

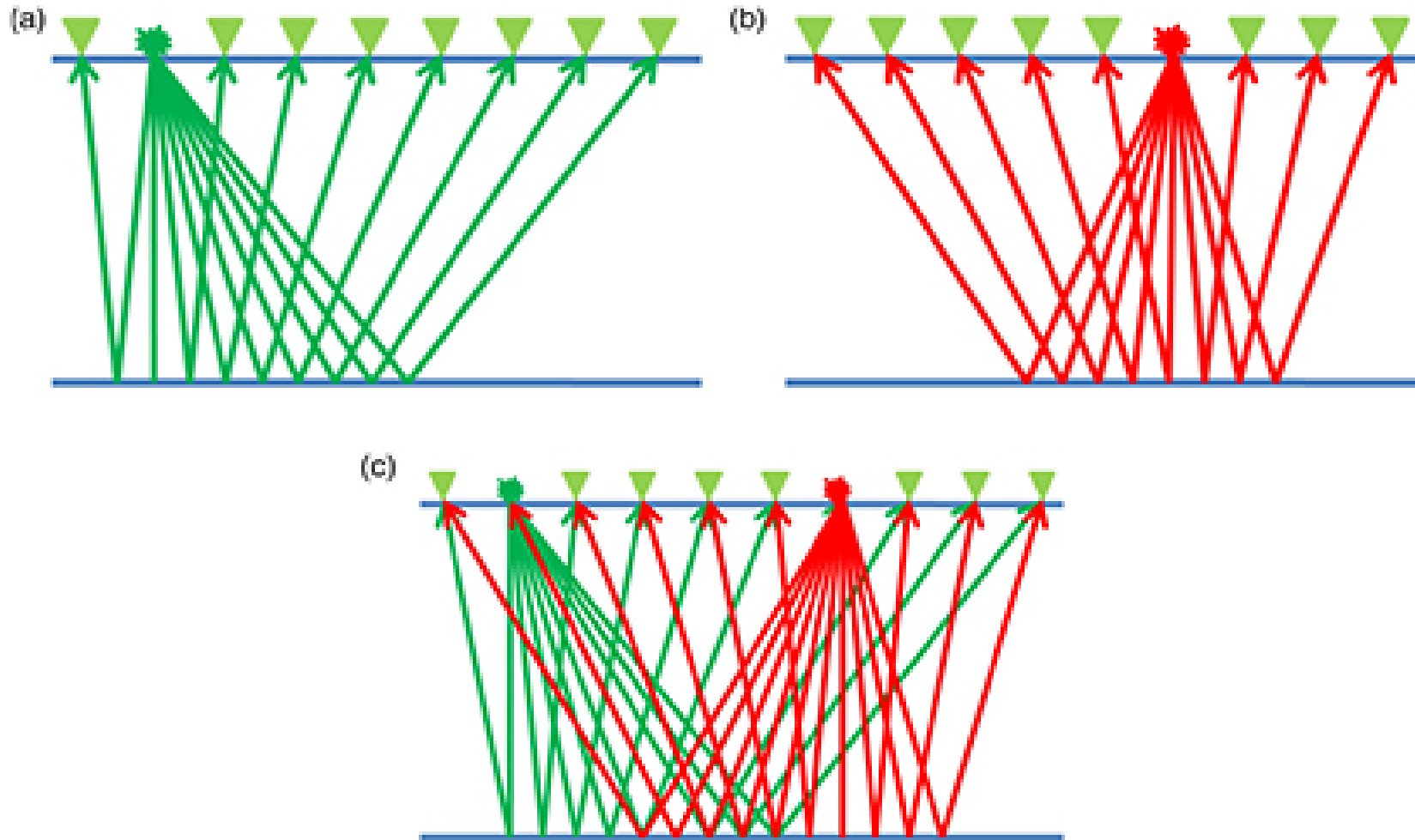
Deblending with Radon operators I: the CMP domain

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Dec 10, 2019 CREWES annual sponsor's meeting

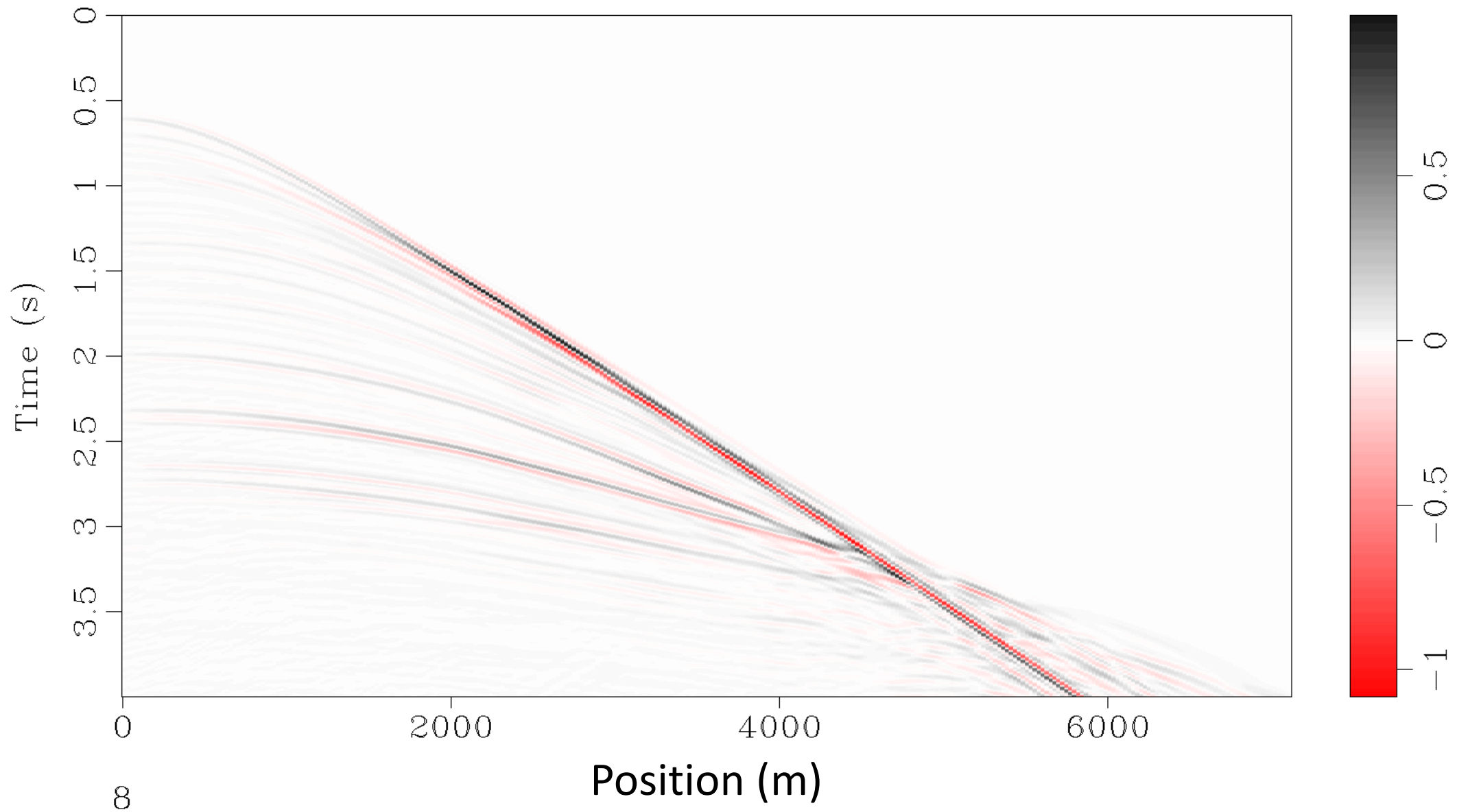


What is Blended data?



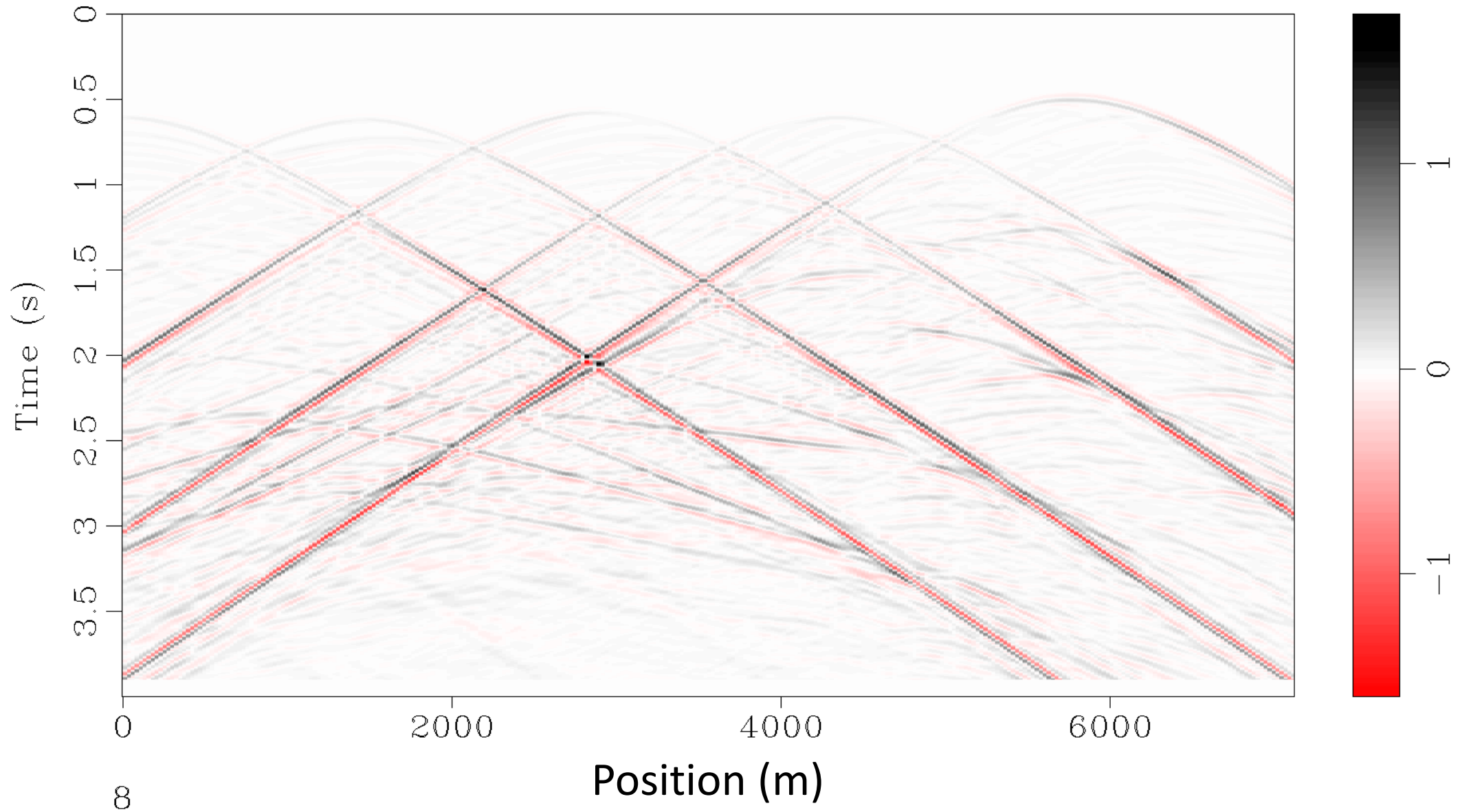


Marmousi shot





Blended Marmousi shot





1	0	$e^{-j\omega\Delta t_1}$	0
0	1	0	$e^{-j\omega\Delta t_2}$

Γ

	0	0	0
0		0	0
0	0		0
0	0	0	

S

	0		0
0		0	

S_{bl}



Forward model of Blending:

$$d = \Gamma m$$

Because the blending matrix Γ is underdetermined the direct inverse cannot be assessed

$$m = (\Gamma^H \Gamma)^{-1} \Gamma^H d$$

Unfortunately, this problem is ill posed and therefore needs to be re-formulated

$$\mathbf{m} = (\Gamma^H \Gamma)^{-1} \Gamma^H d$$

Pseudo-deblending

$$S_{pdb} = \Gamma^H S_{bl}, \quad \text{Where } S_{bl} = \Gamma S,$$

Therefore Pseudo deblending can be considered an operation on the pre-blended dataset:

$$S_{pbl} = \Gamma^H \Gamma S.$$

$$S_{pbl} = S \Gamma^H \Gamma.$$

$e^{-j\omega\Delta t_i}$	0
0	$e^{-j\omega\Delta t_k}$
$e^{-j\omega\Delta t_j}$	0
0	$e^{-j\omega\Delta t_l}$

 \cdot





$e^{+j\omega\Delta t_i}$	0	$e^{+j\omega\Delta t_j}$	0
0	$e^{+j\omega\Delta t_k}$	0	$e^{+j\omega\Delta t_l}$

 $=$

1	0	$e^{-j\omega\Delta t_{ij}}$	0
0	1	0	$e^{-j\omega\Delta t_{kl}}$
$e^{-j\omega\Delta t_{ji}}$	0	1	0
0	$e^{-j\omega\Delta t_{lk}}$	0	1

 $\Gamma^H \times \Gamma = \Gamma^H \Gamma$











	0	0	0
0		0	0
0	0		0
0	0	0	

 \times

1	0	$e^{-j\omega\Delta t_{ij}}$	0
0	1	0	$e^{-j\omega\Delta t_{kl}}$
$e^{-j\omega\Delta t_{ji}}$	0	1	0
0	$e^{-j\omega\Delta t_{lk}}$	0	1

