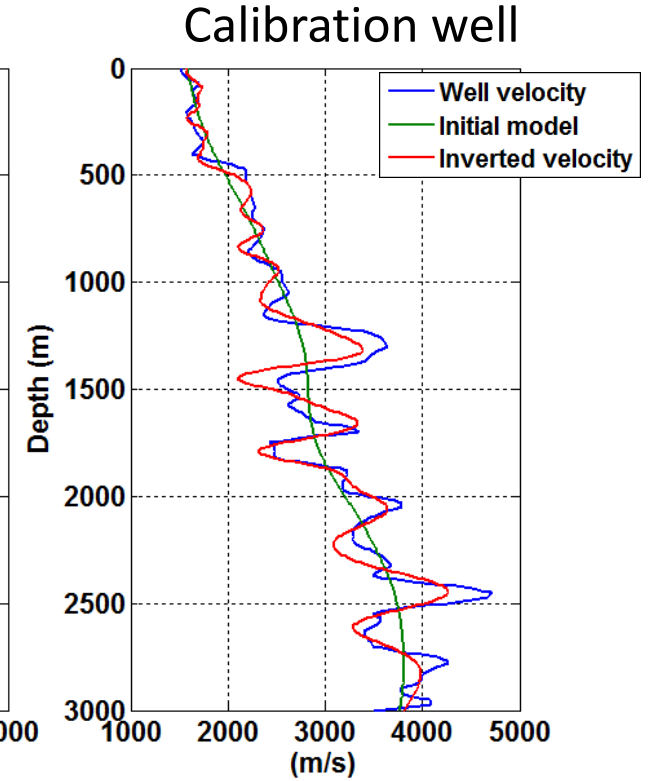
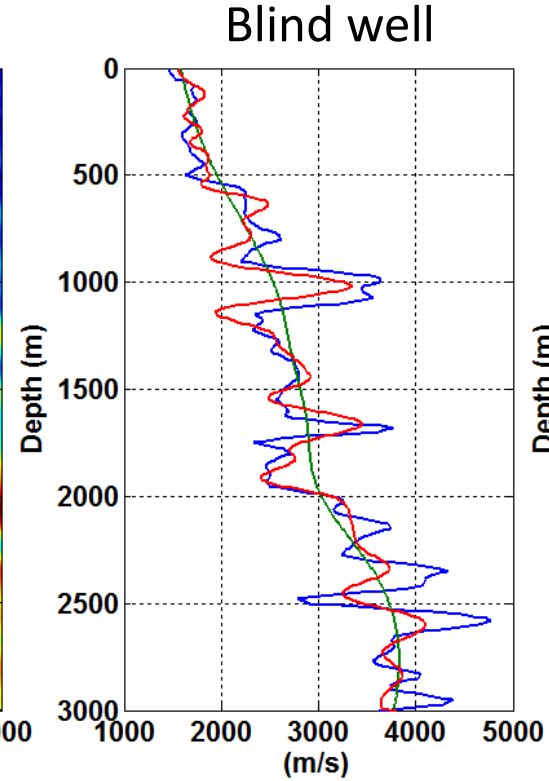
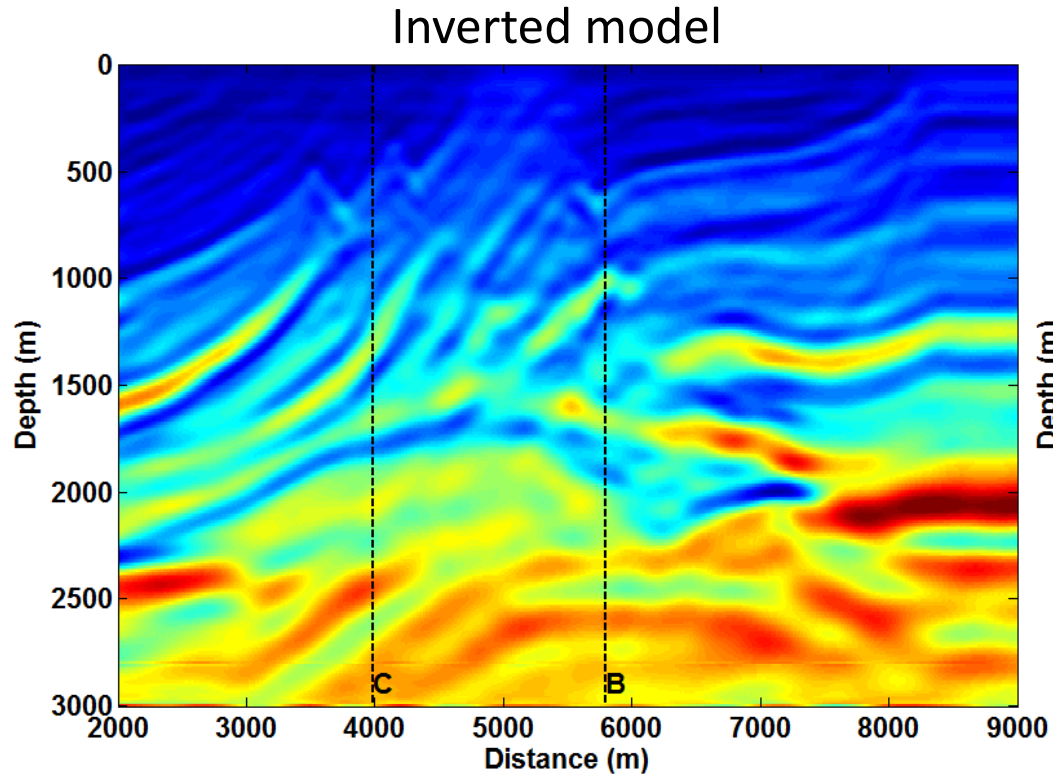
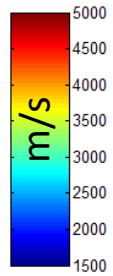
Evolution of the inverted model with more iterations

Iteration
5



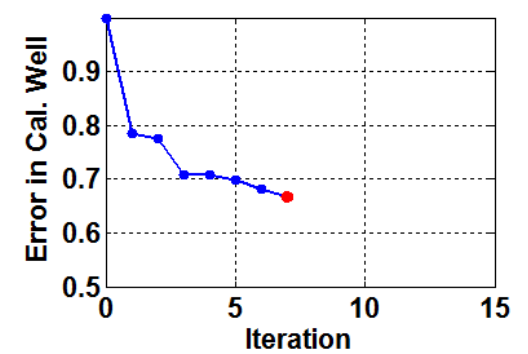
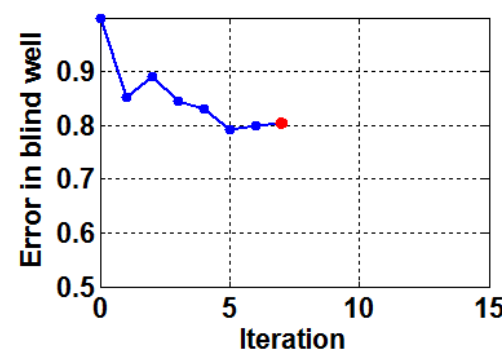
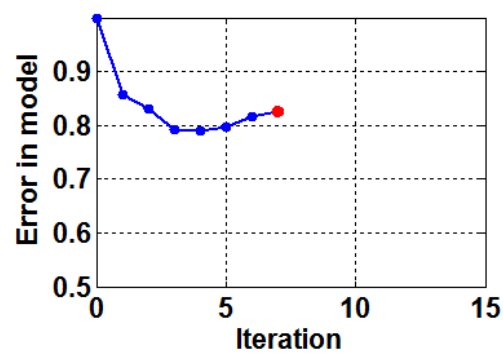
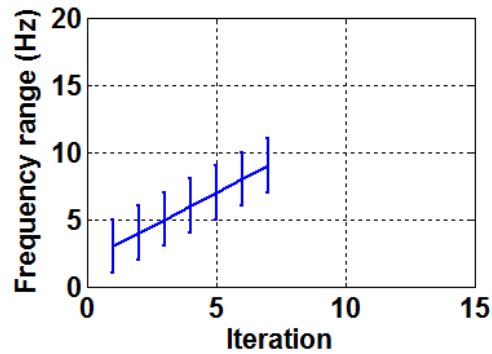
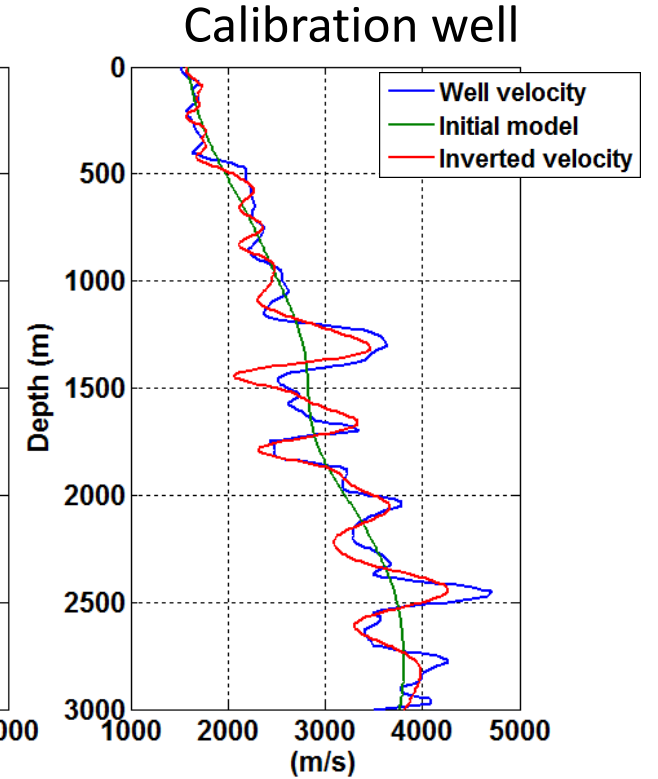
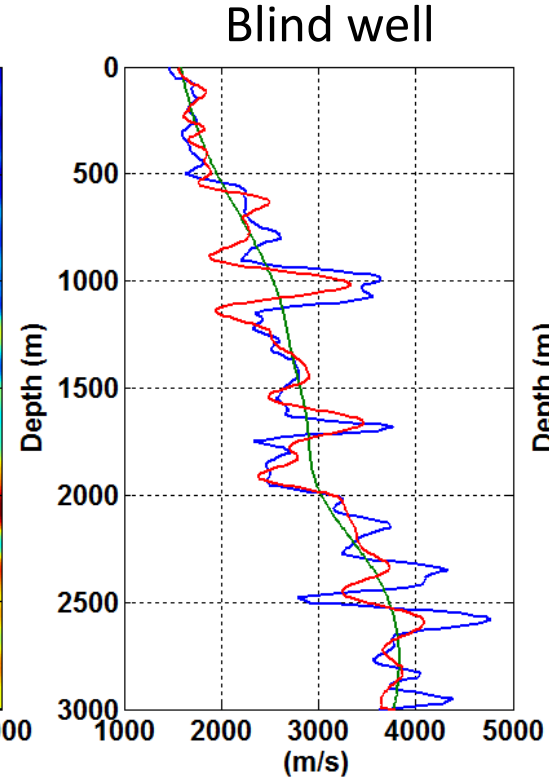
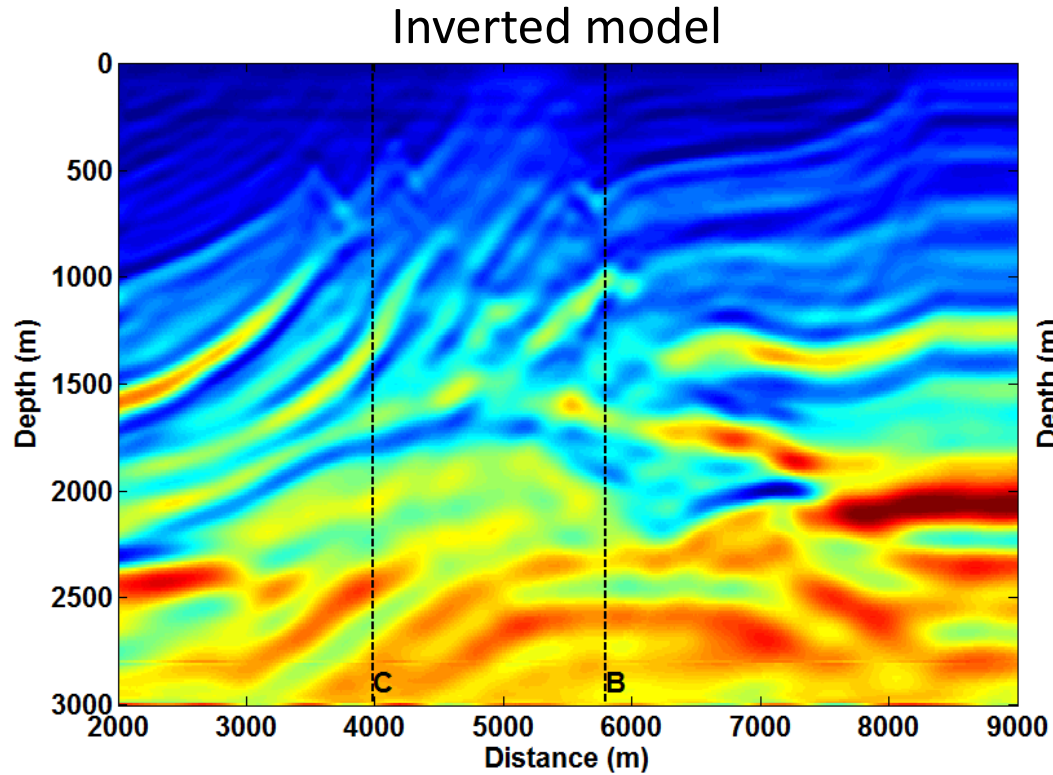
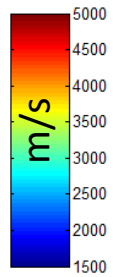
Evolution of the inverted model with more iterations

Iteration
6



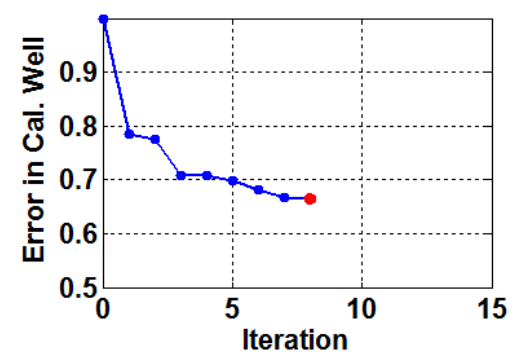
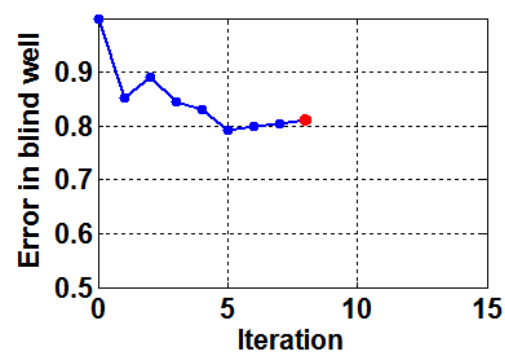
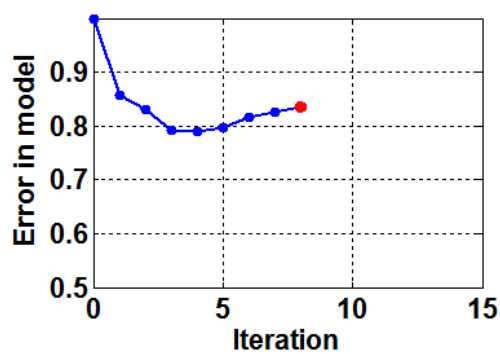
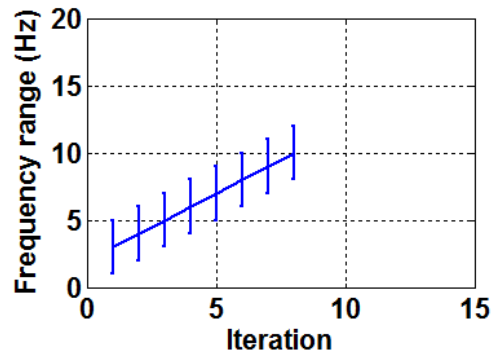
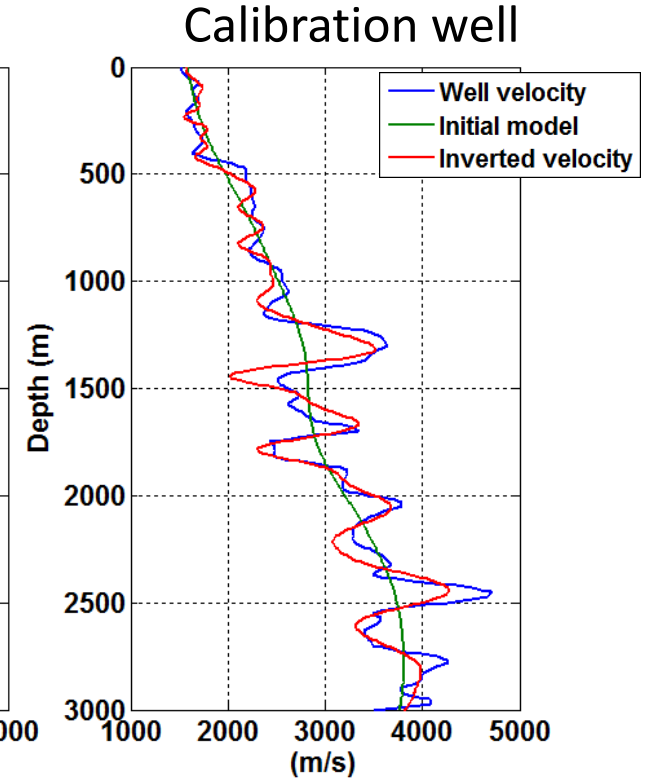
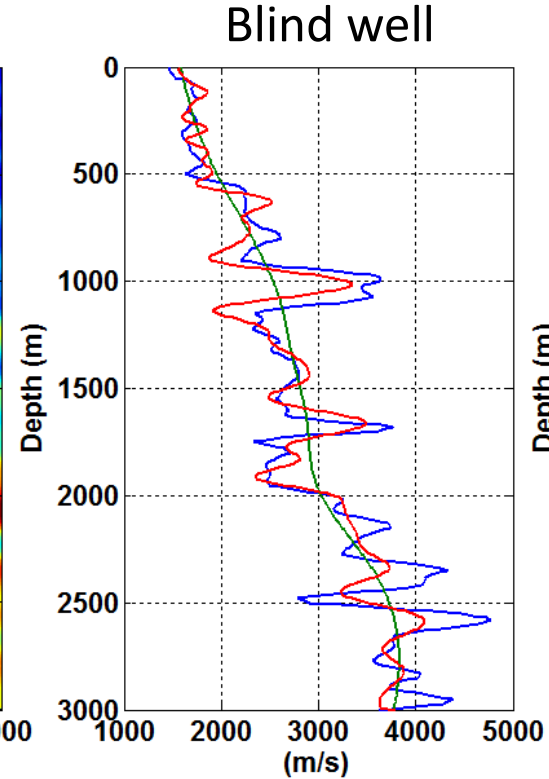
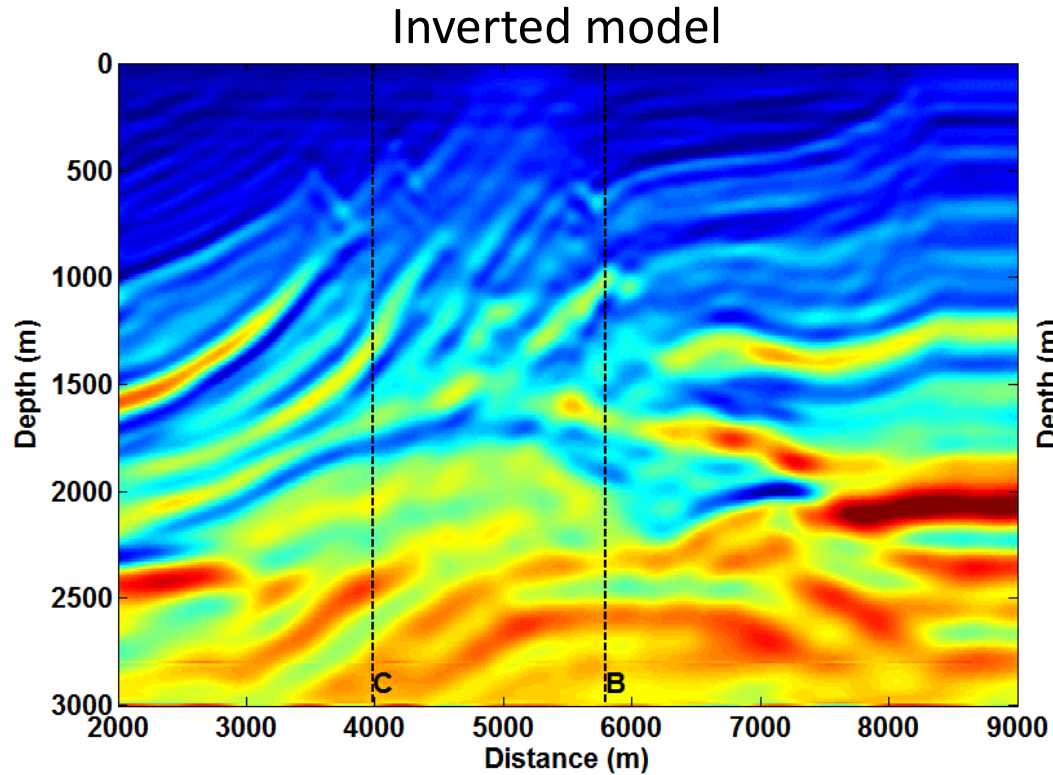
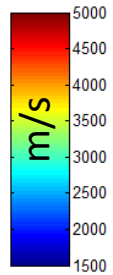
Evolution of the inverted model with more iterations

Iteration
7



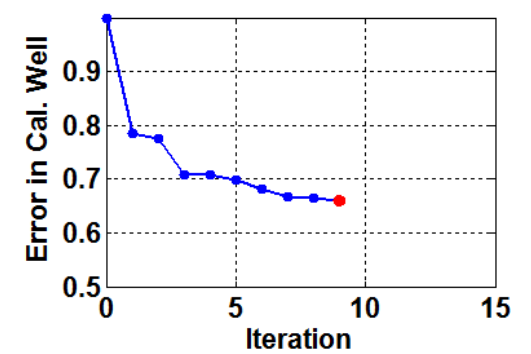
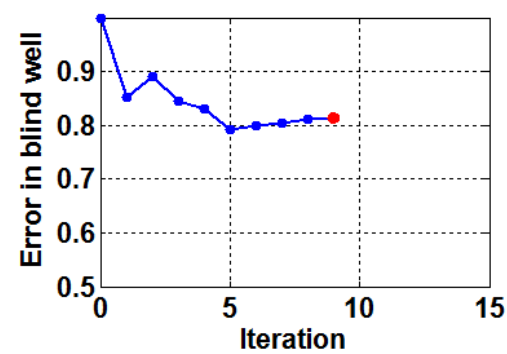
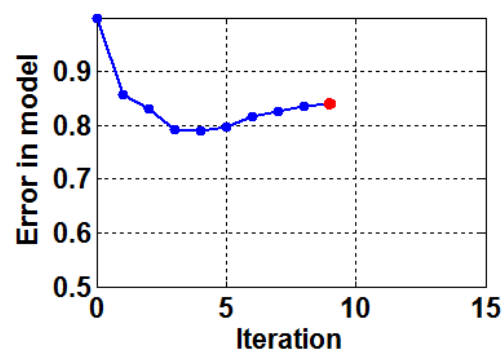
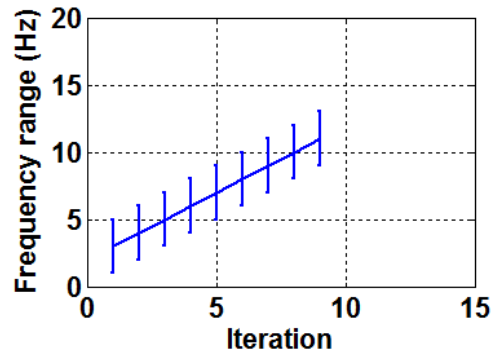
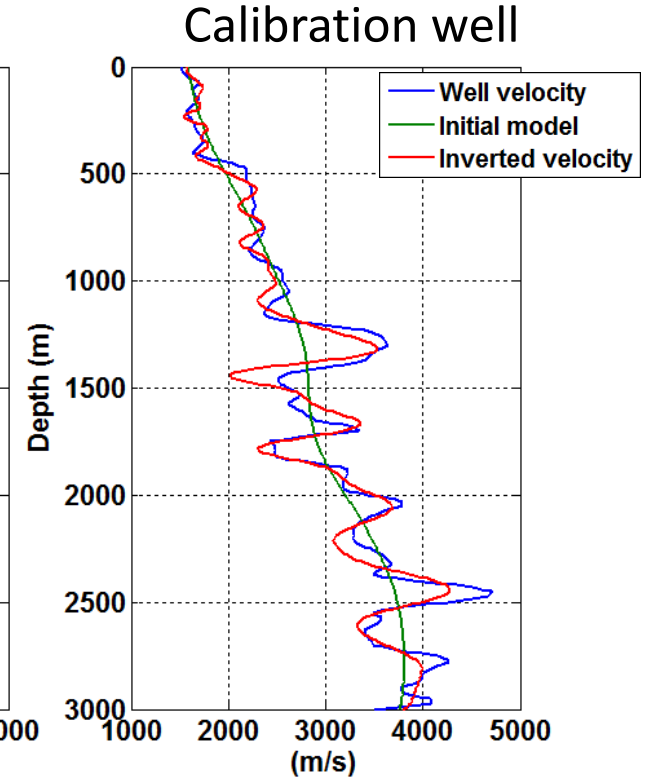
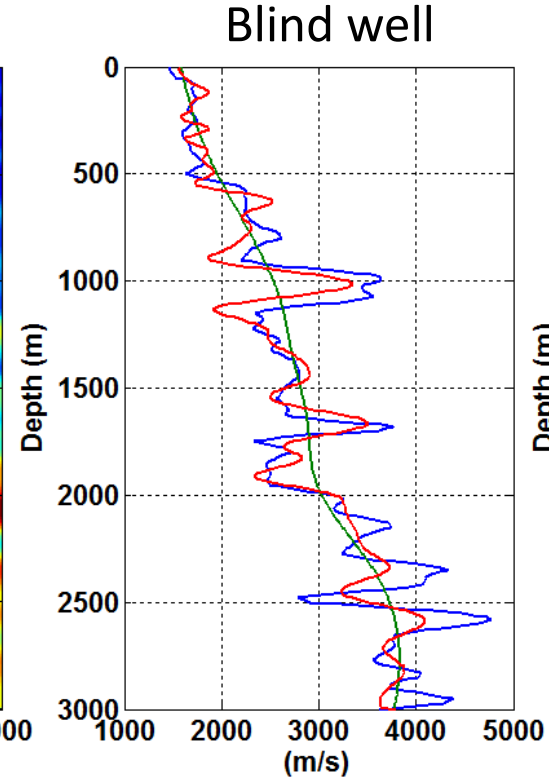
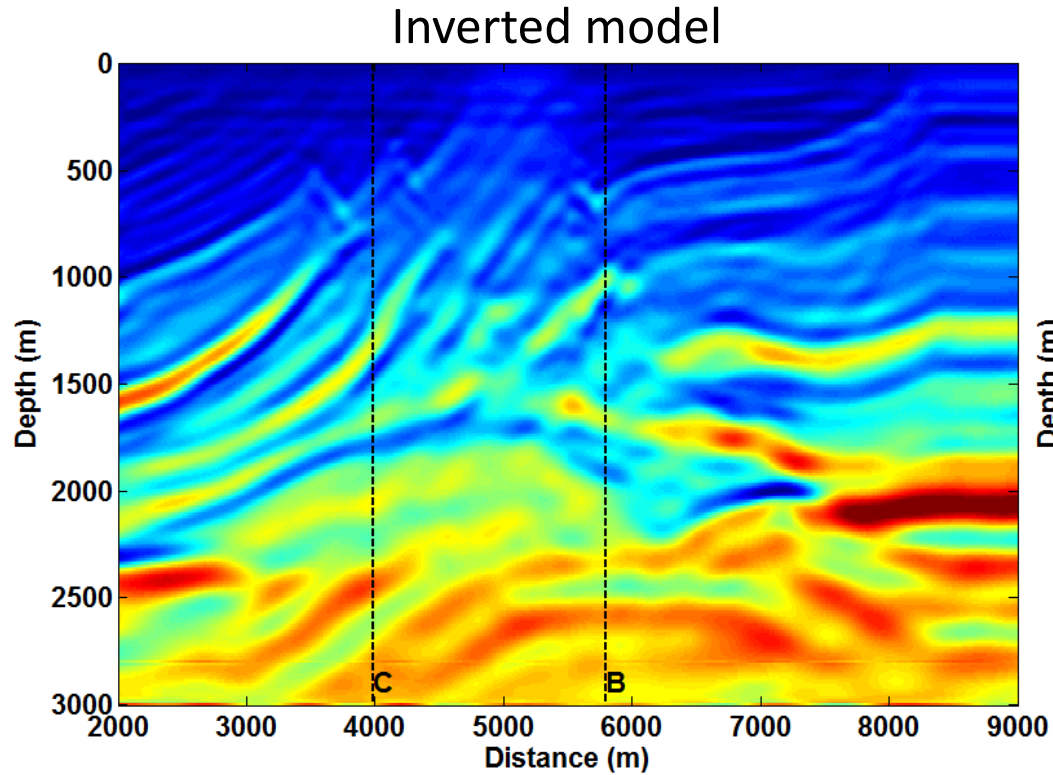
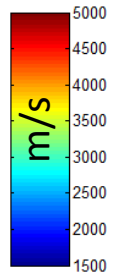
Evolution of the inverted model with more iterations