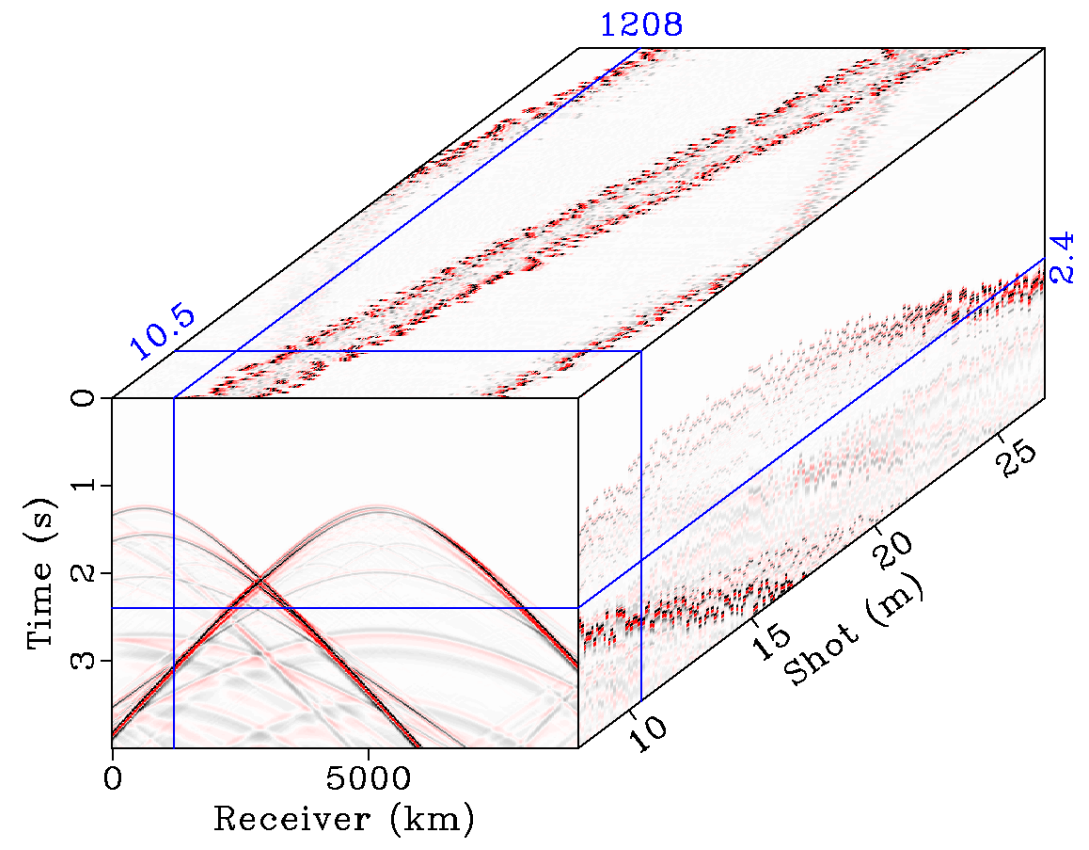
 $=$

	0		0
0		0	
	0		0
0		0	

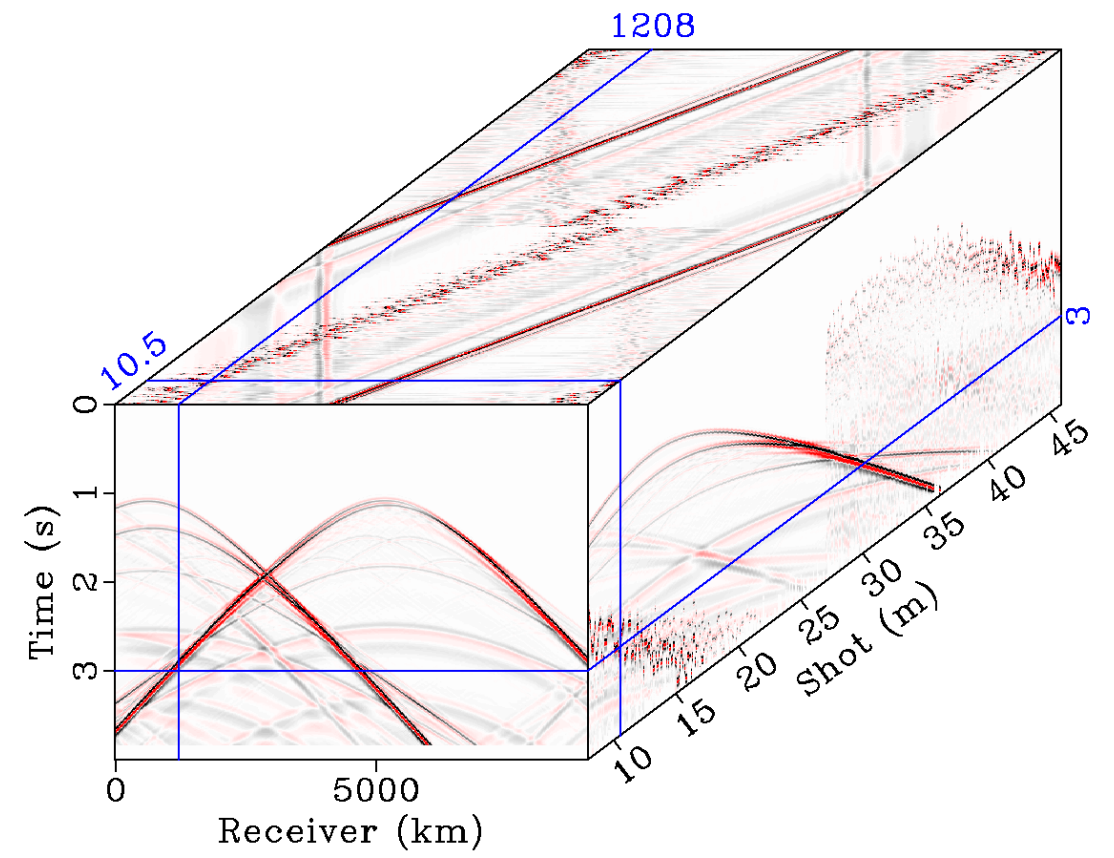
$$S \Gamma^H \Gamma = S_{pbl}$$



Blended Data



Pseudo Deblended Data

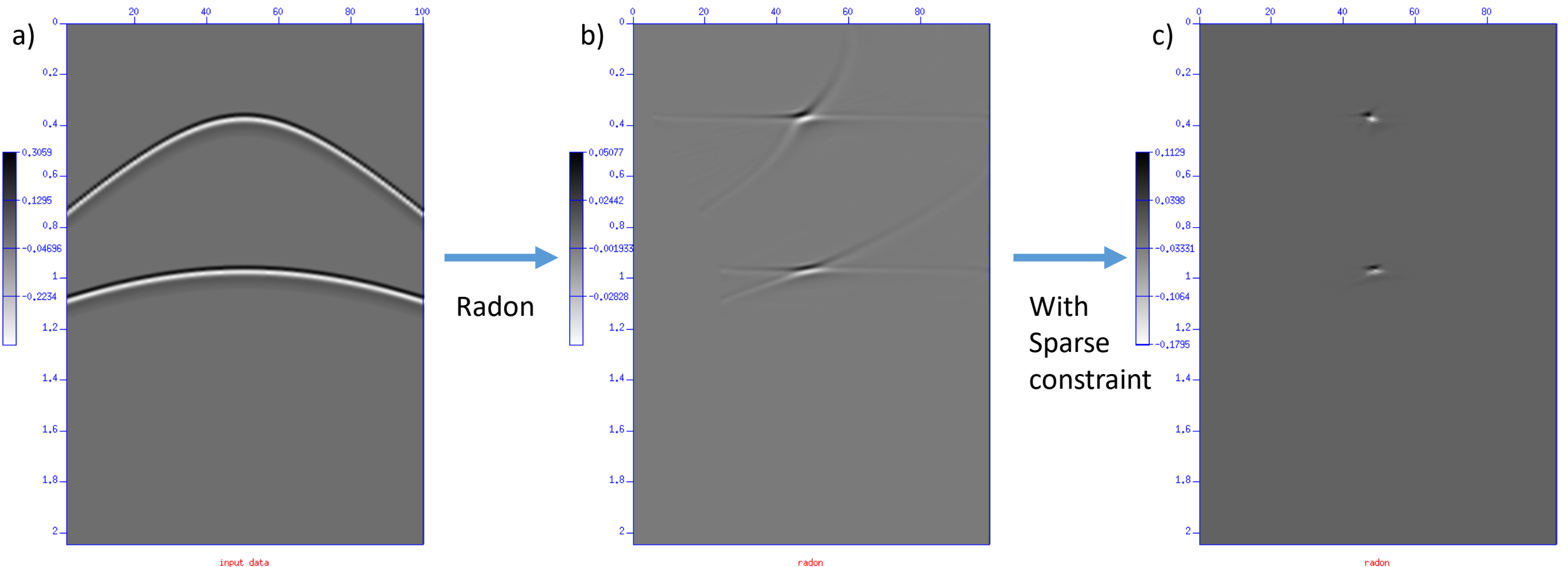




Sparse Hyperbolic Radon Transform

$$u(p, \tau) = \int_{h_1}^{h_2} d(h, t = \sqrt{\tau^2 + p^2 h^2}) dh$$

where $u(p,t)$ is the radon space data, p is the slowness, t is the two way travel time, h_1 is the upper offset limit, h_2 the lower offset limit, and d is the data space to be transformed. The slowness p is then defined as the inverse of velocity $1/V$.





Radon Denoising

$$S_{pdb} = S_{bl} \Gamma^H$$

$$\left\| S_{pdb} - Rm \right\|_2^2 + \mu \|m\|_1$$

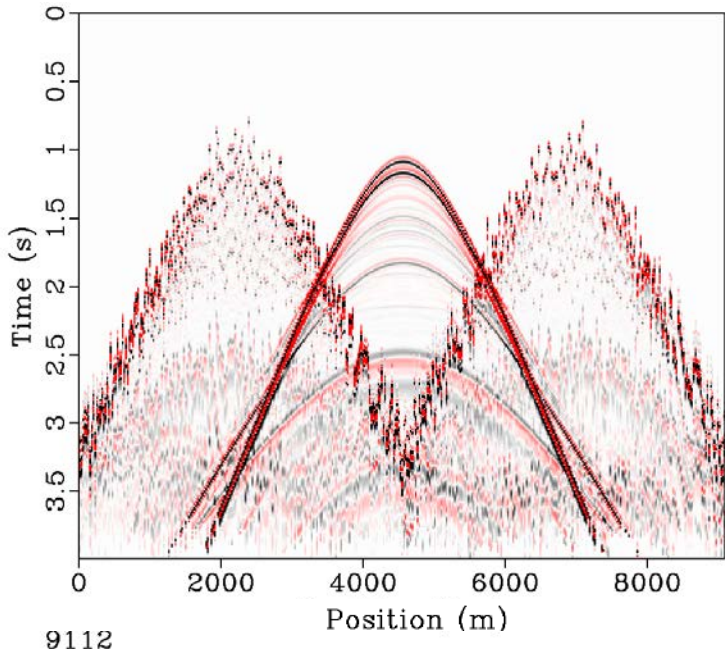
Radon Inversion

$$\left\| S_{bl} - \Gamma Rm \right\|_2^2 + \mu \|m\|_1$$

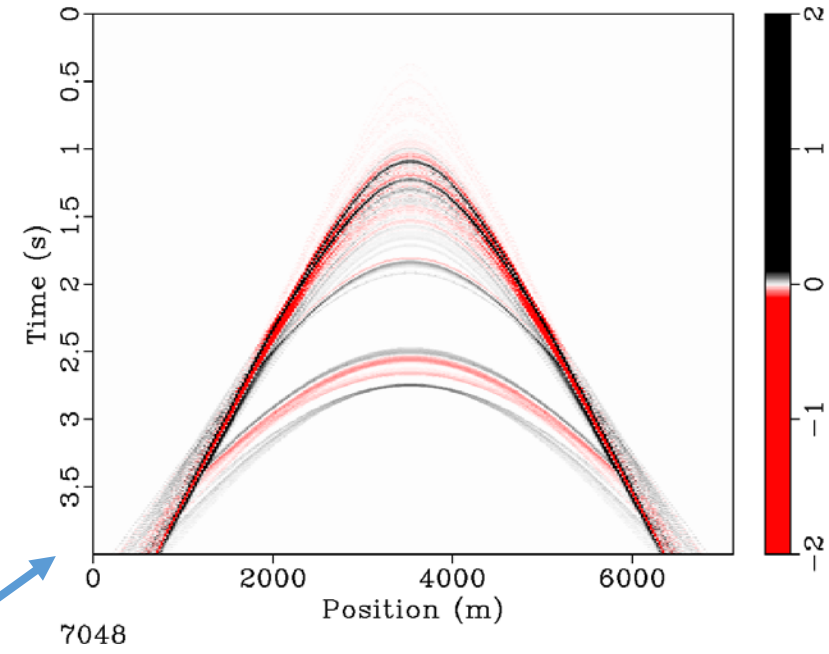
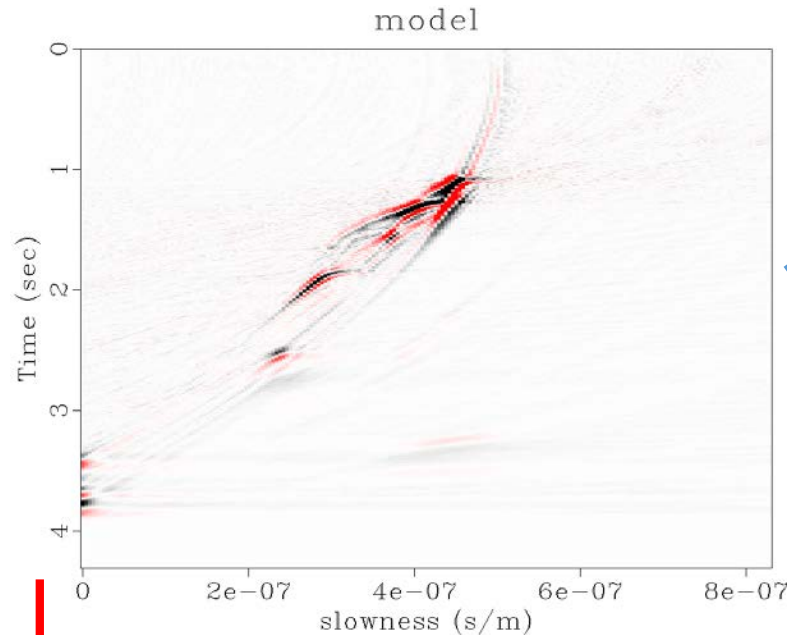


Denoising – sparse radon transform

$$\left\| S_{pdb} - \boxed{R}m \right\|_2^2 + \mu \|m\|_1$$



Adjoint Operator



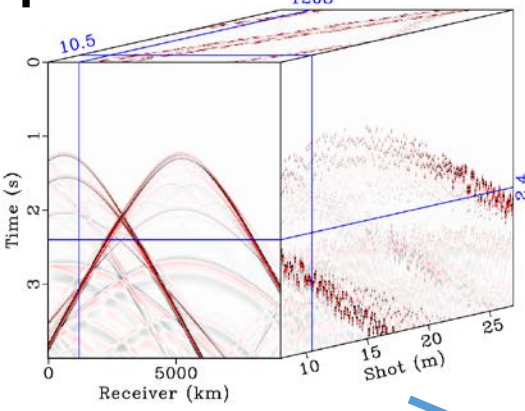
Forward Operator



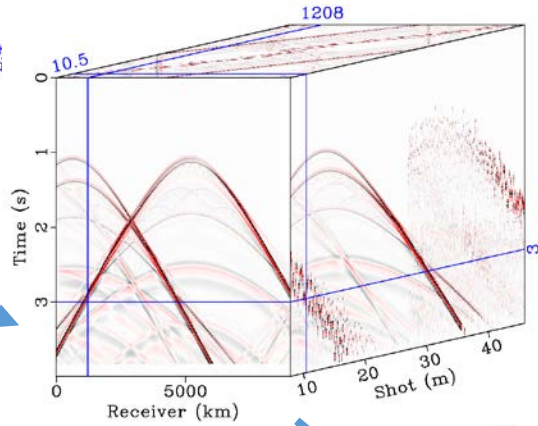
Sparse Inversion

$$\|S_{bl} - \Gamma R m\|_2^2 + \mu \|m\|_1$$

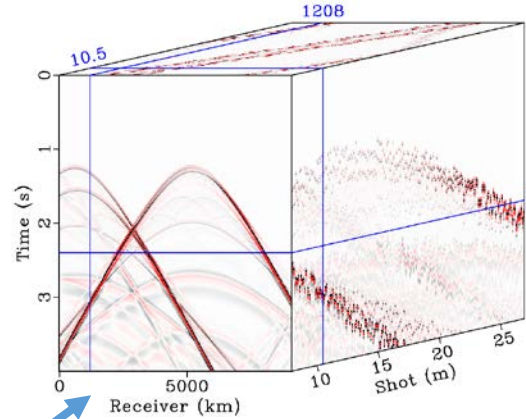
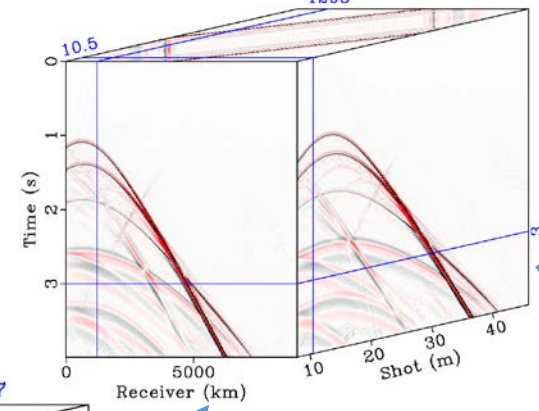
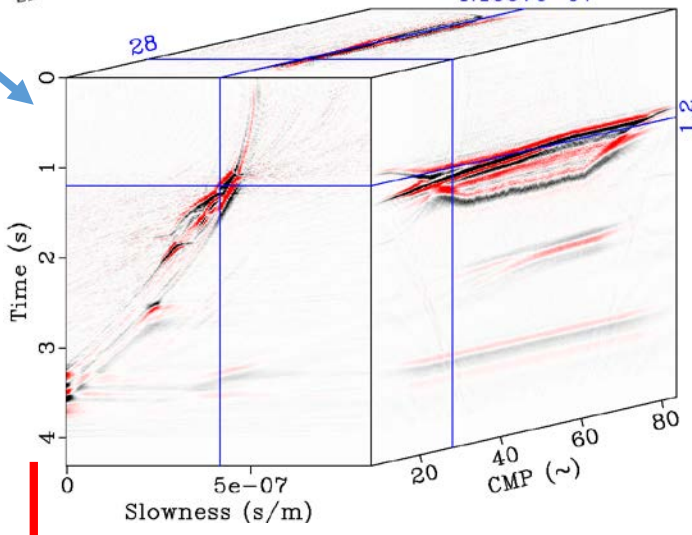
Fitting