Iteration
8



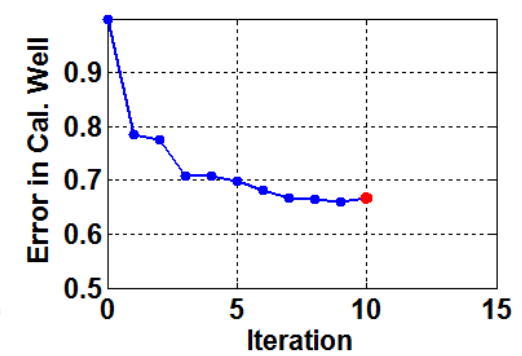
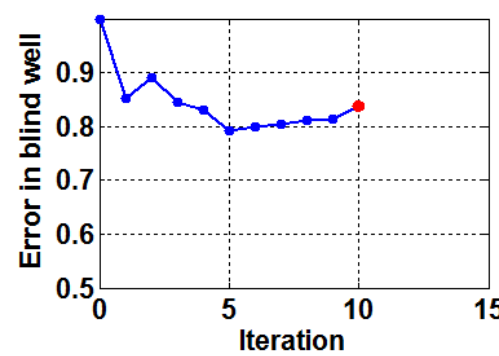
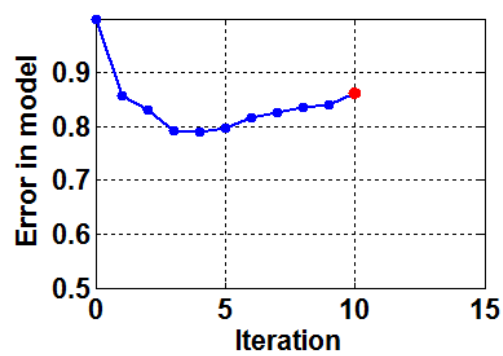
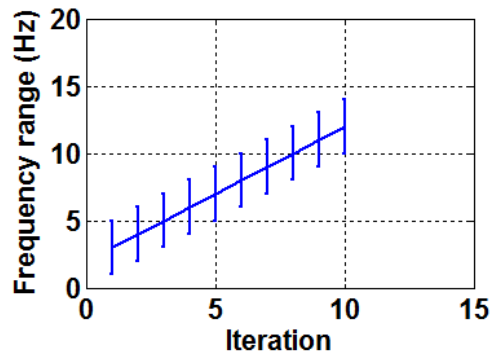
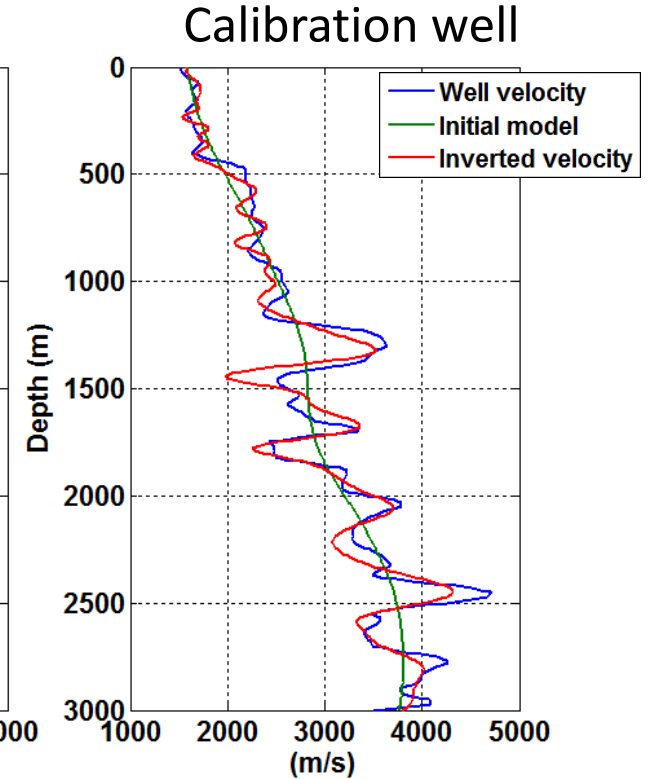
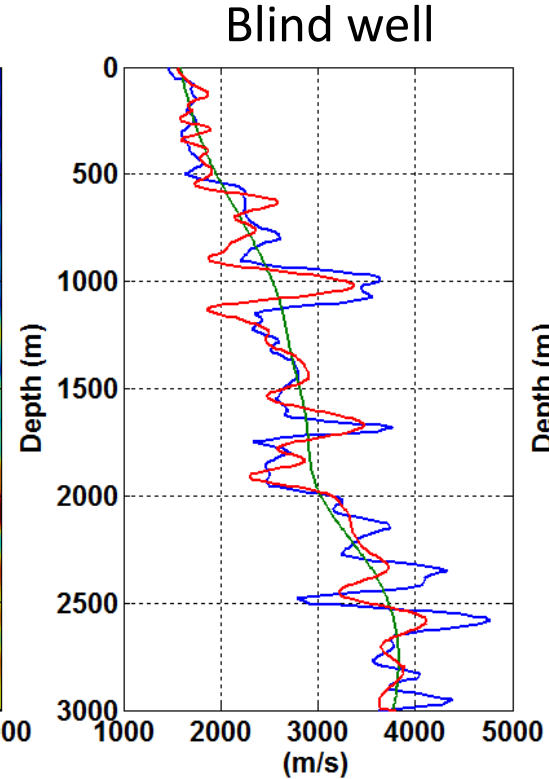
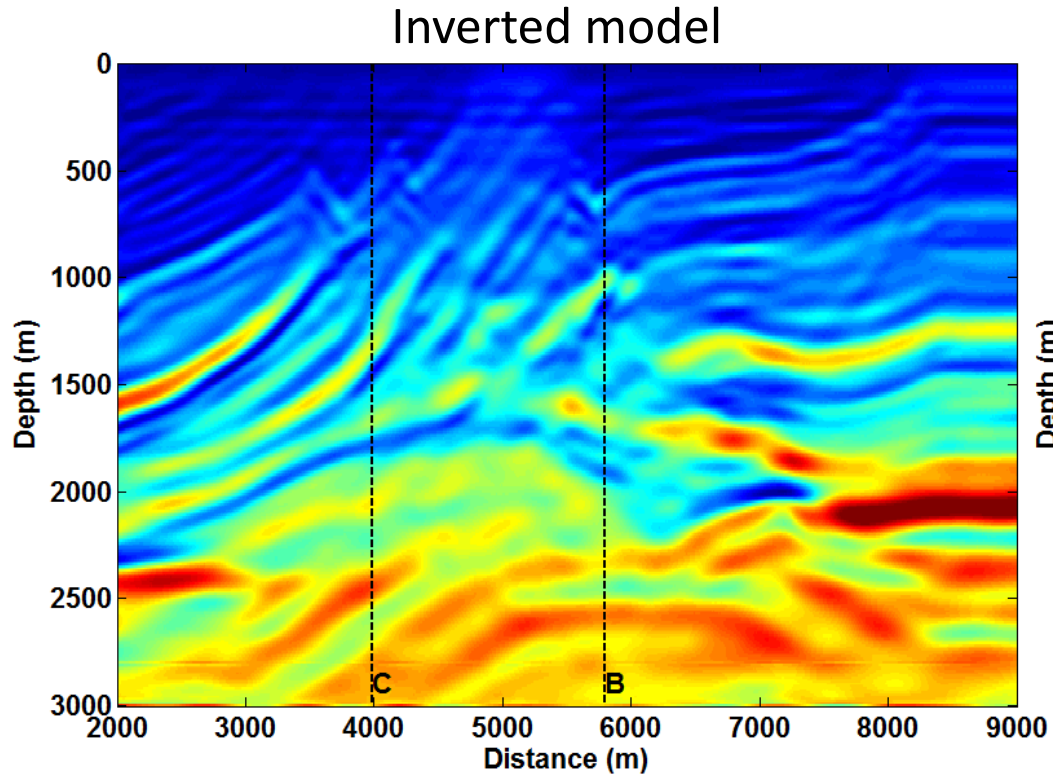
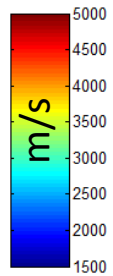
Evolution of the inverted model with more iterations

Iteration
9



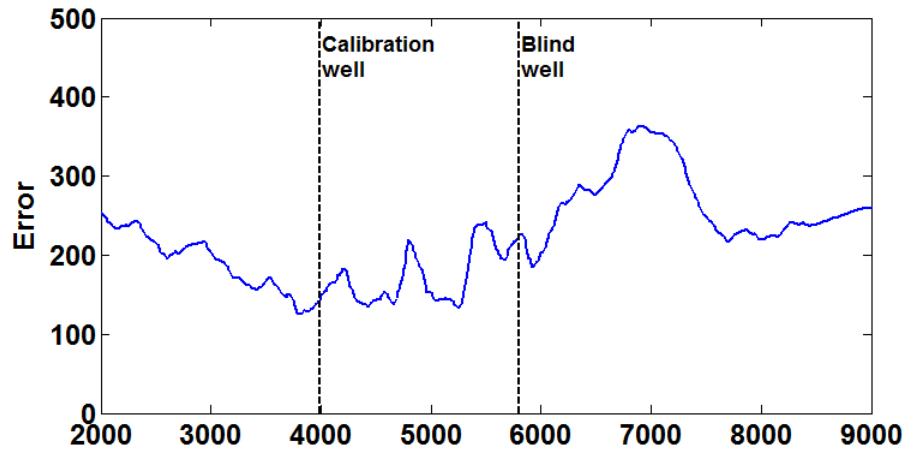
Evolution of the inverted model with more iterations

Iteration
10

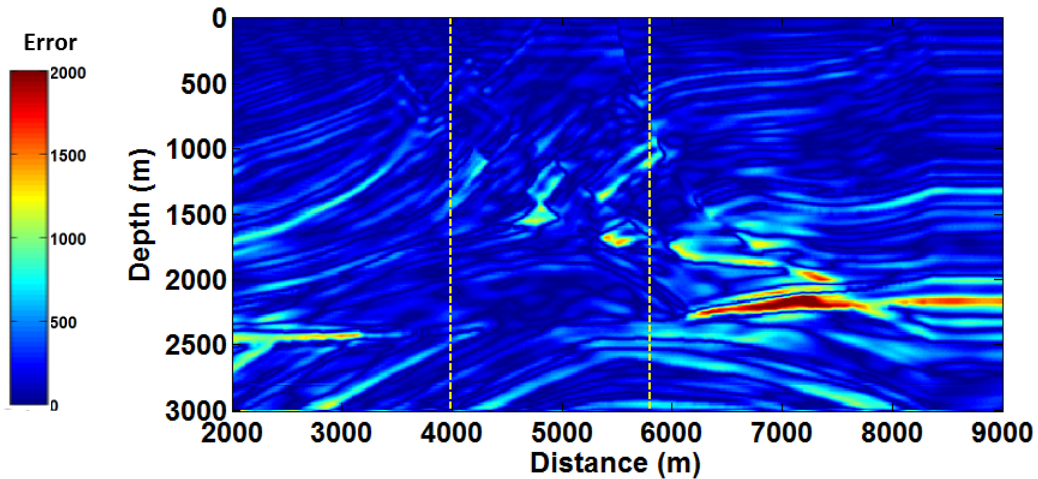


Spatial distribution of the error

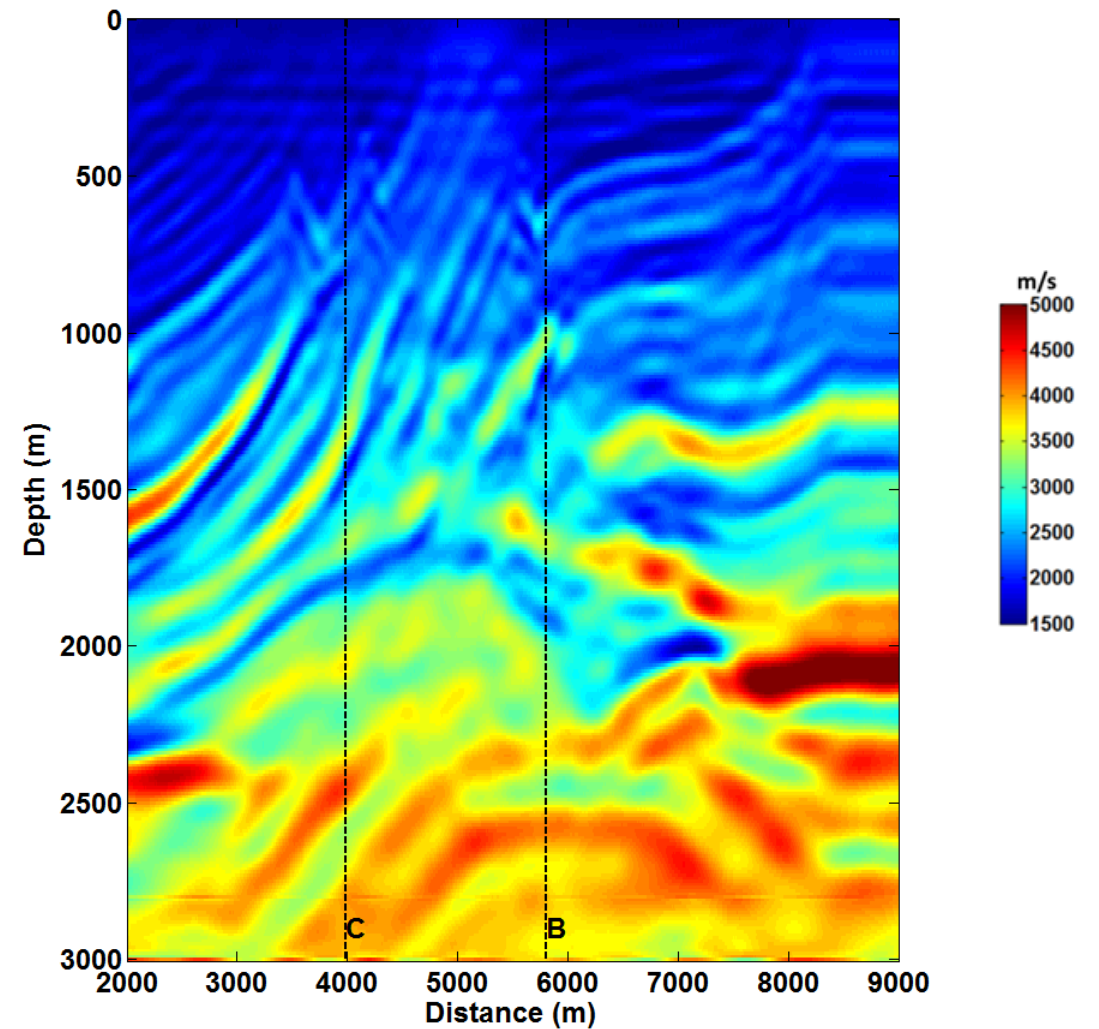
Horizontal distribution of the error

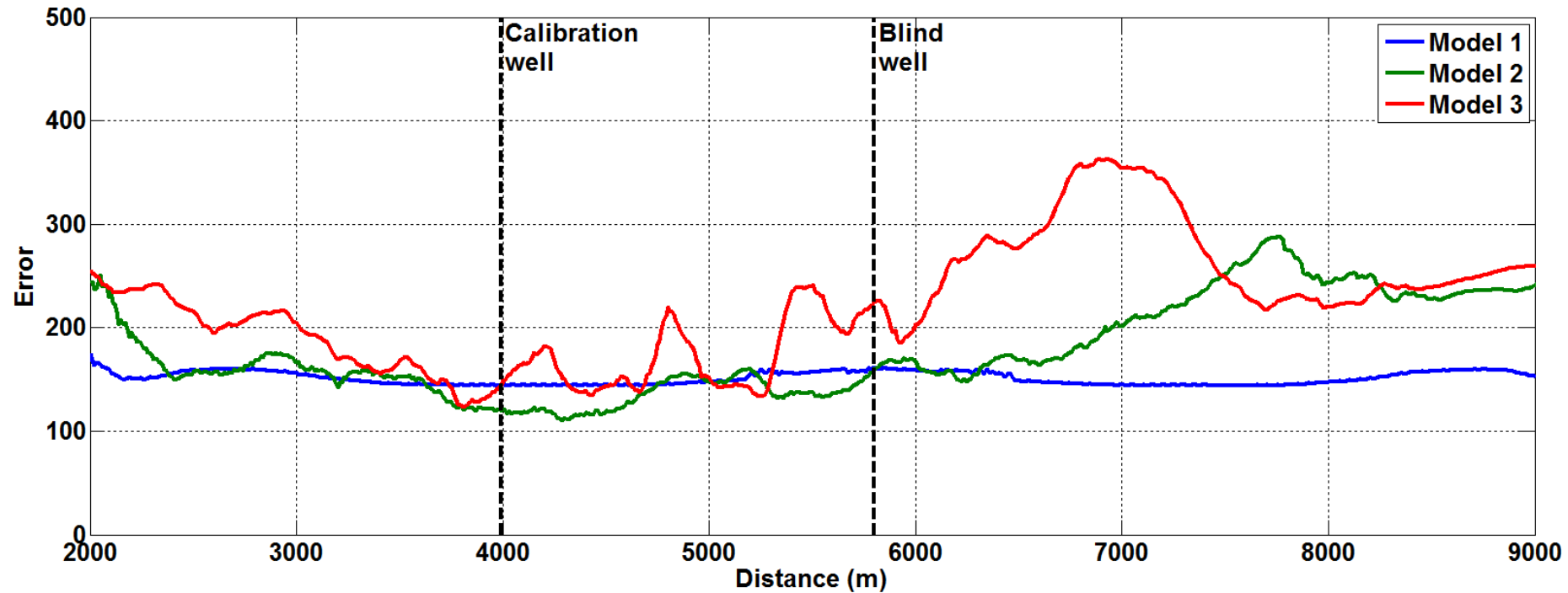


Spatial distribution of the error



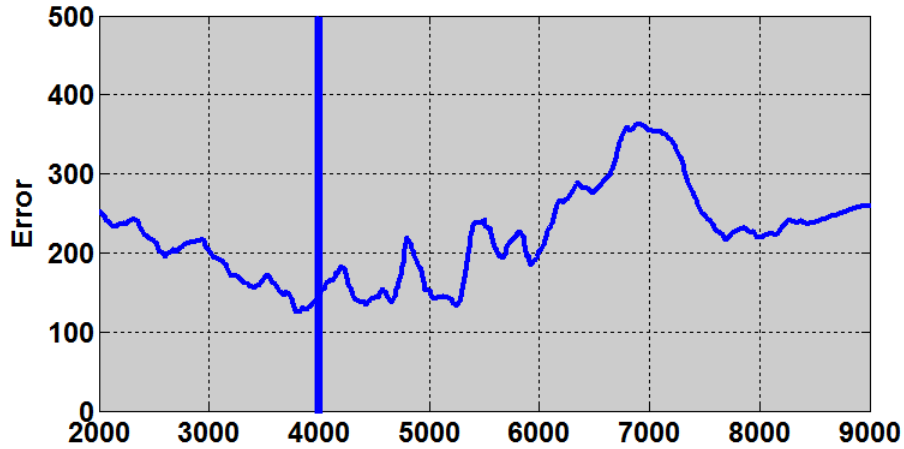
Inverted velocity model



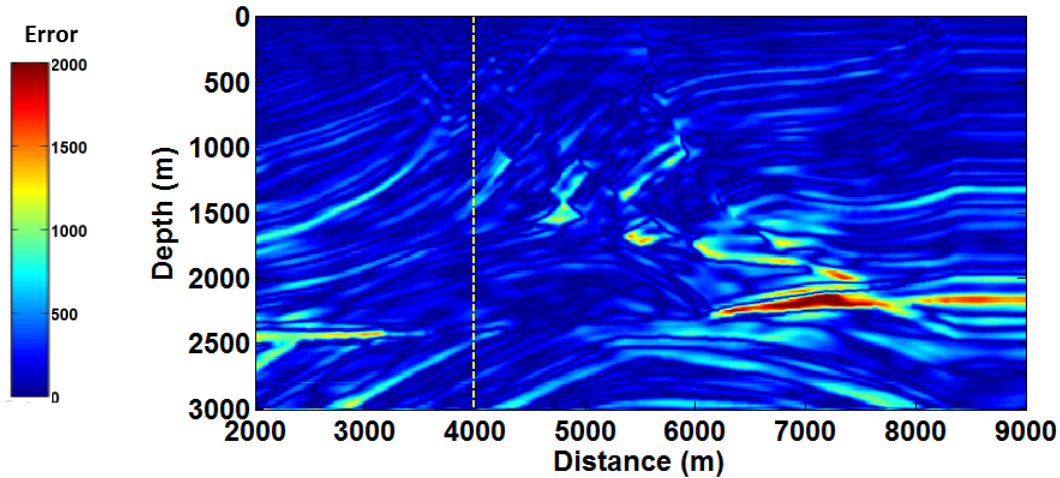


- We found a consistently low error in the well location even for the most complex model.
- Well calibration satisfactorily performs in the presence of moderate lateral velocity changes (Model 1 and 2).
- The error increases in the presence of high velocity contrasts.

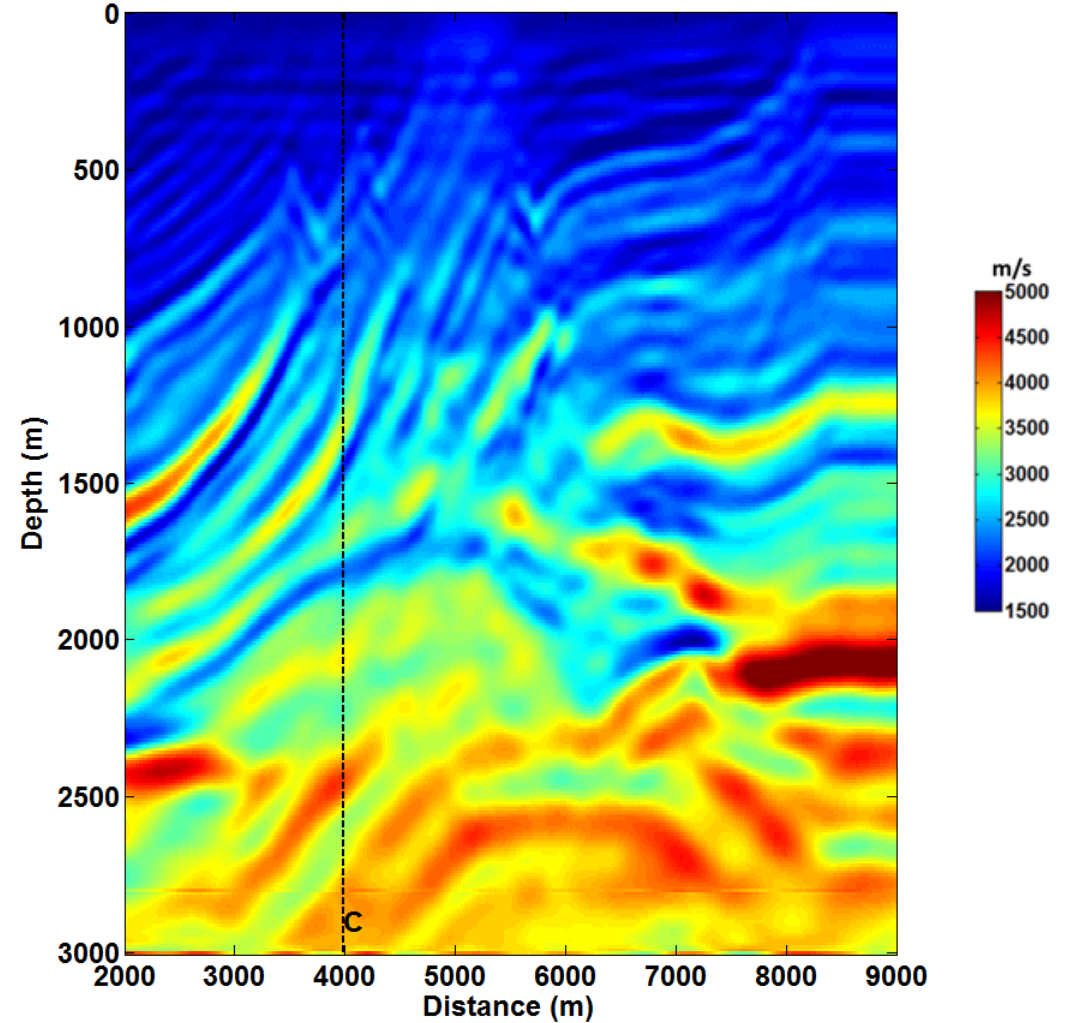
Horizontal distribution of the error



Spatial distribution of the error



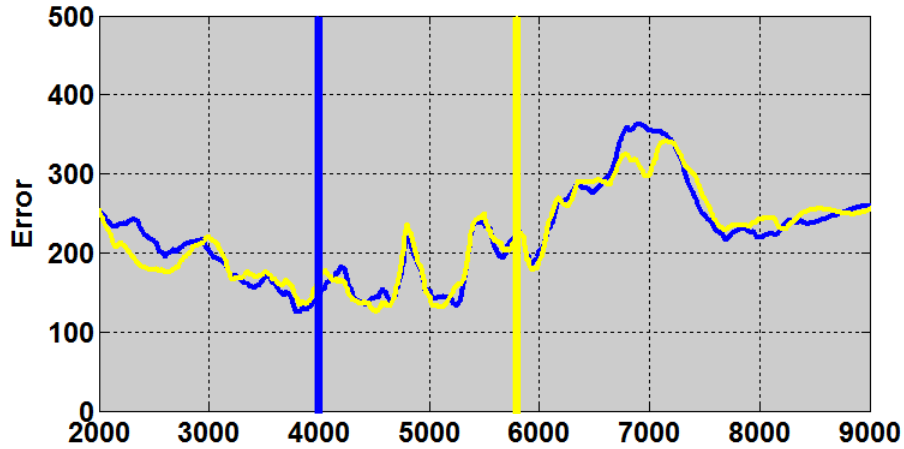
Calibration well at 4000 m



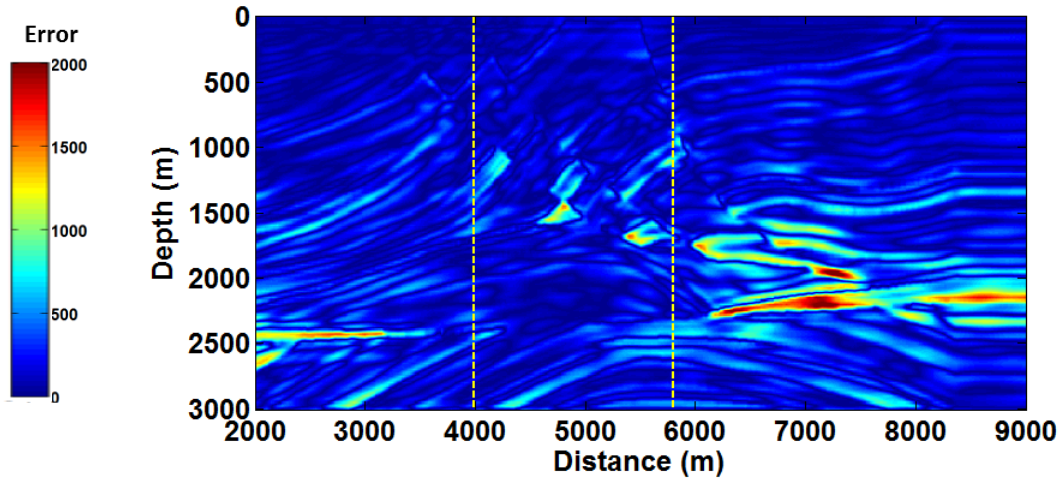
What if the calibration well is in another location?