Pseudo



Radon



Blending

Adjoint Operator

Forward Operator

Events are centered

Dipping and complex geometries are centered for the most part with no shifted apexes

Radon operator

Relatively simpler, just hyperbolic instead of apex shifted
Reduces computational time

3D data is normally sorted into CMP bins for processing

Traces per CMP not consistent

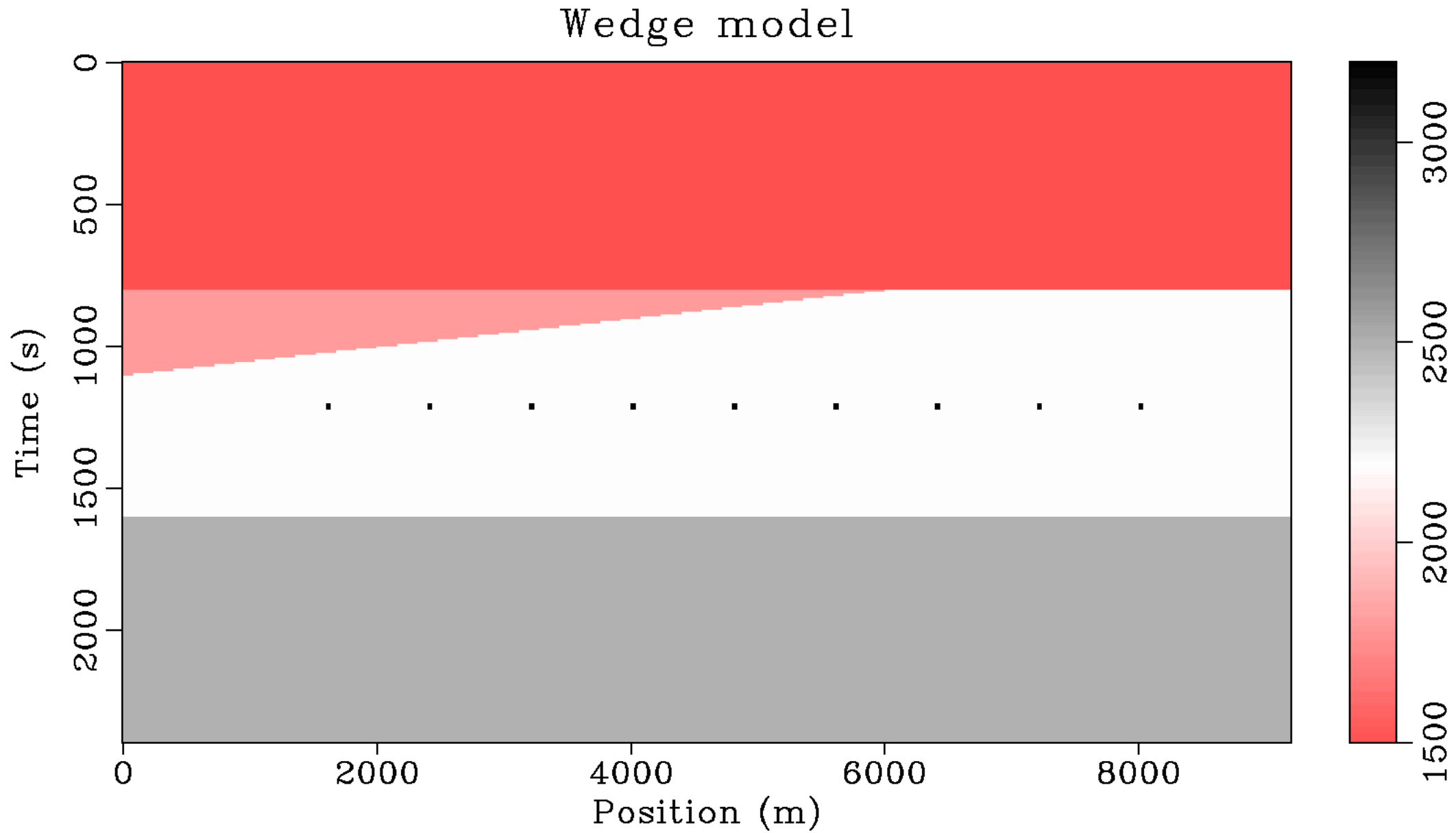
- Traces per CMP varies based on location within survey

- Very few traces at the edges

Aliasing

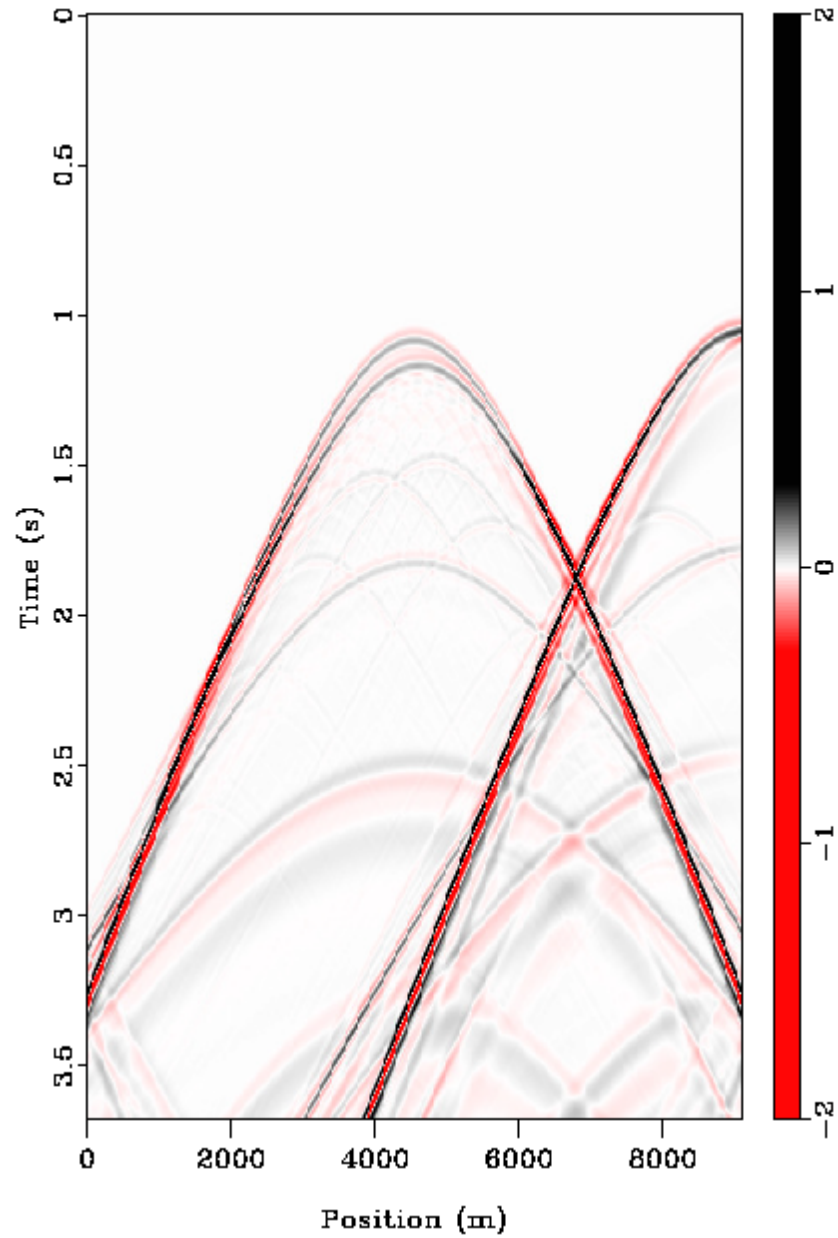
- CMP domain has half the sampling interval compared to receiver/domain

- High likelihood events will be aliased

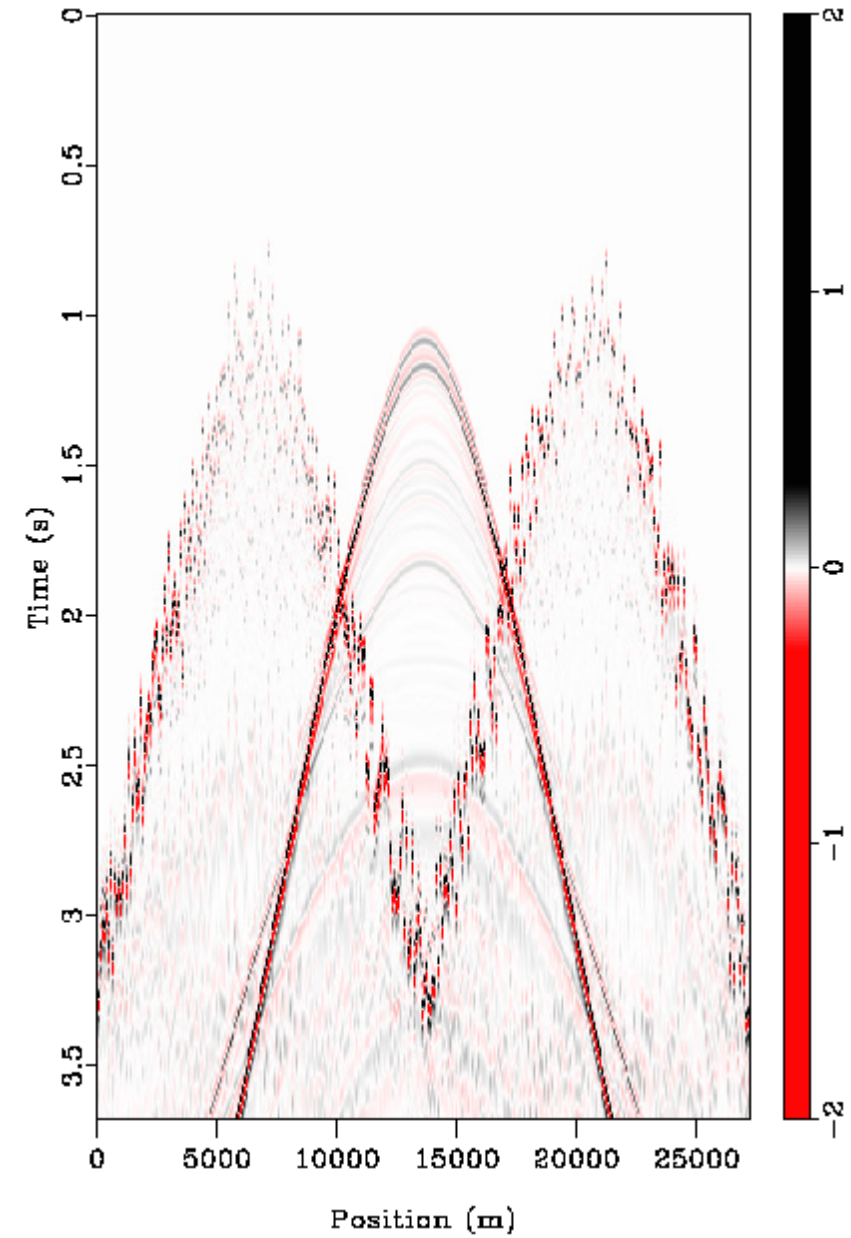




b) Pseudo deblended (CSG)

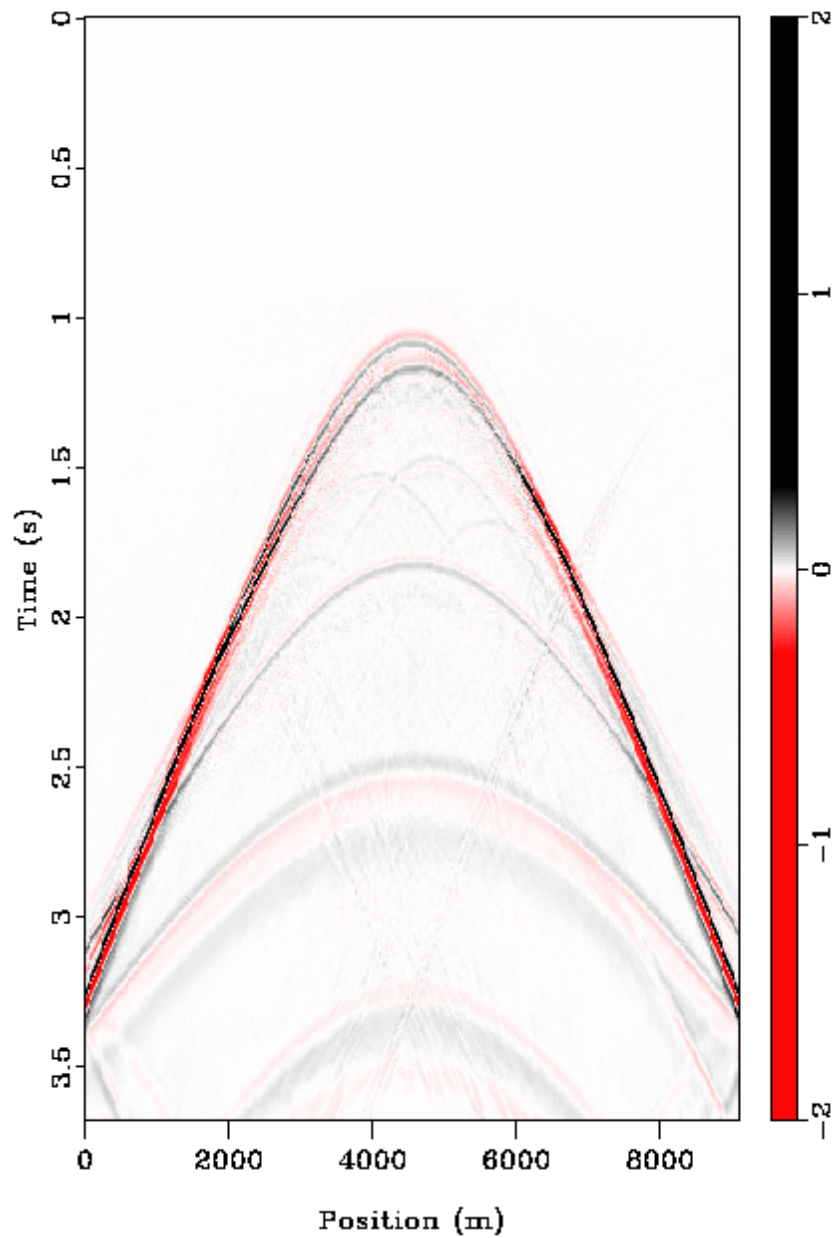


b) Pseudo deblended (CMP)