Model 3

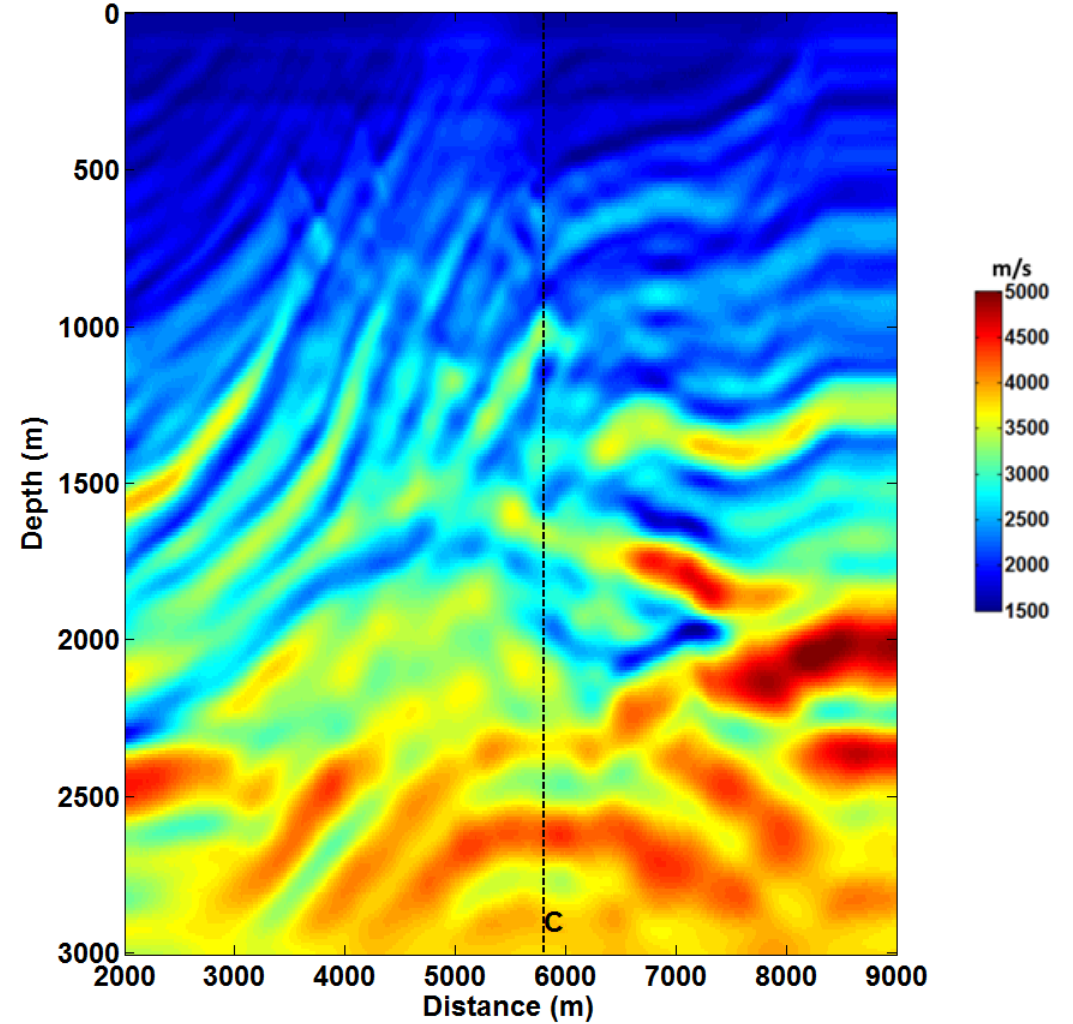
Horizontal distribution of the error



Spatial distribution of the error



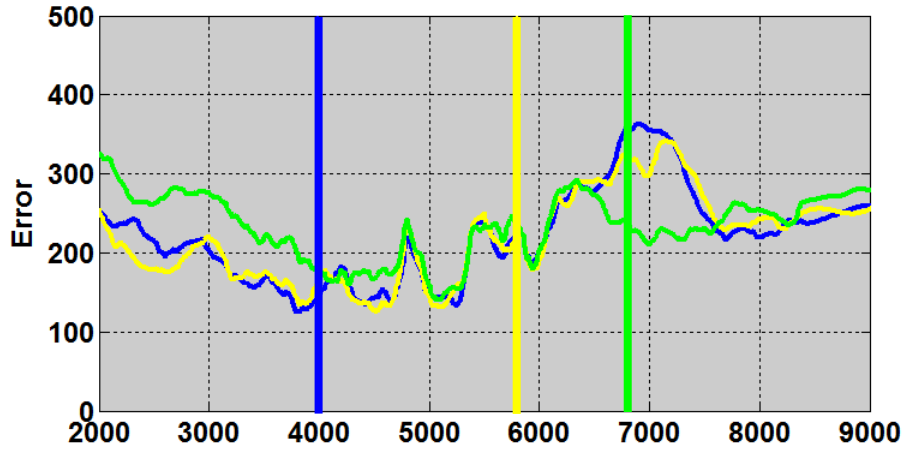
Calibration well at 5800 m



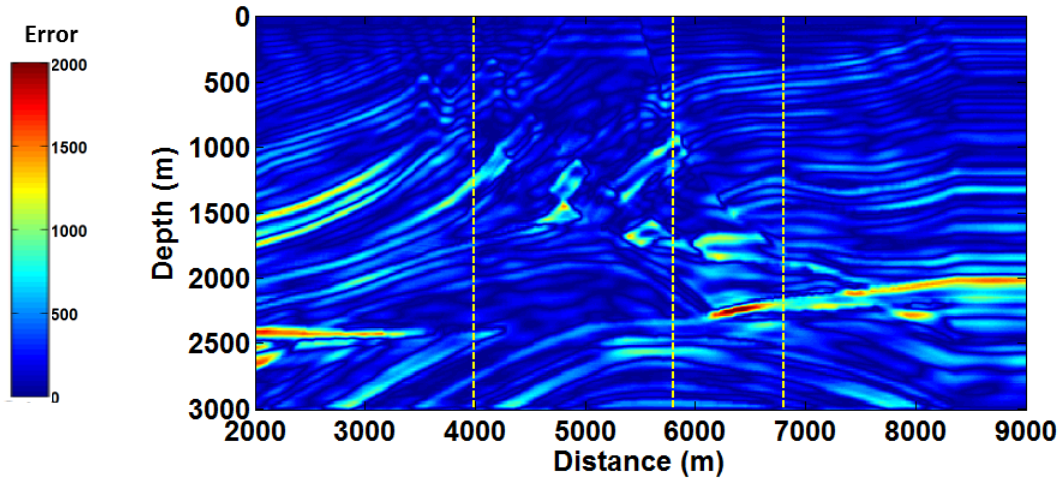
What if the calibration well is in another location?