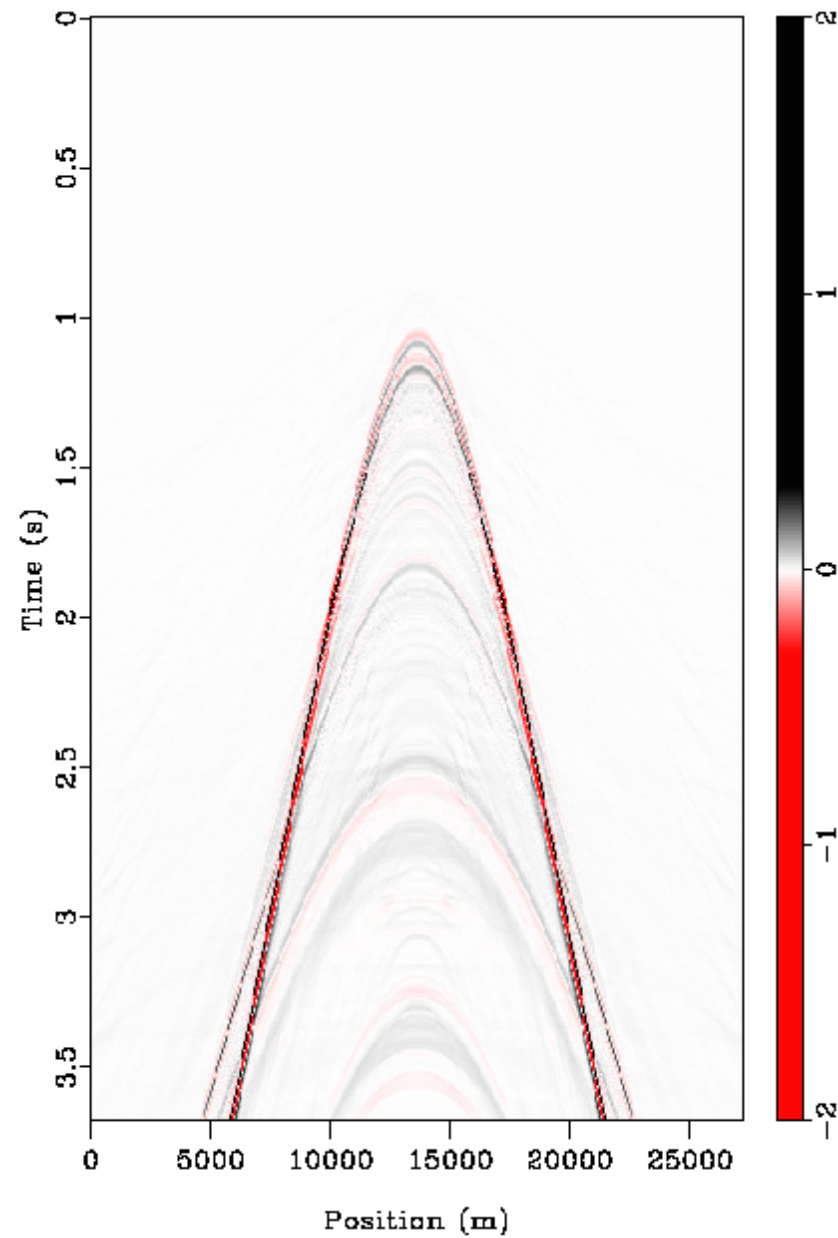


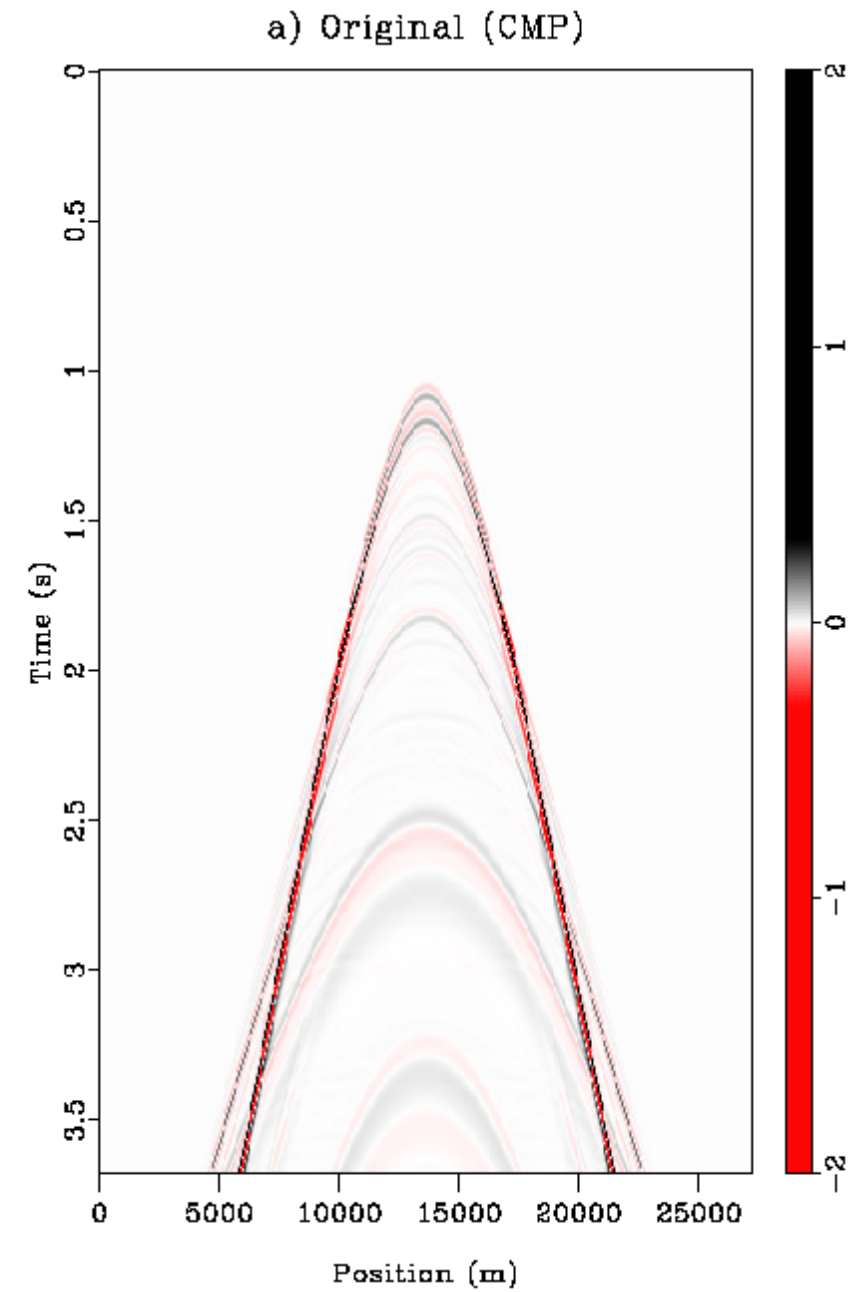
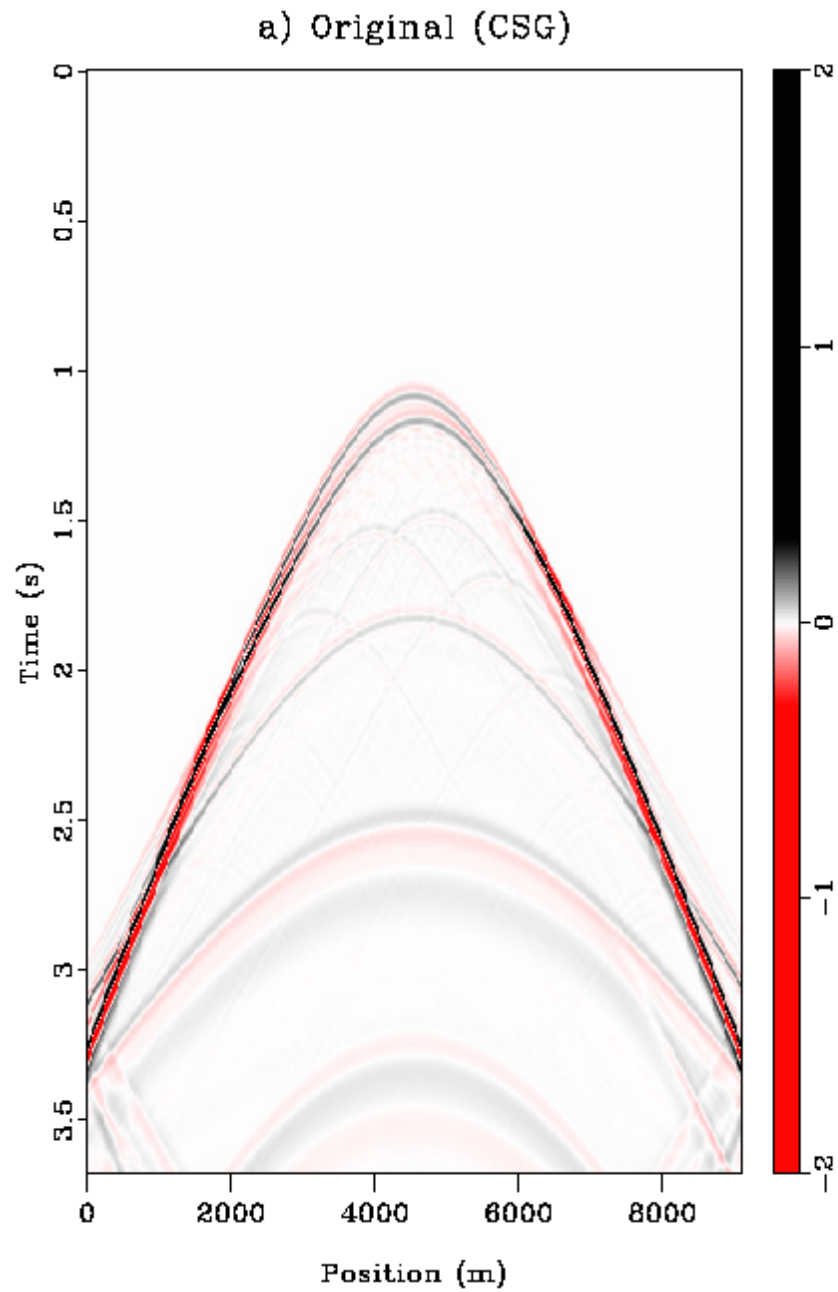


c) Deblended (CSG)



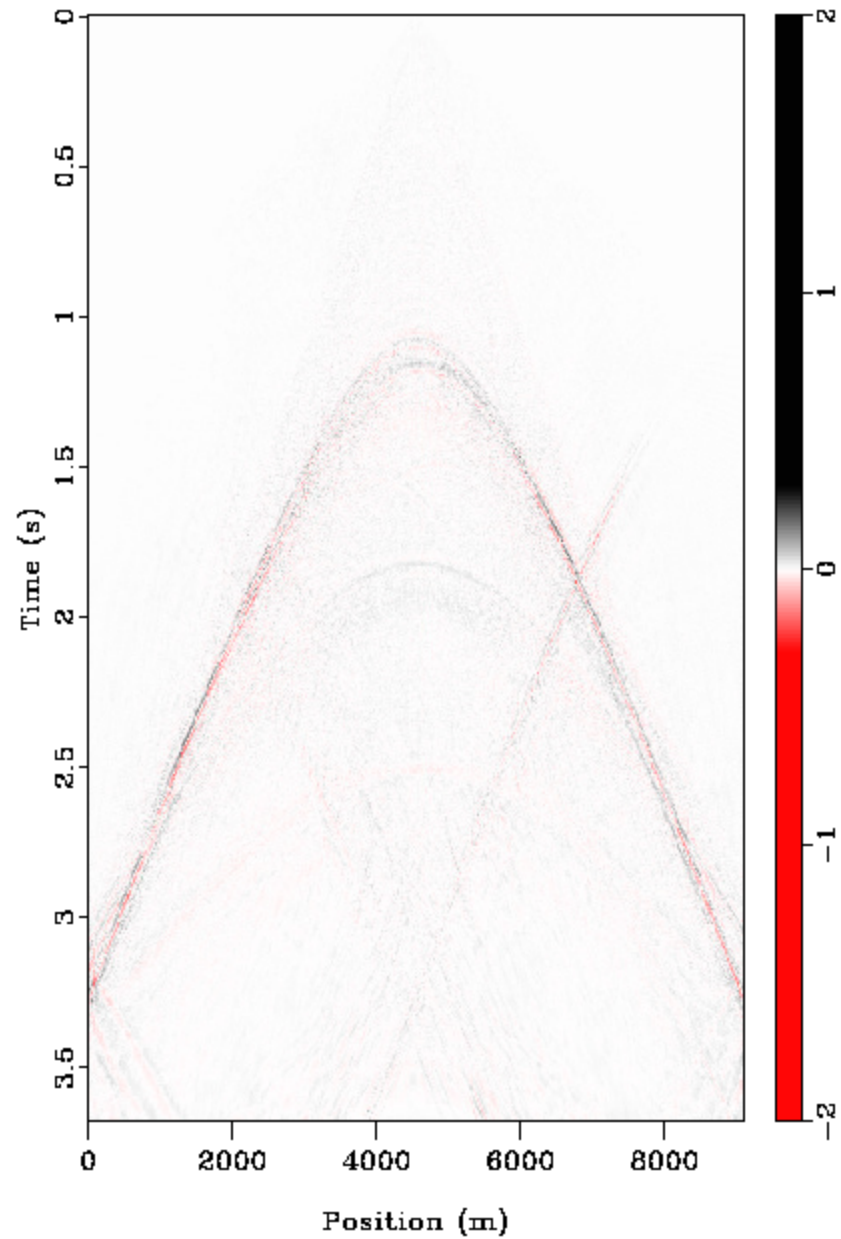
c) Deblended (CMP)



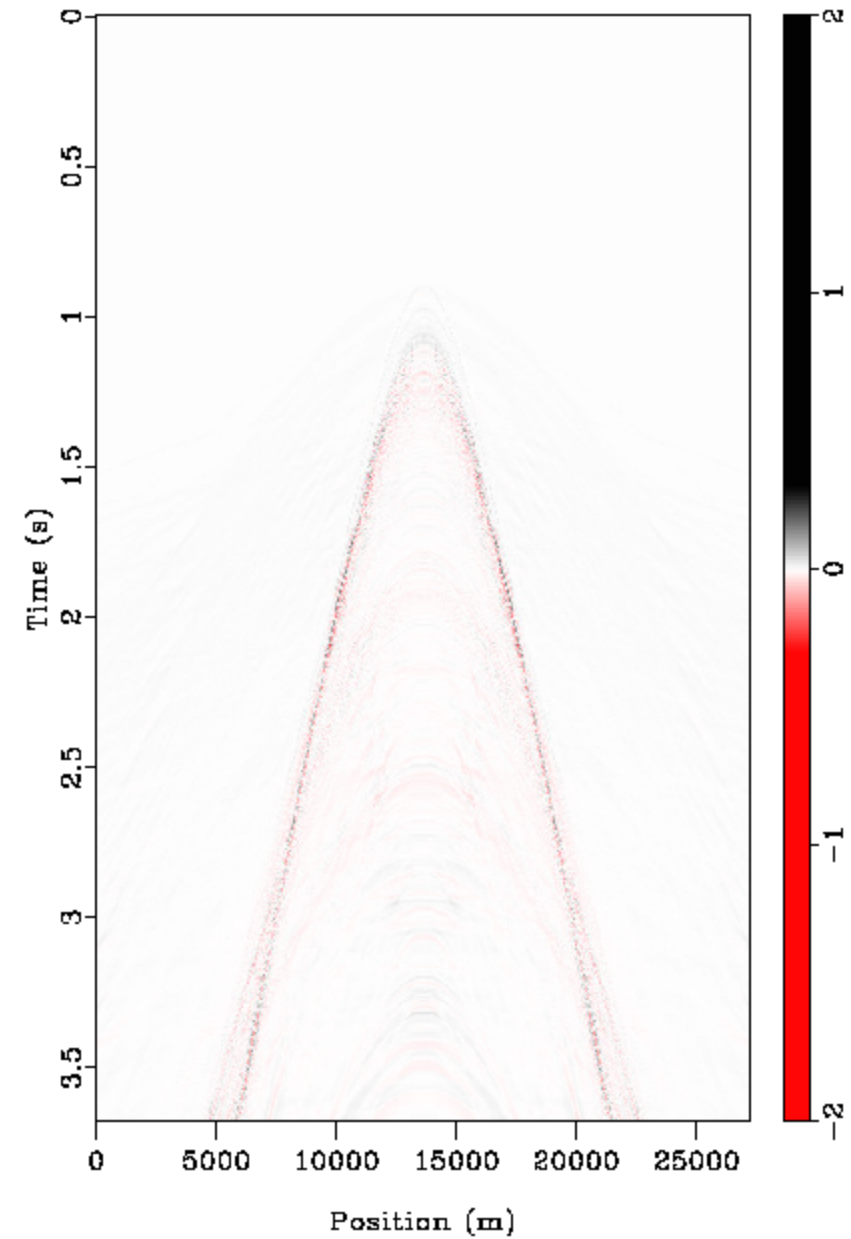




d) Difference (CSG)

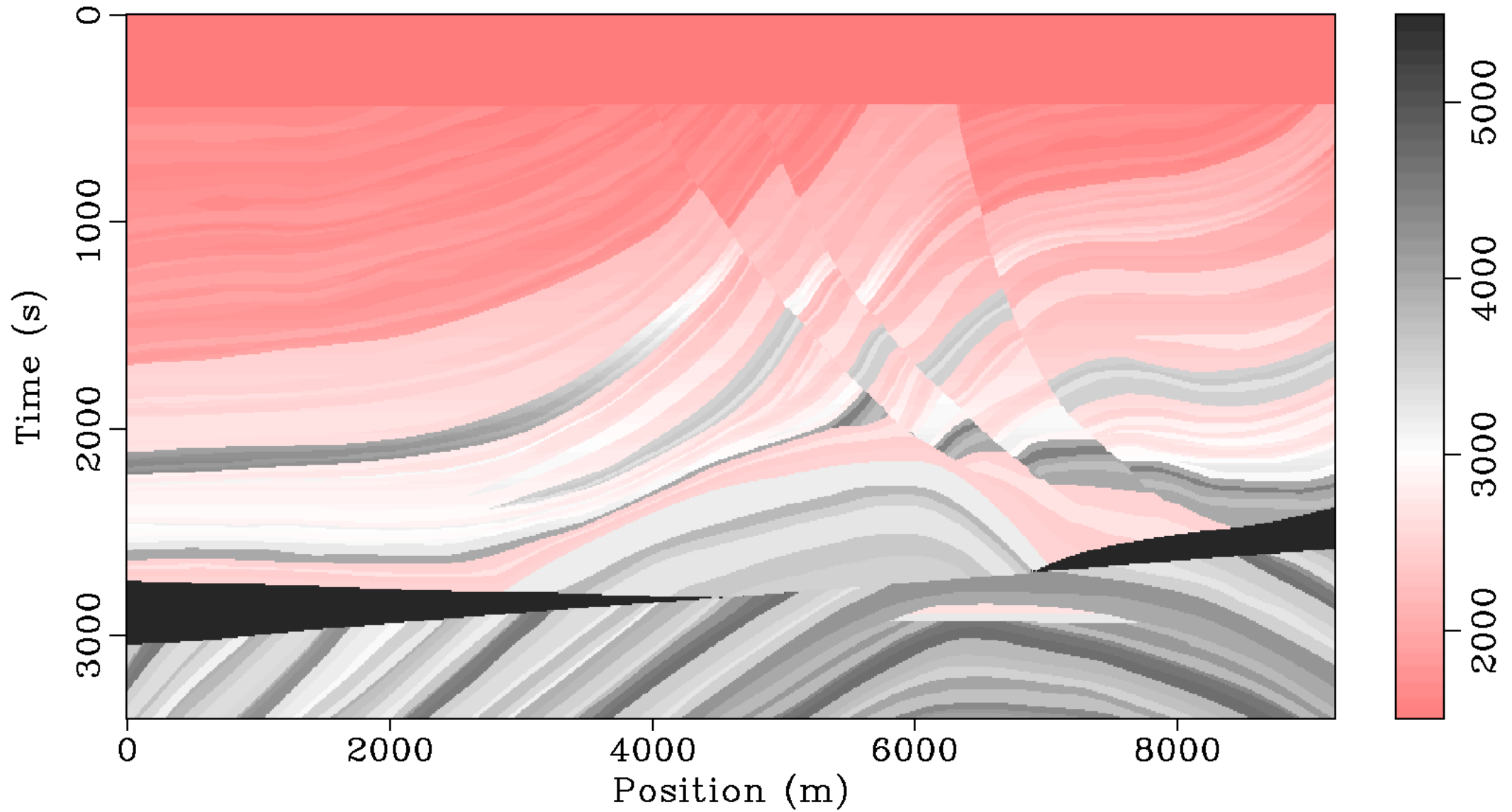


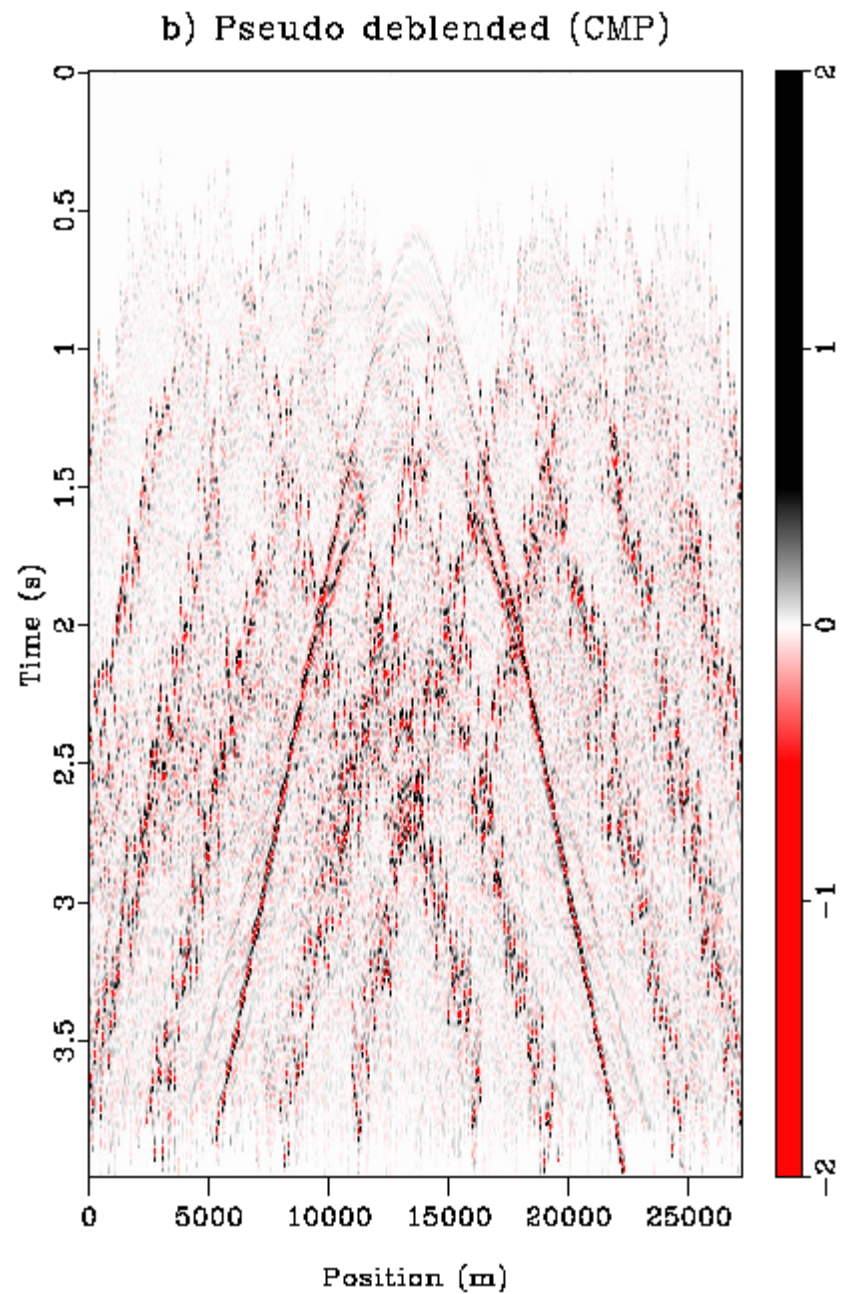
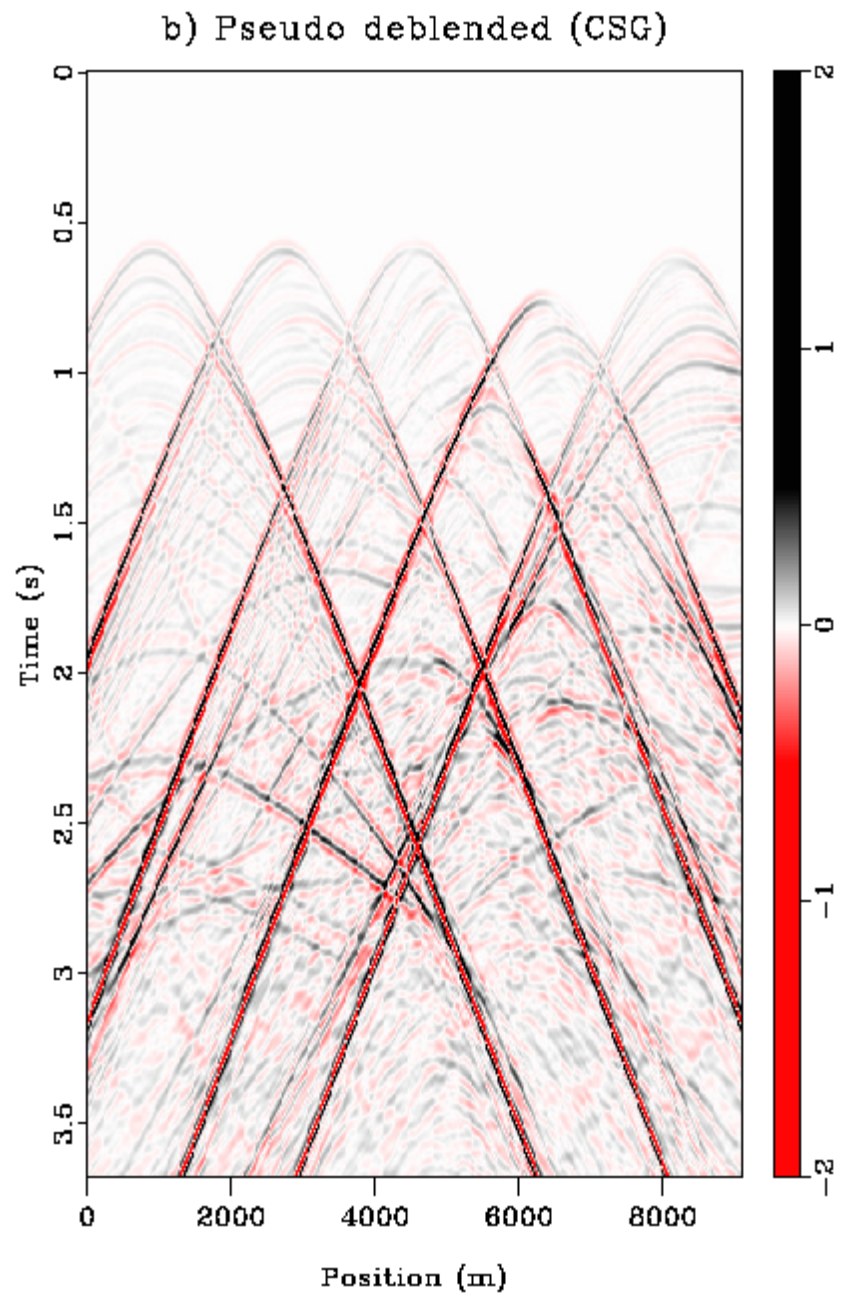
d) Difference (CMP)