Model 3

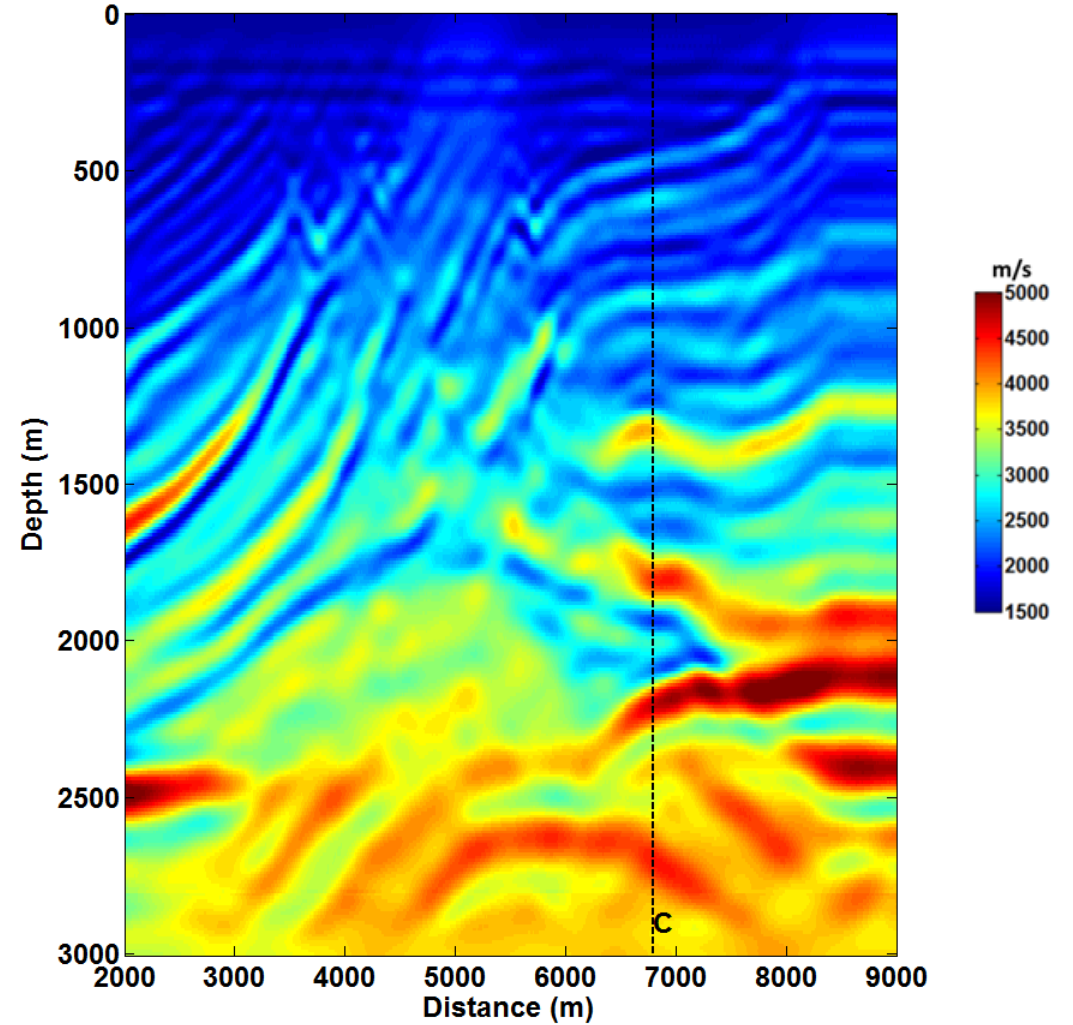
Horizontal distribution of the error



Spatial distribution of the error

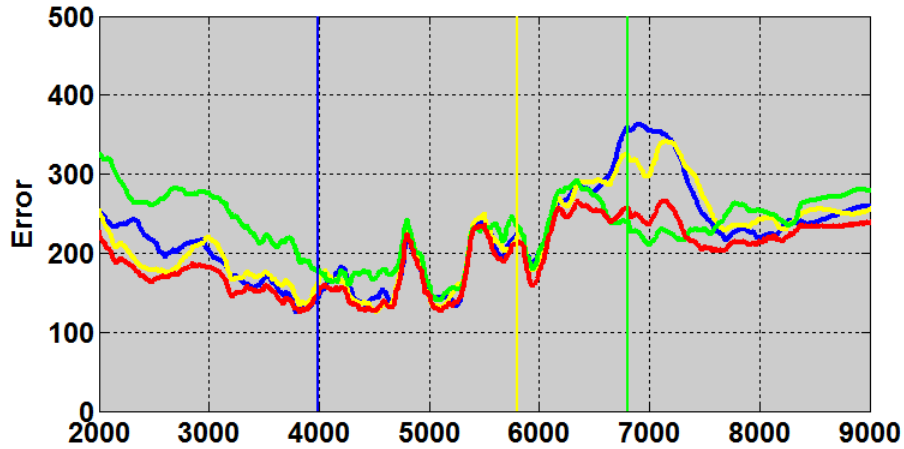


Calibration well at 6800 m

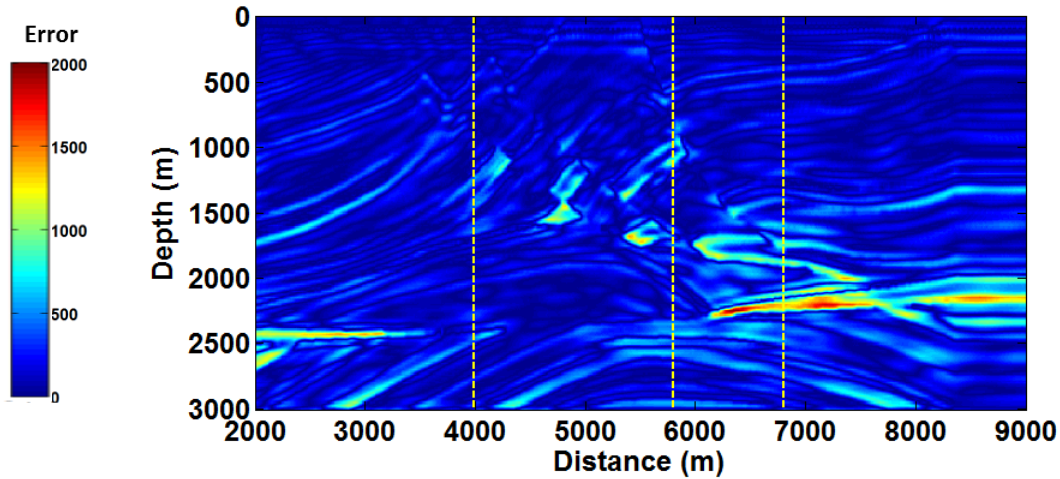


Using the three wells to obtain one match filter

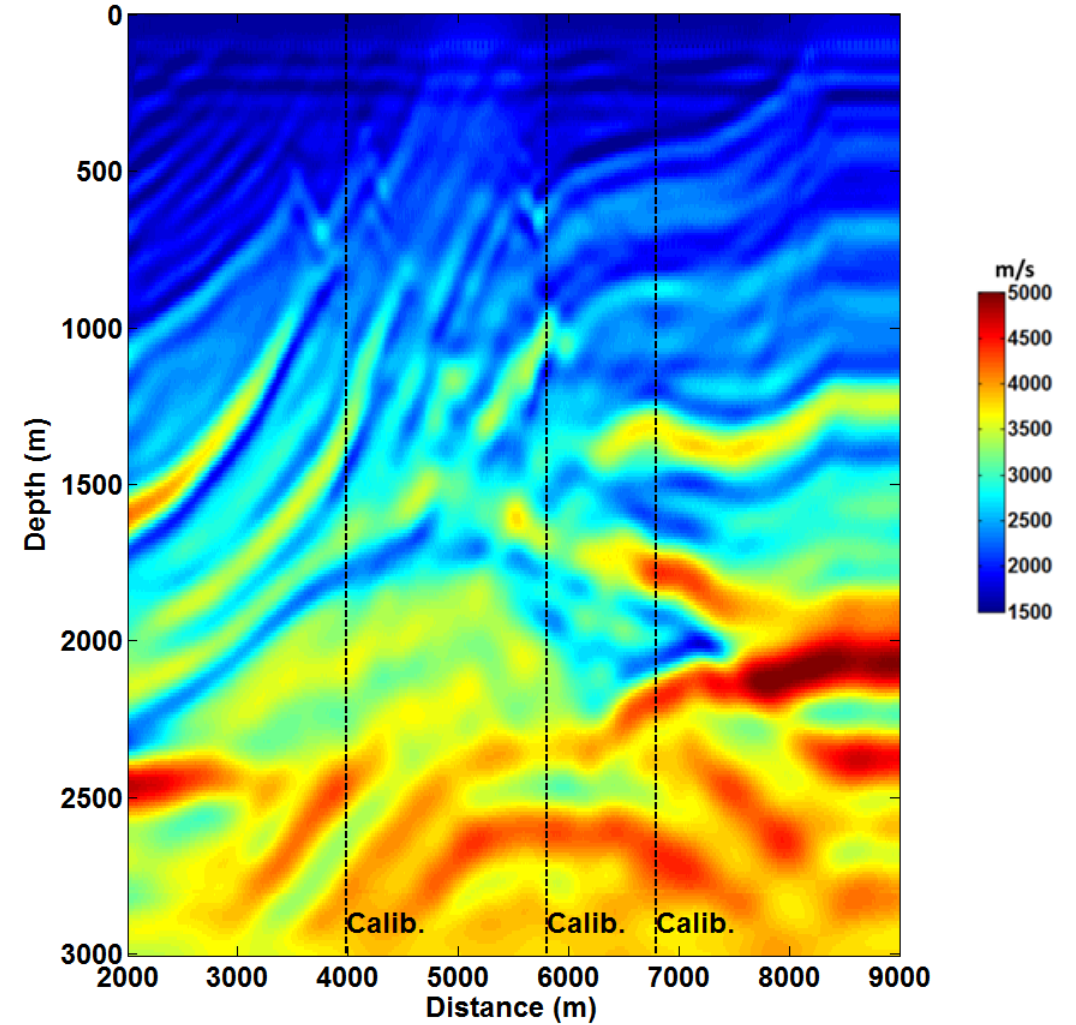
Horizontal distribution of the error



Spatial distribution of the error

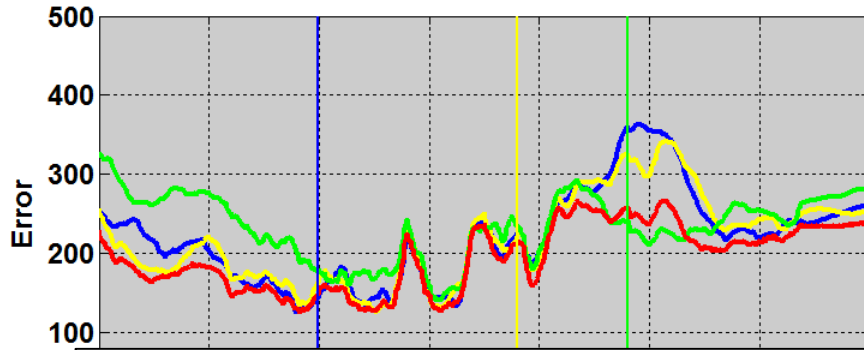


Average match filter

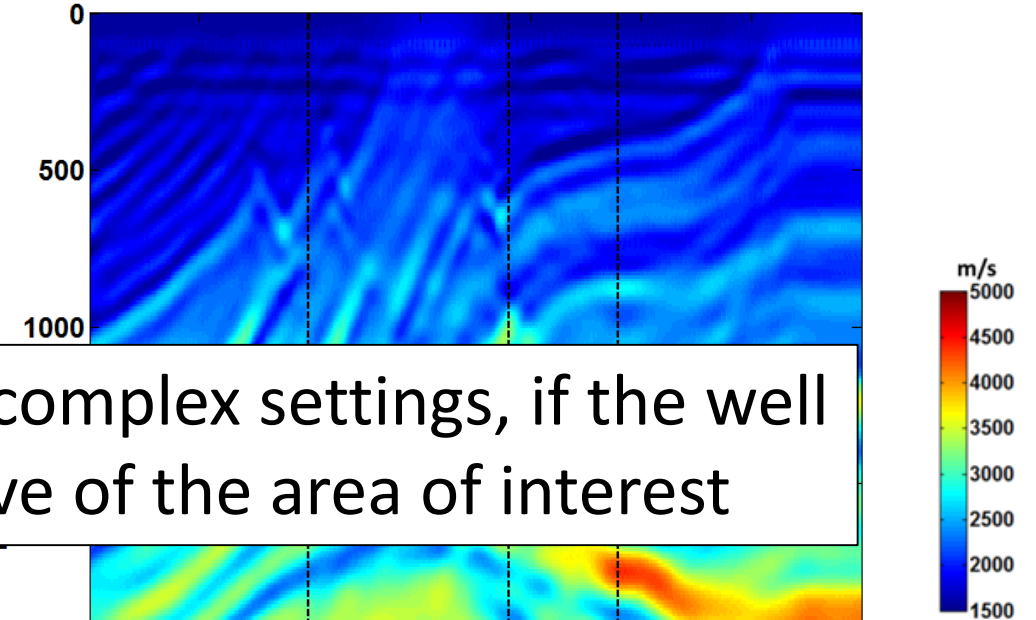


Using the three wells to obtain one match filter

Horizontal distribution of the error

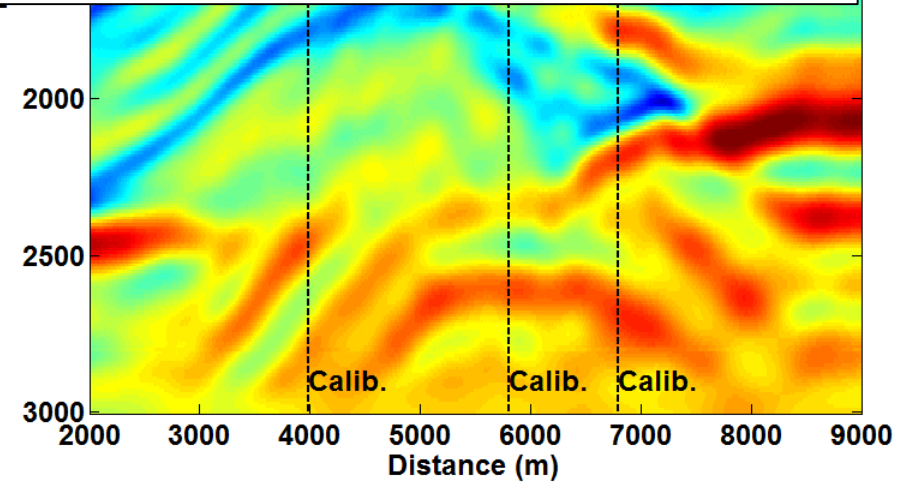
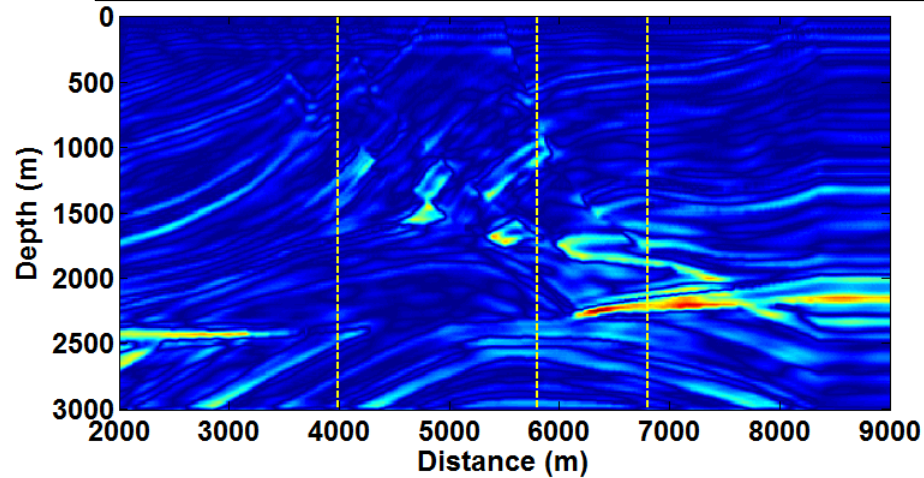


Average match filter



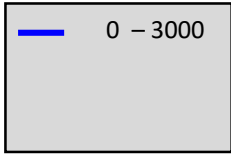
Well calibration works in high complex settings, if the well information is representative of the area of interest

Error

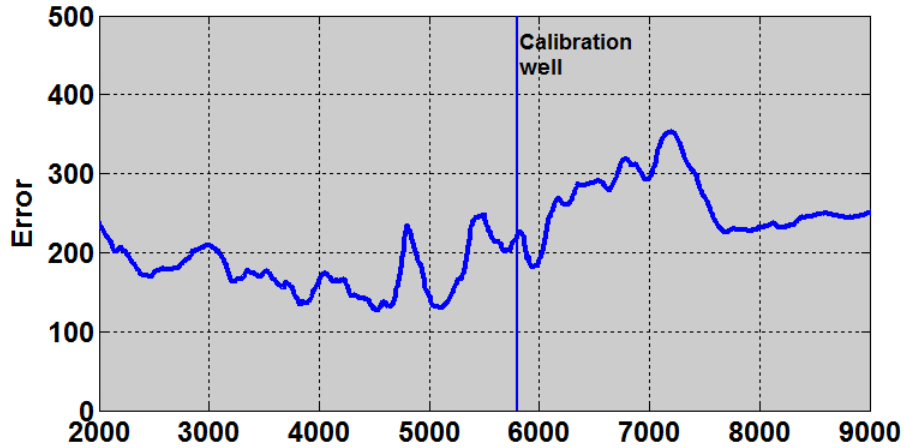


Varying depth interval

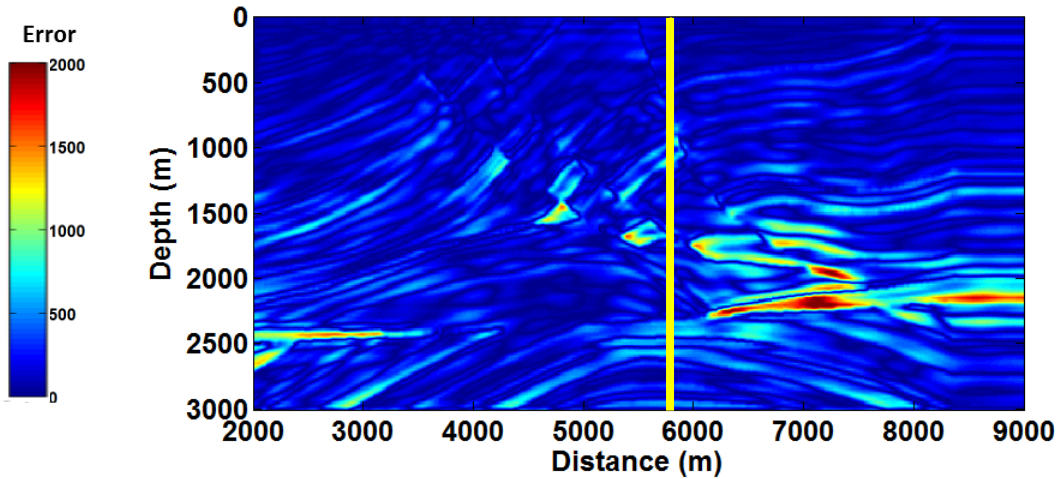
Depth interval (m)



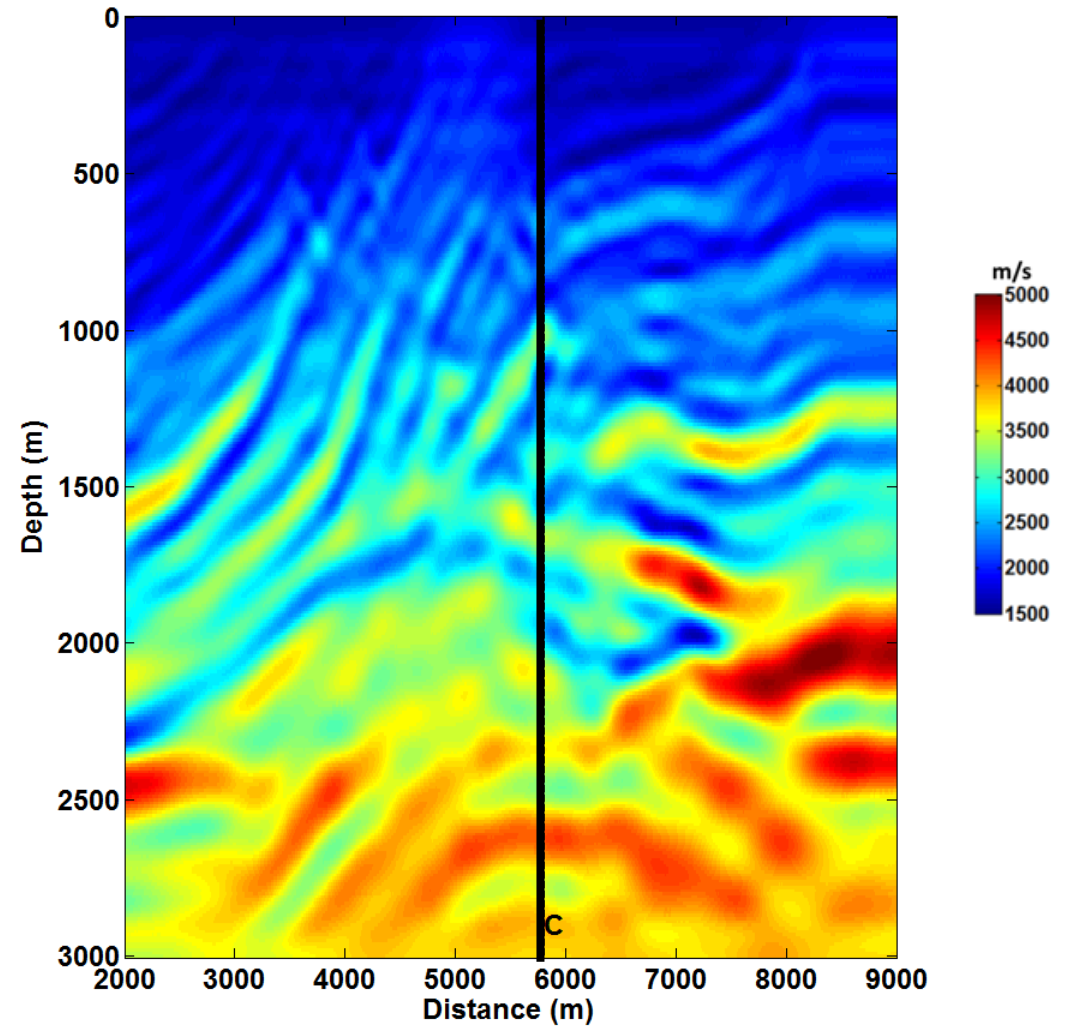
Horizontal distribution of the error



Spatial distribution of the error

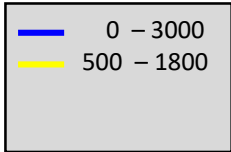


From 0 to 3000 m

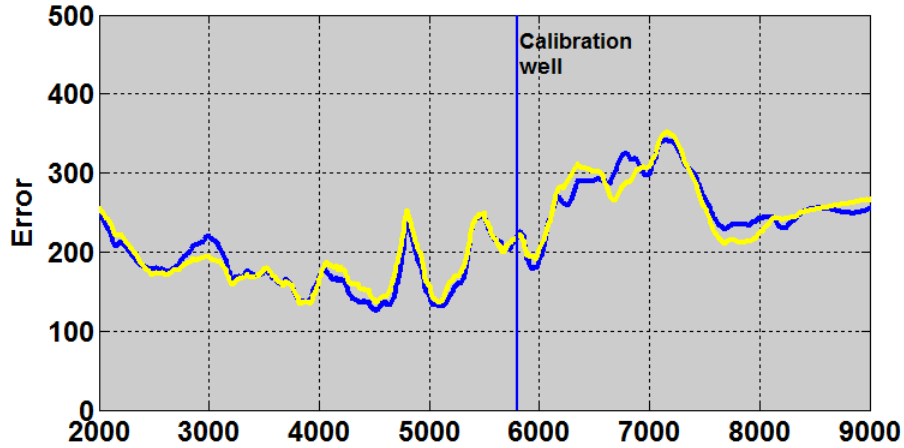


Varying depth interval

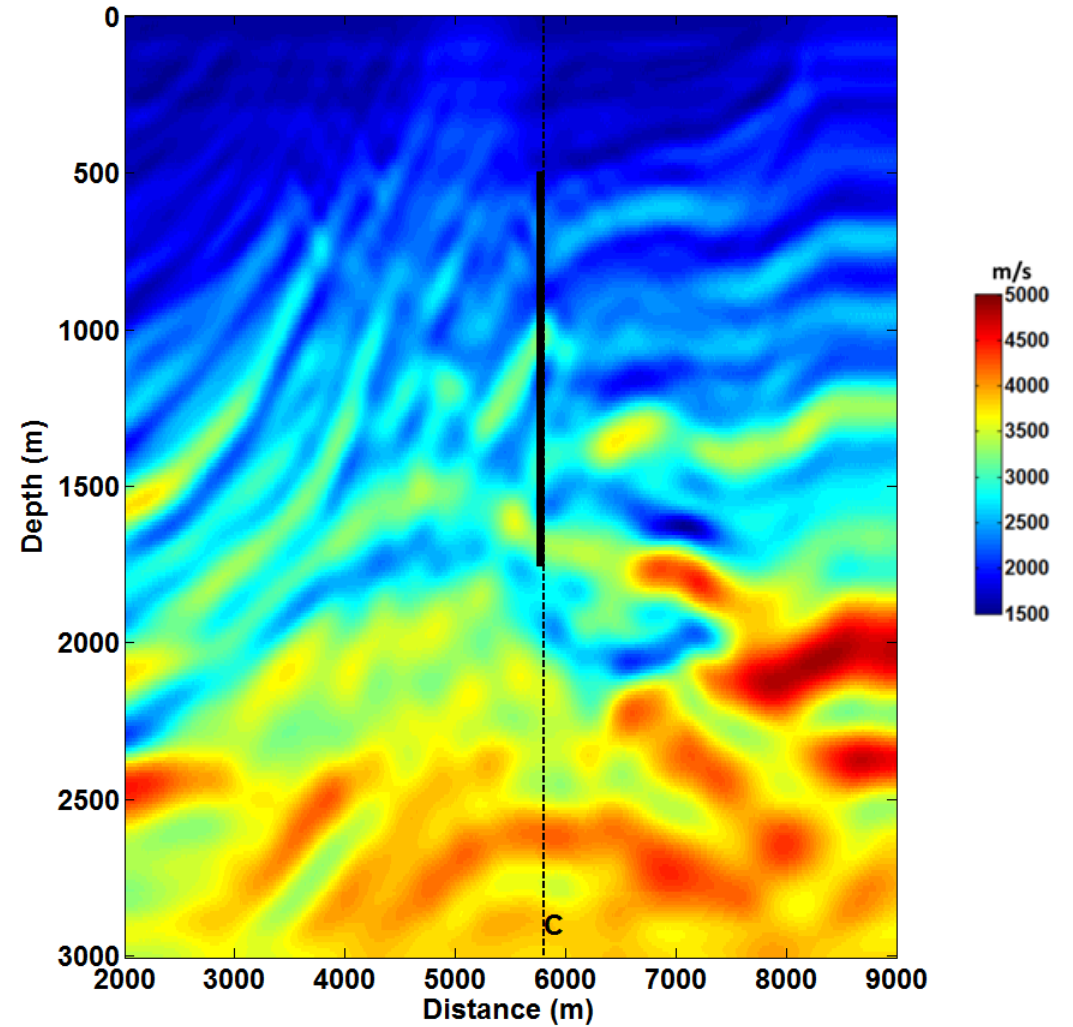
Depth interval (m)



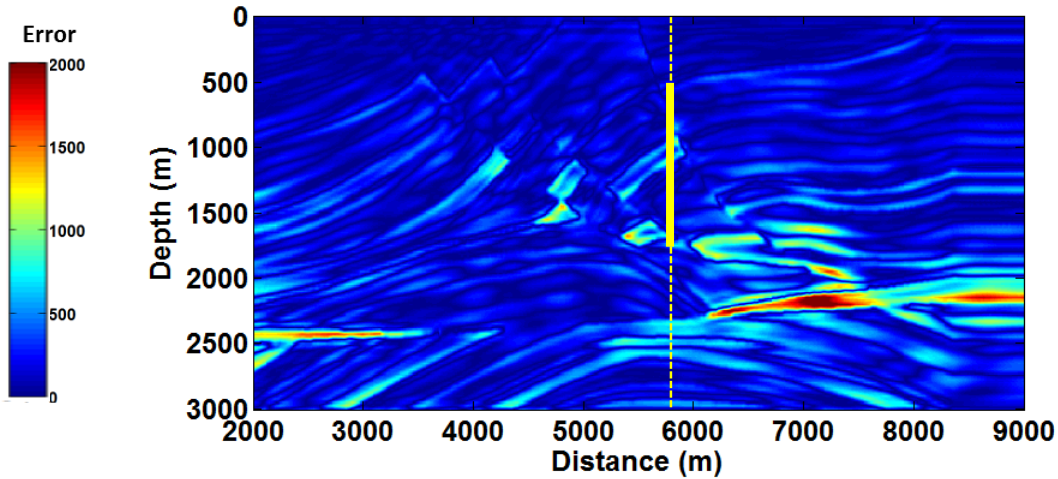
Horizontal distribution of the error



From 500 to 1800 m

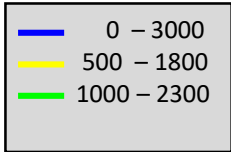


Spatial distribution of the error

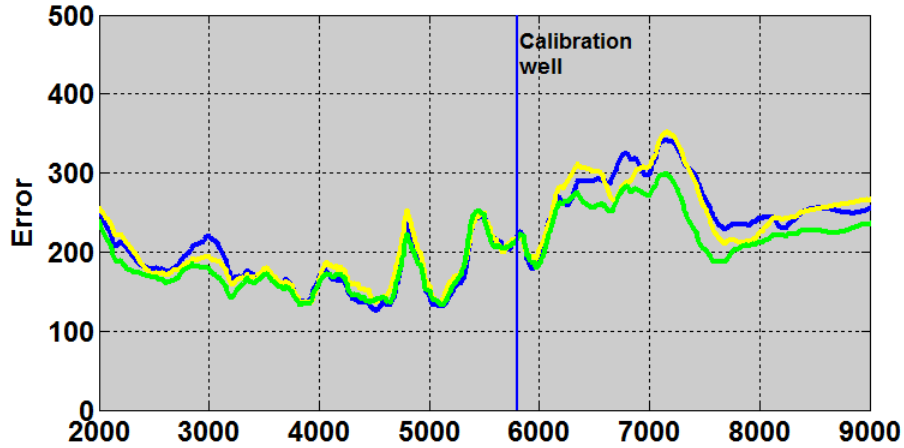


Varying depth interval

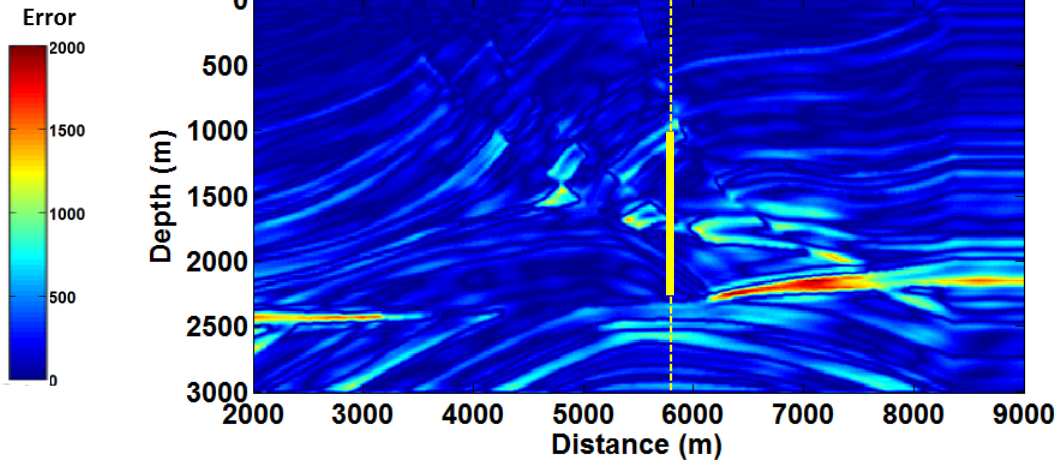
Depth interval (m)