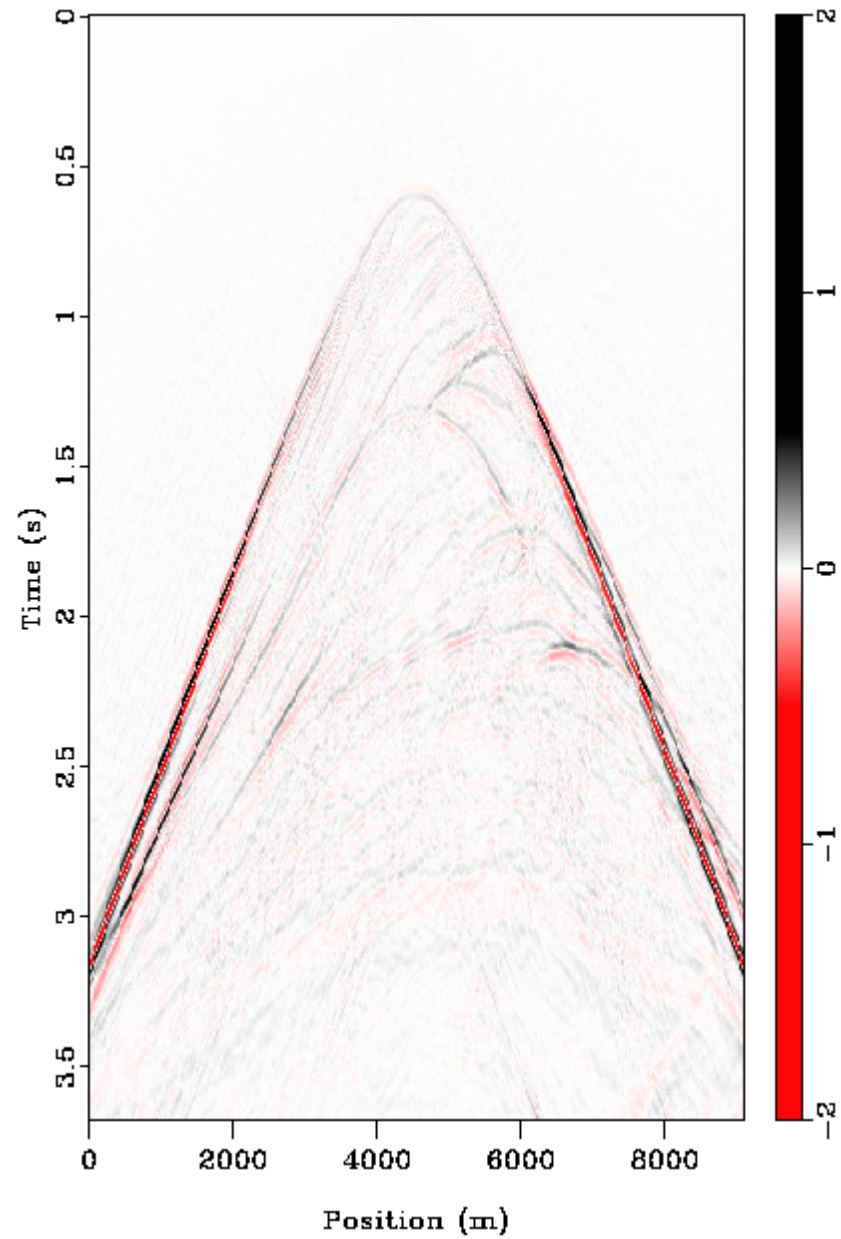
MarmousiExtended



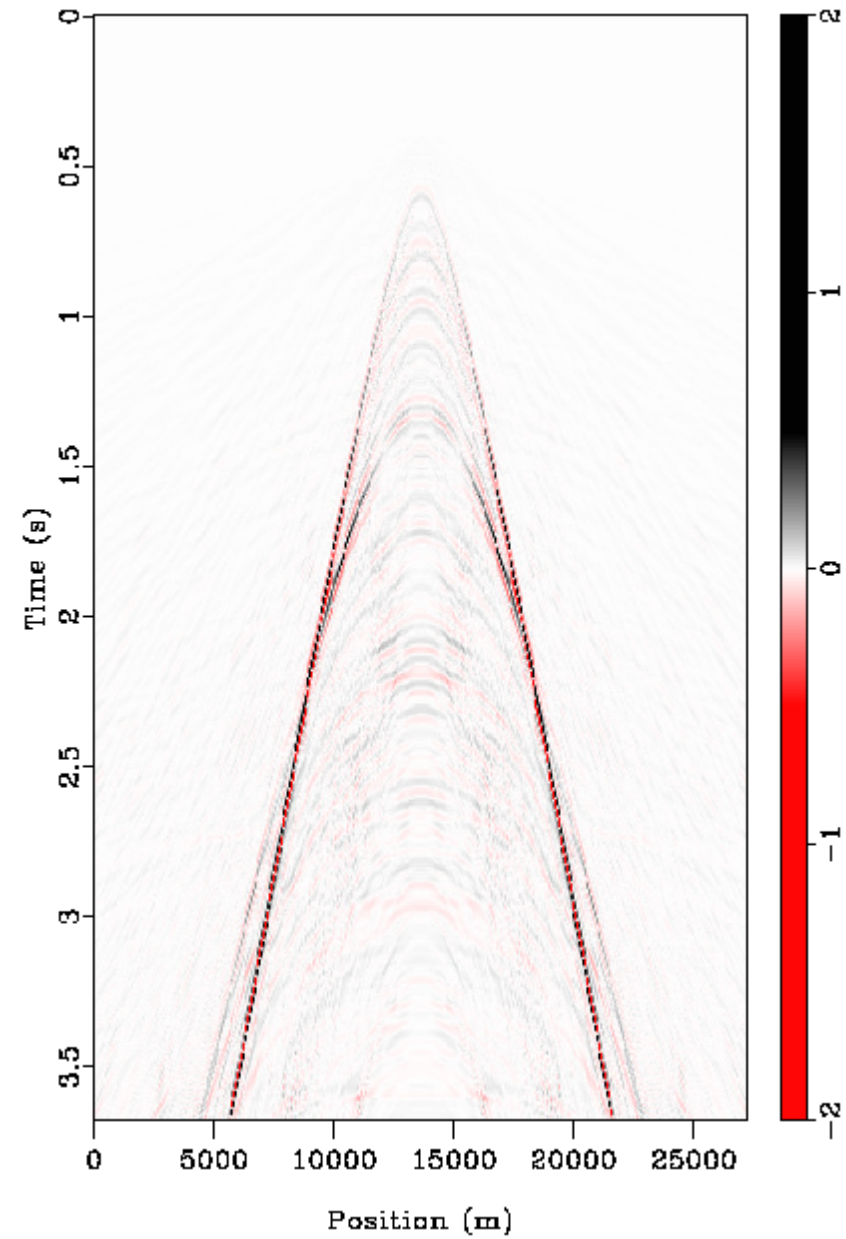




c) Deblended (CSG)

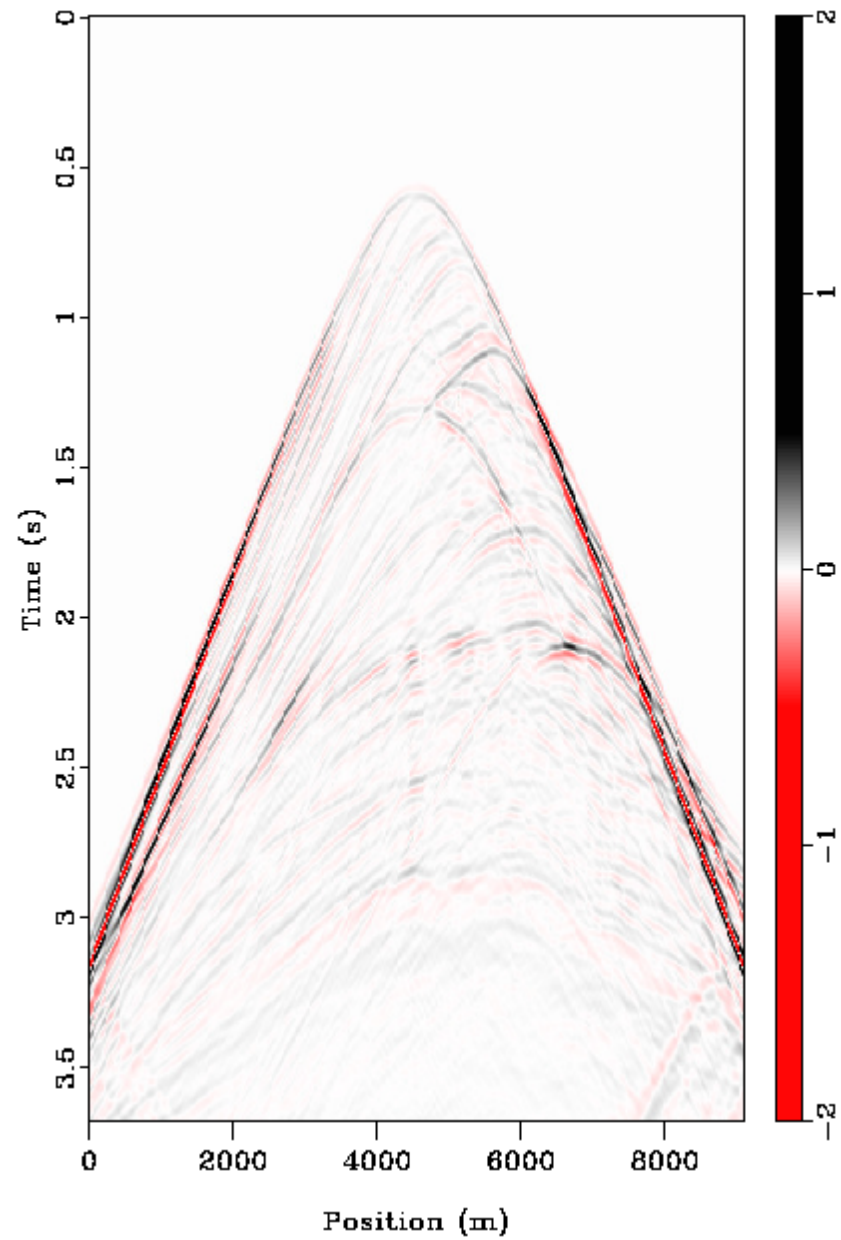


c) Deblended (CMP)

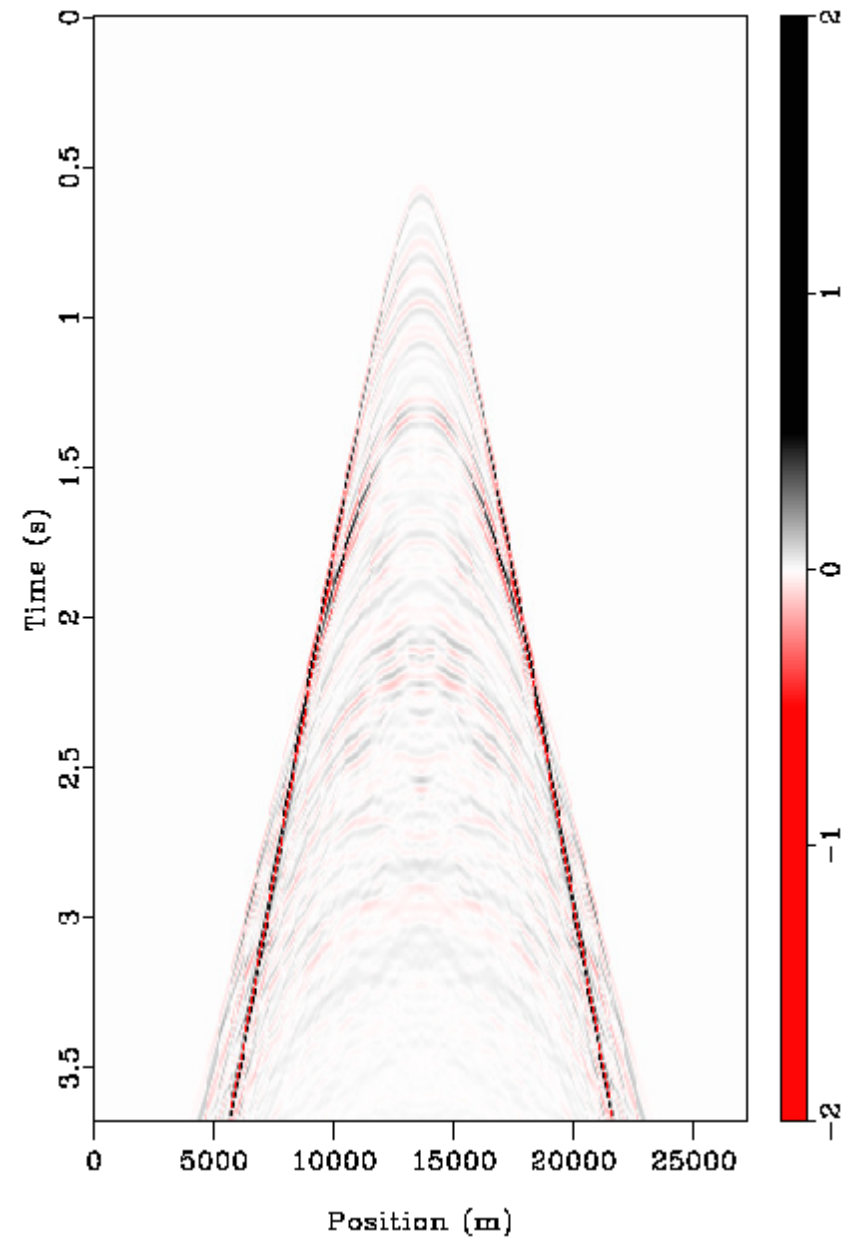




a) Original (CSG)

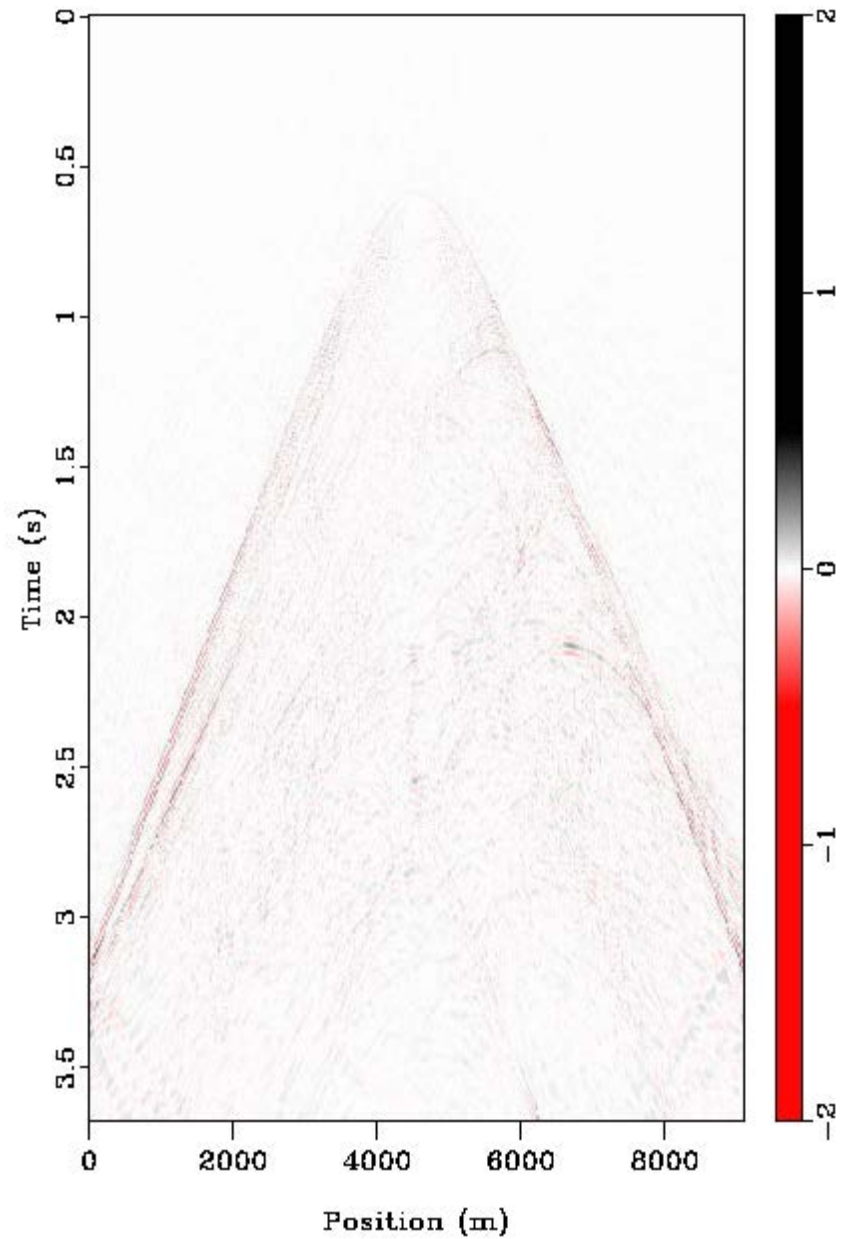


a) Original (CMP)