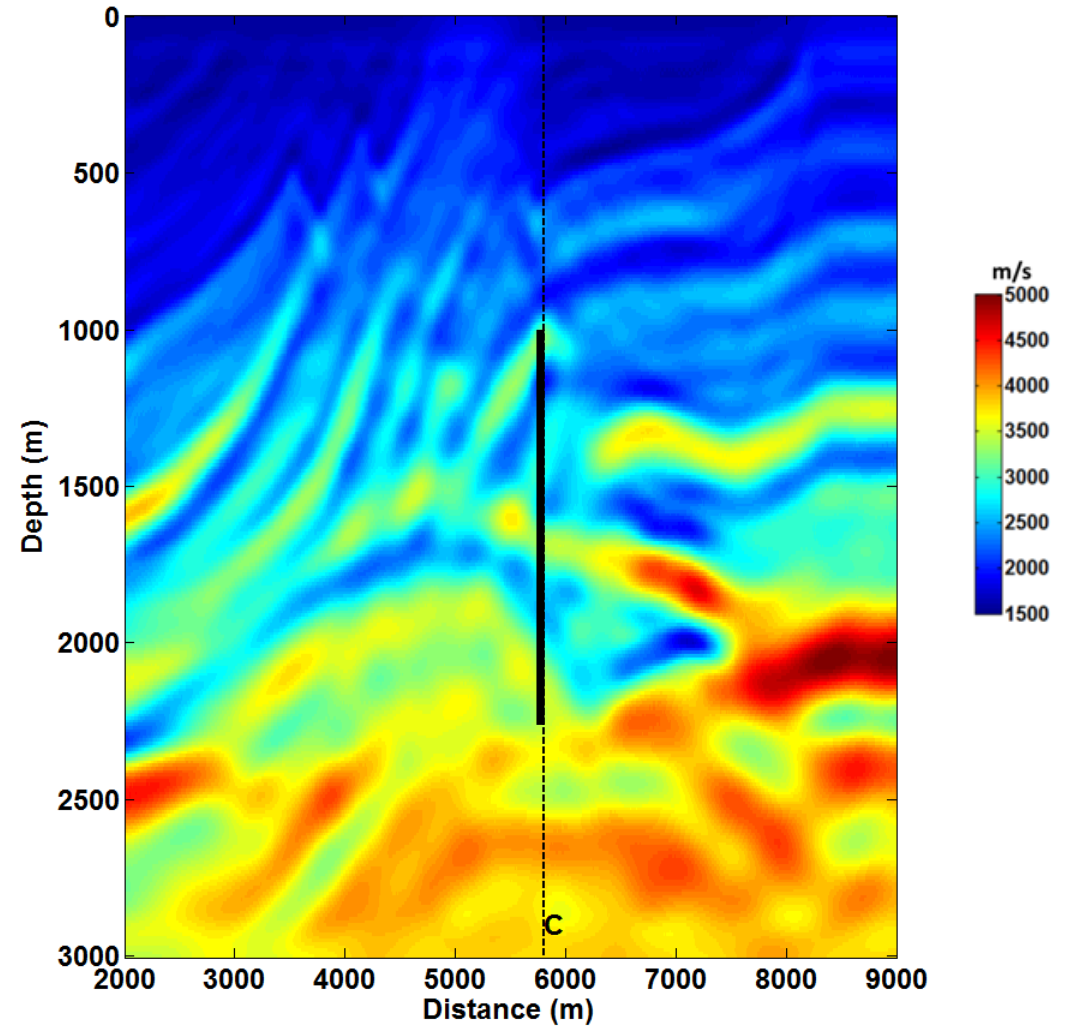
Horizontal distribution of the error



Spatial distribution of the error

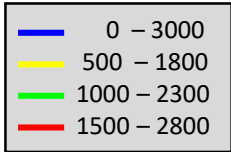


From 1000 to 2300 m

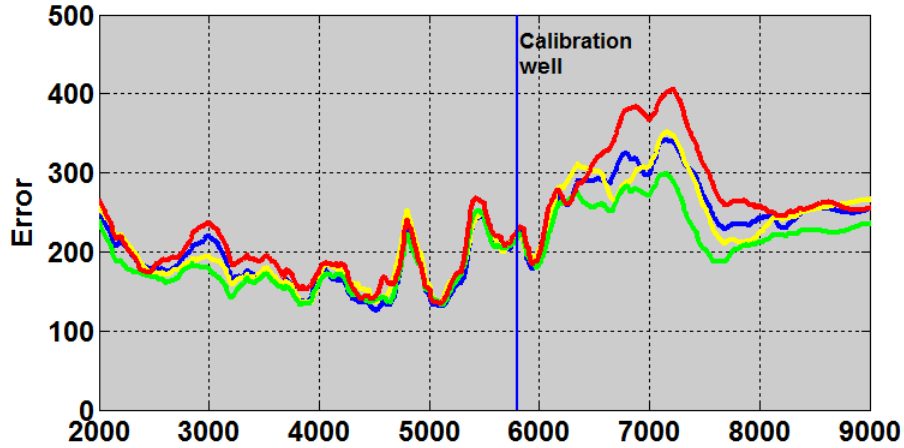


Varying depth interval

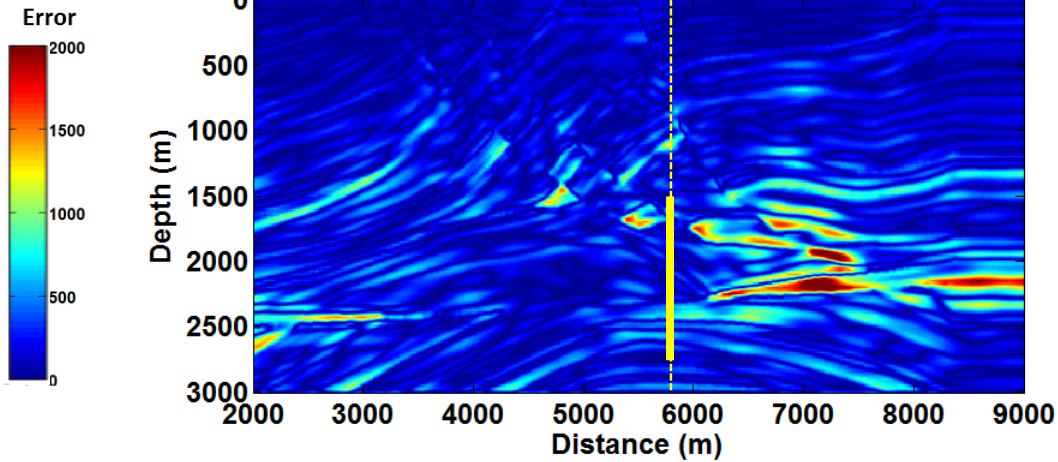
Depth interval (m)



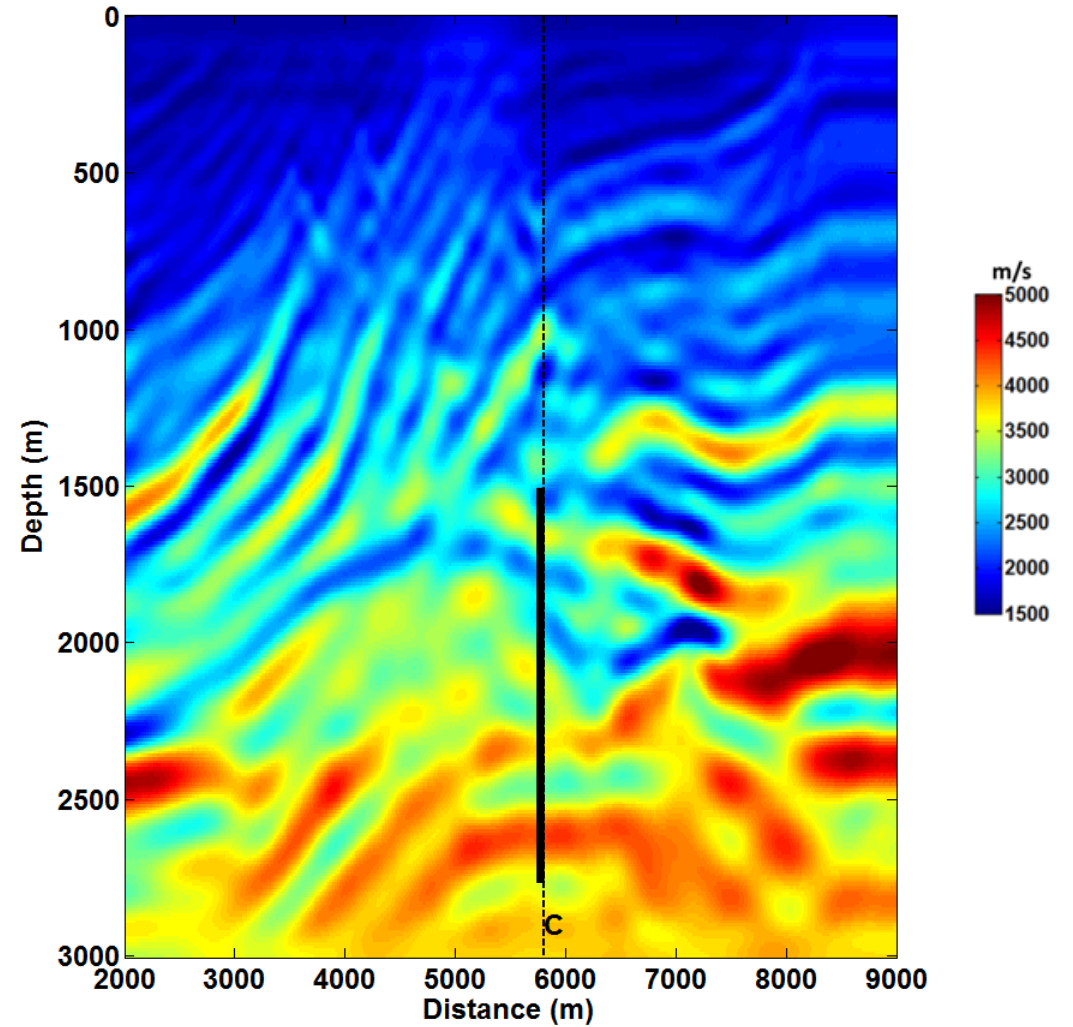
Horizontal distribution of the error



Spatial distribution of the error

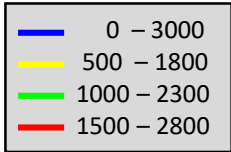


From 1500 to 2800 m

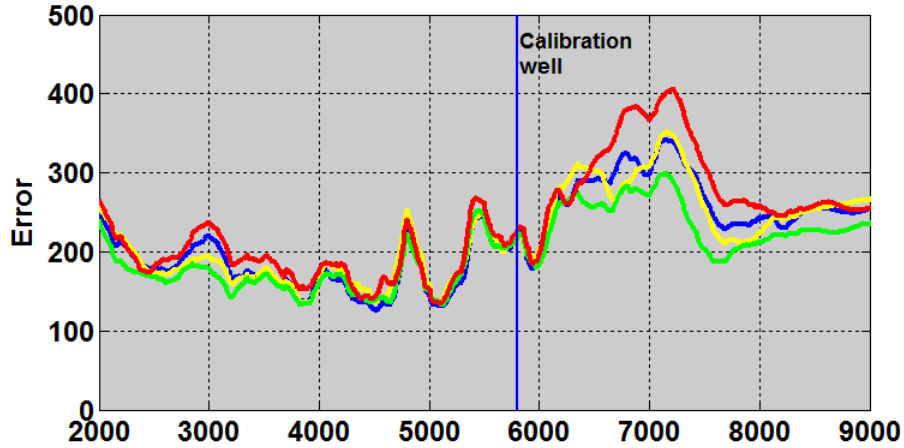


Varying depth interval

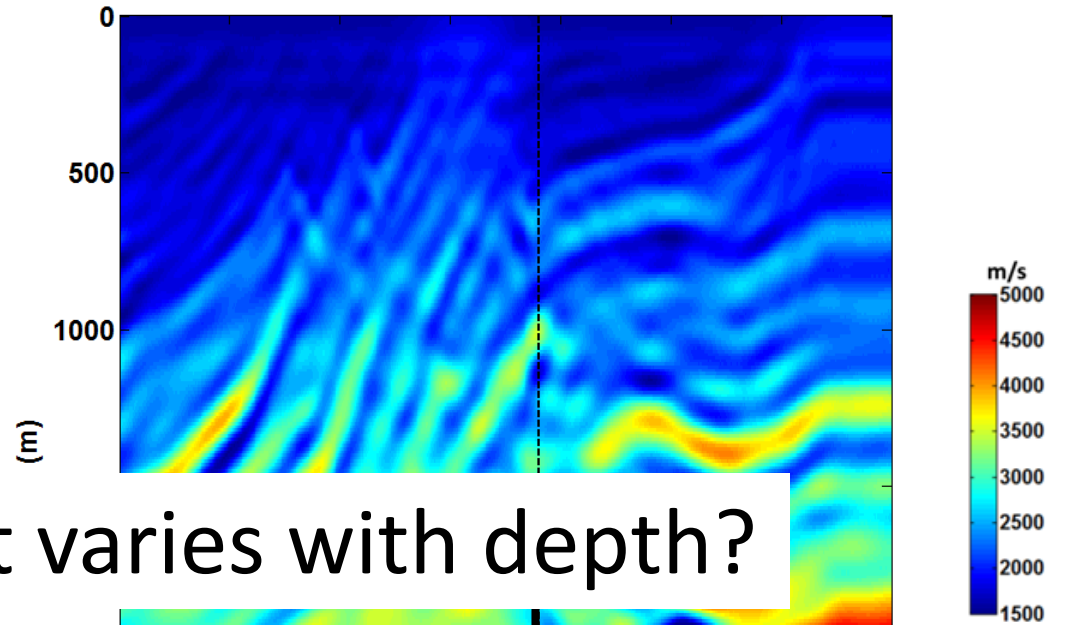
Depth interval (m)



Horizontal distribution of the error



From 1500 - 2800 m

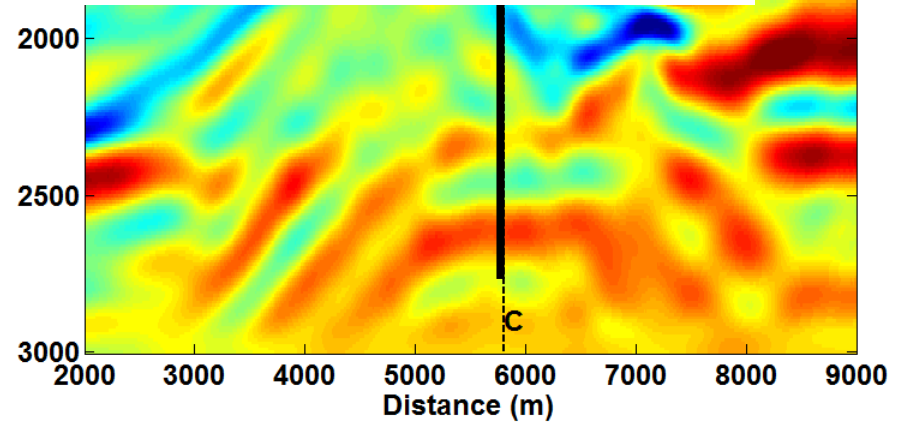
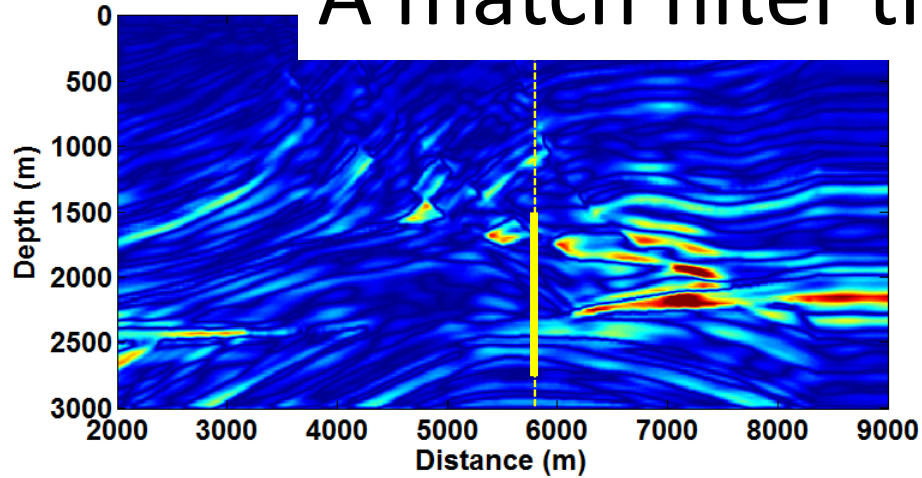


Spat

A match filter that varies with depth?

Error

Color scale for Error, ranging from 0 (blue) to 2000 (red).



Conclusions

- The gradient, calculated with a one-way wave migration method (PSPI) with a deconvolution imaging condition, points to the right direction in order to minimize the objective function in the FWI scheme.
- A scalar, estimated with well information, calibrates the gradient and produces suitable velocity perturbations to update the model. This was confirmed by consistently low errors in the well location even for the most complex model.
- Well calibration satisfactorily performs in the presence of moderate lateral velocity changes, such as in Model 1 and 2.
- Well calibration works in strong lateral velocity contexts, providing that the well is representative of the geology of the zone of interest.
- A match filter that varies both laterally and vertically may be a worthy option if we have multiple wells available and wide vertical coverage.

Future work

- We will address the elastic case. The goal will be, following IMMI's philosophy, to incorporate the knowledge and experience in AVO analysis and inversion into the FWI process.
- We will investigate how the integration of AVO information into the process of FWI can help finding a better scalar in a multi-parameter context.

Acknowledgements

Sponsors of CREWES for their support

NSERC through the grant CRDPJ 461179-13

PEMEX and the government of Mexico for funding this research

Thank you