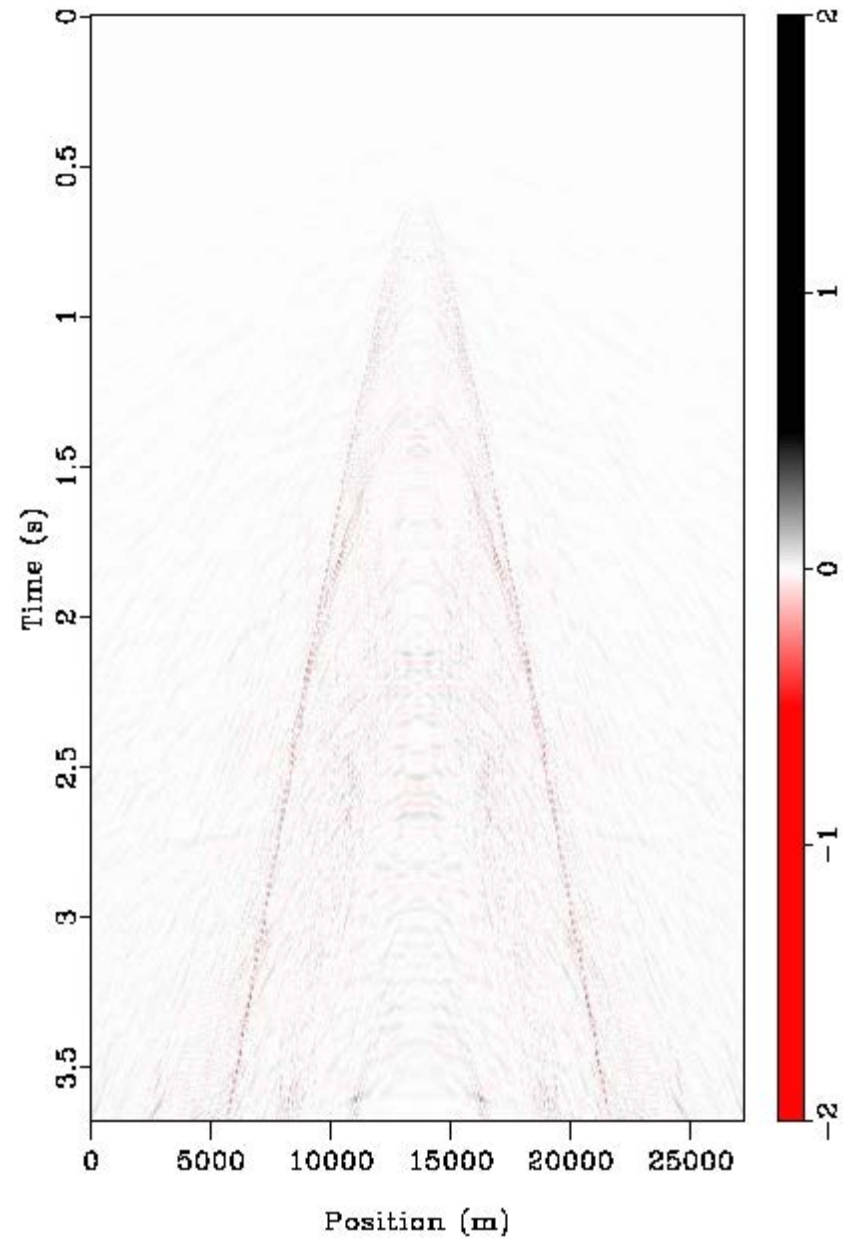




d) Difference (CSG)

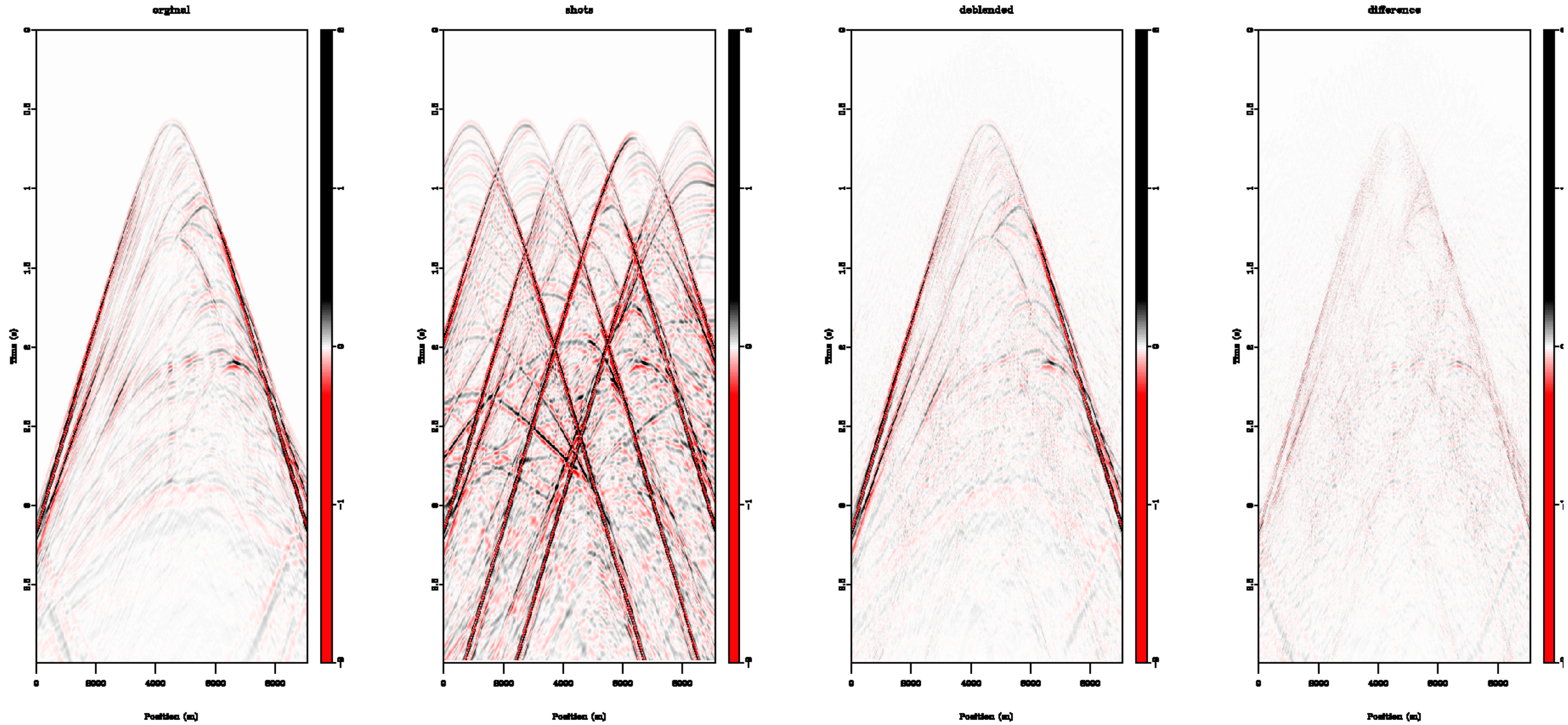


d) Difference (CMP)



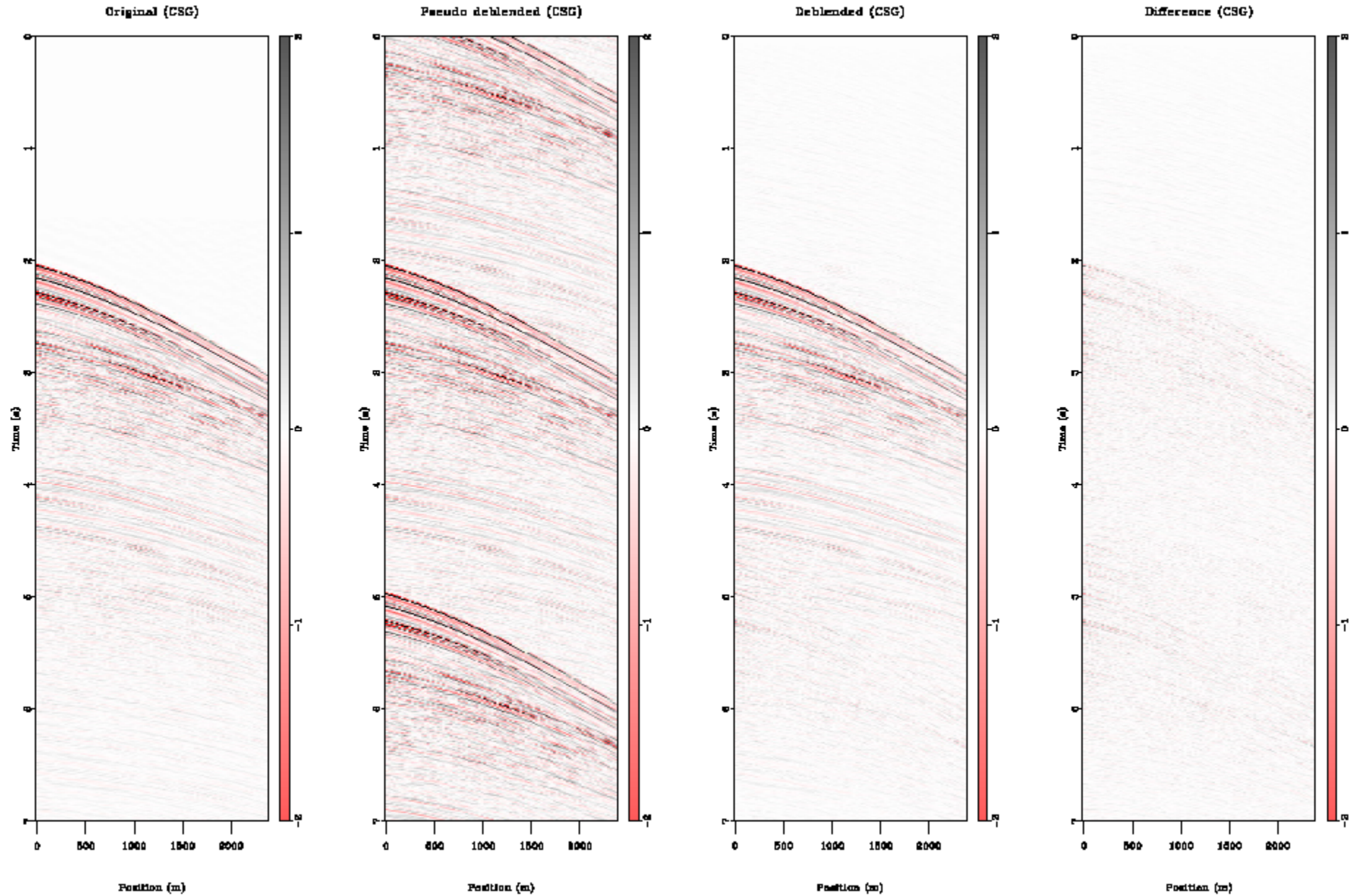


Results - Marmousi

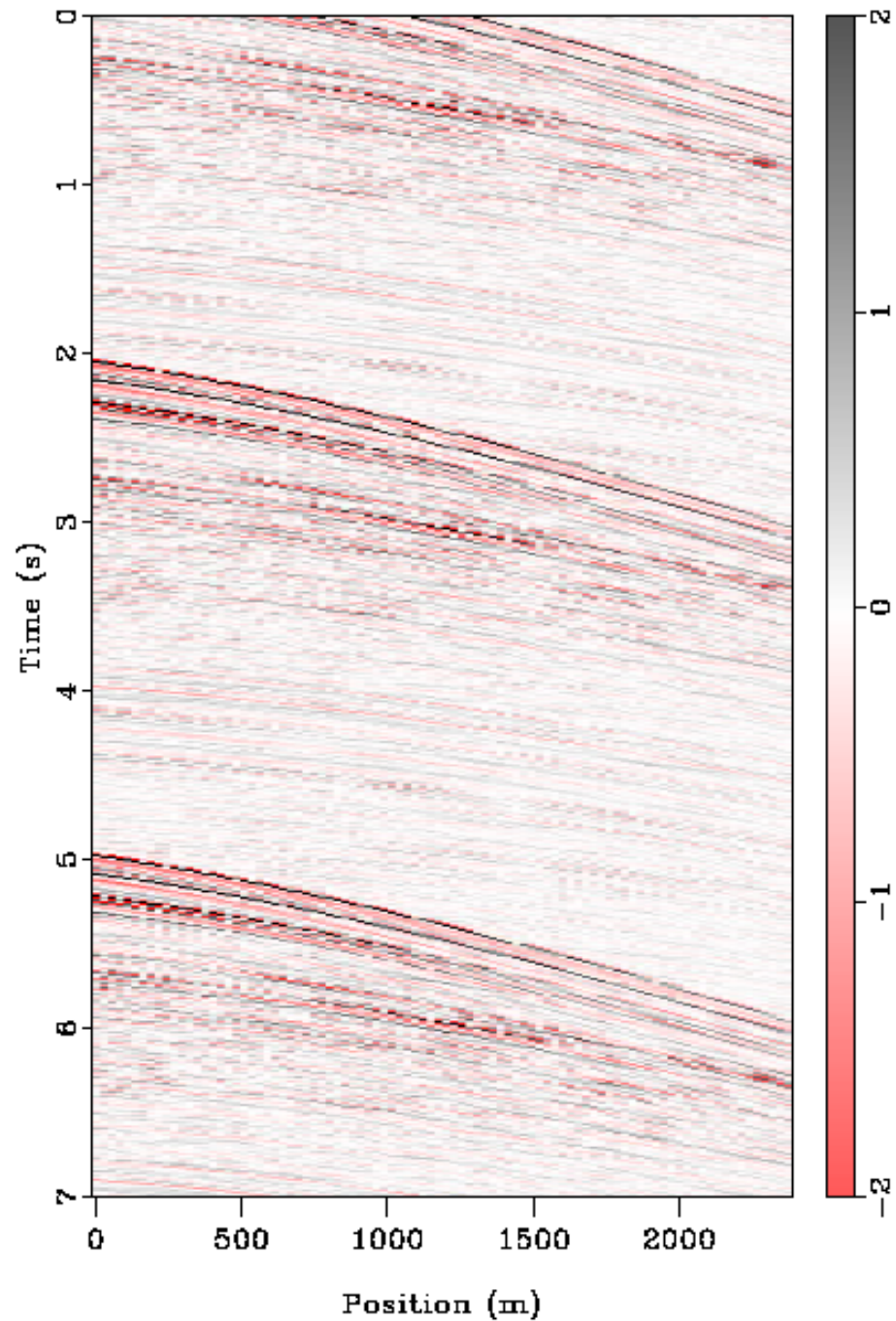




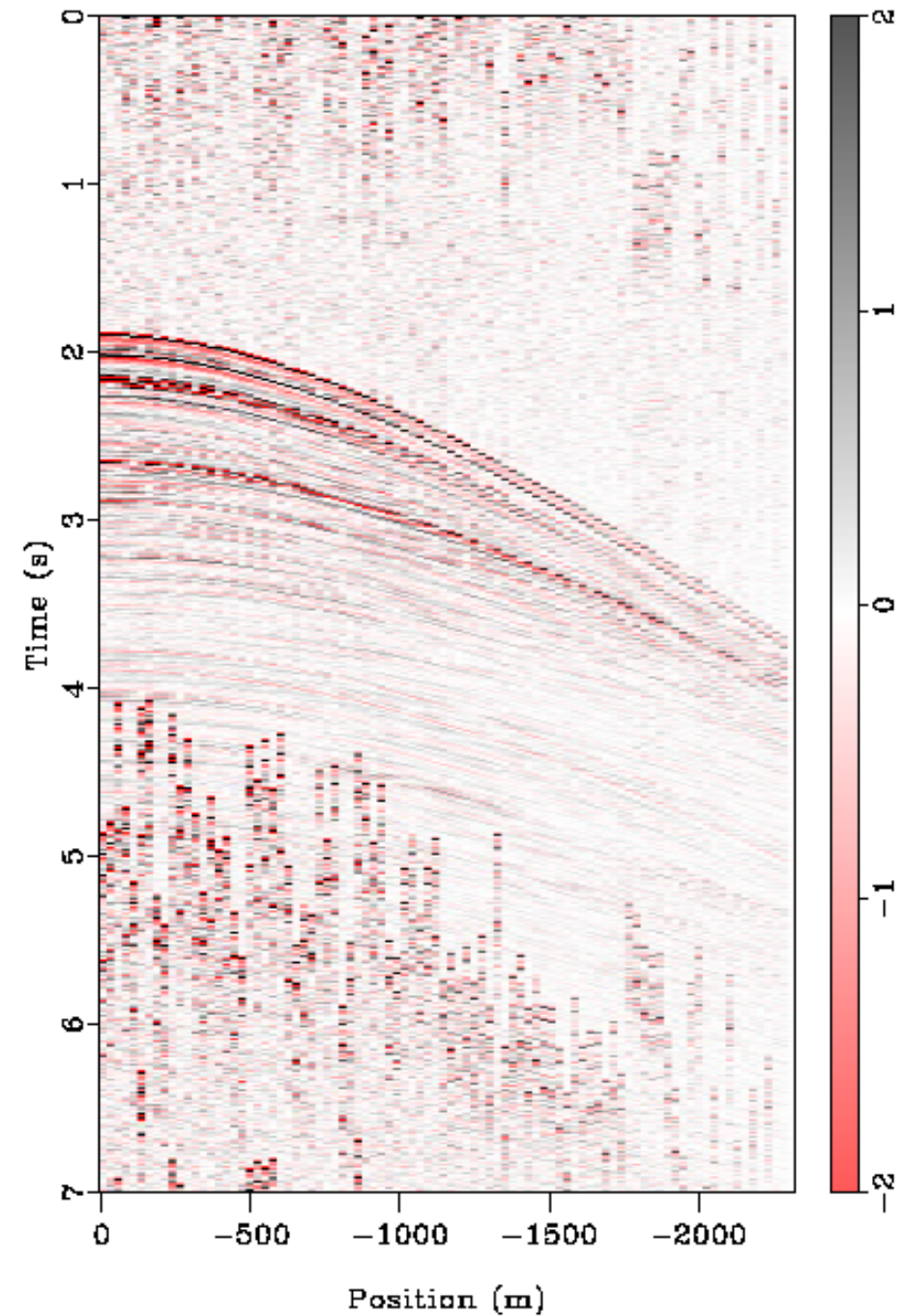
Gulf of Mexico Dataset



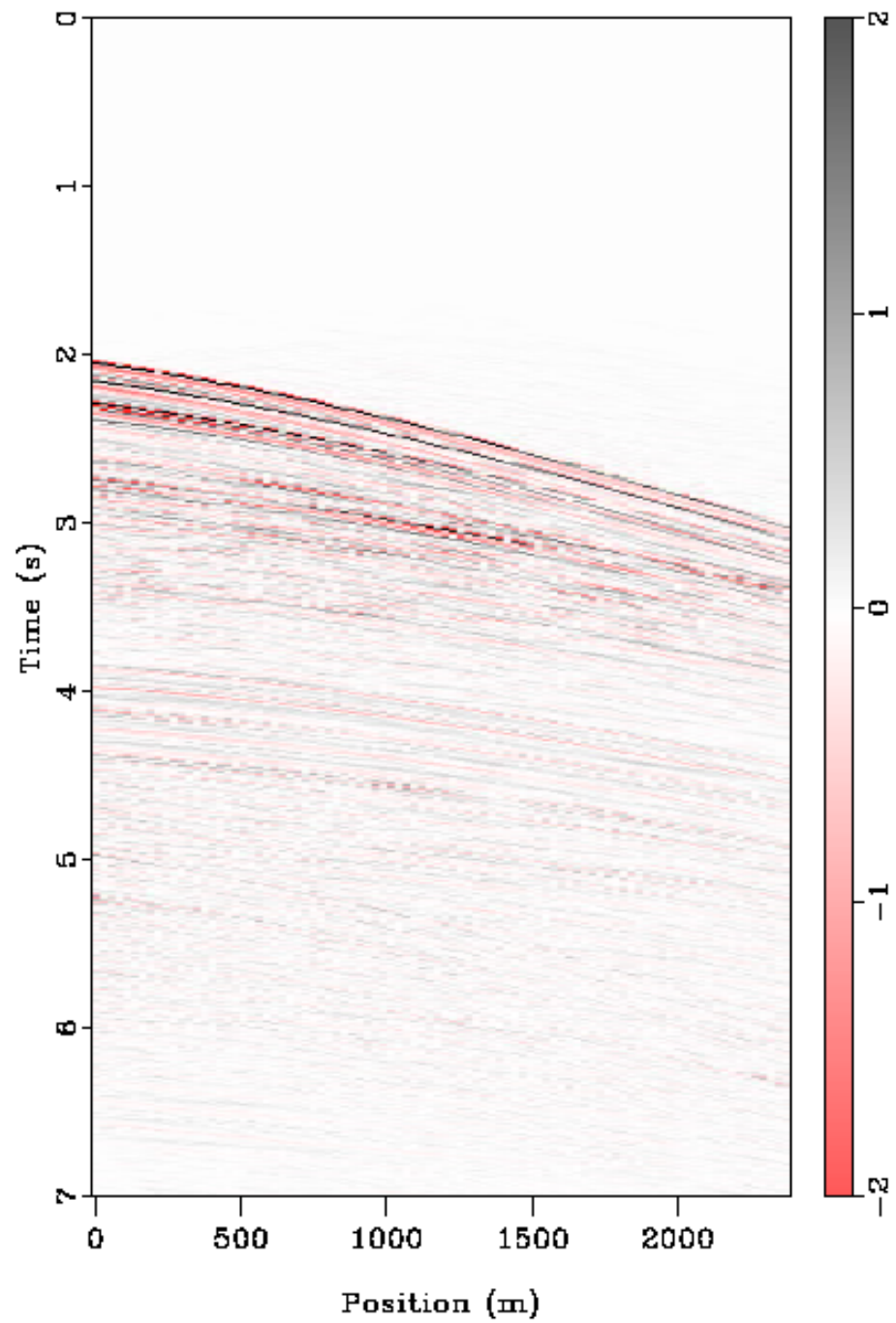
a) Pseudo deblended (CSG)



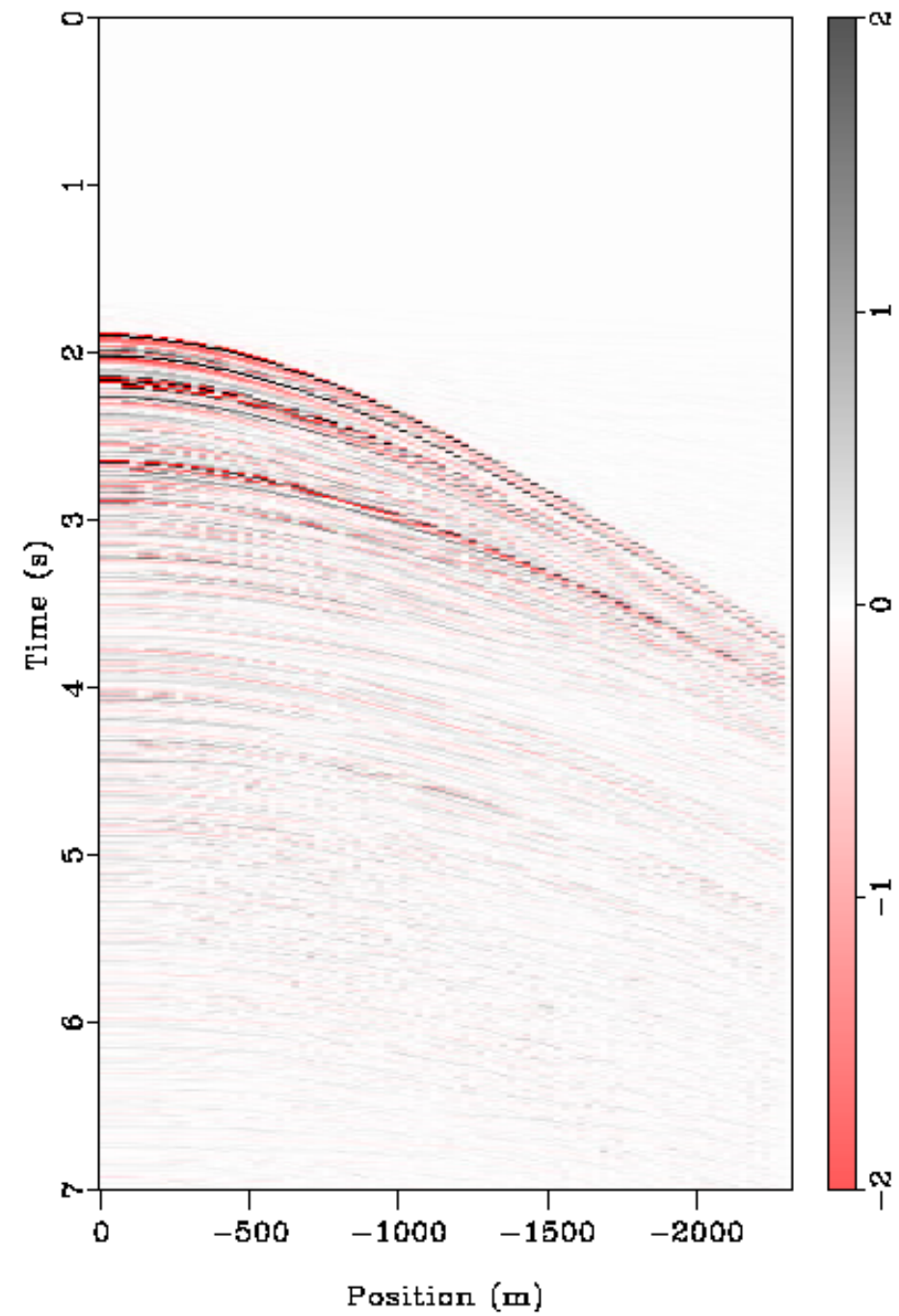
a) Pseudo deblended (CMP)



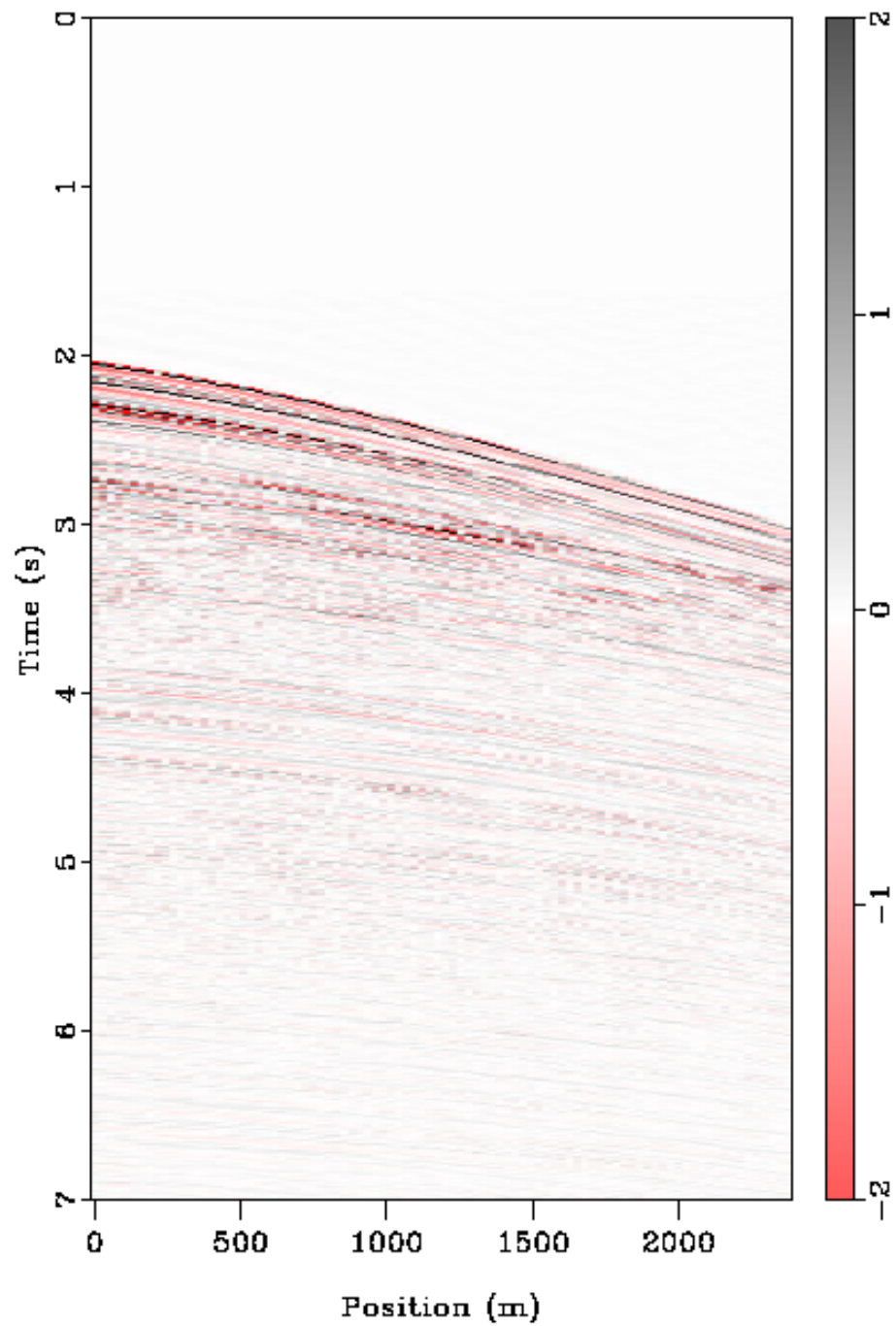
b) Deblended (CSG)



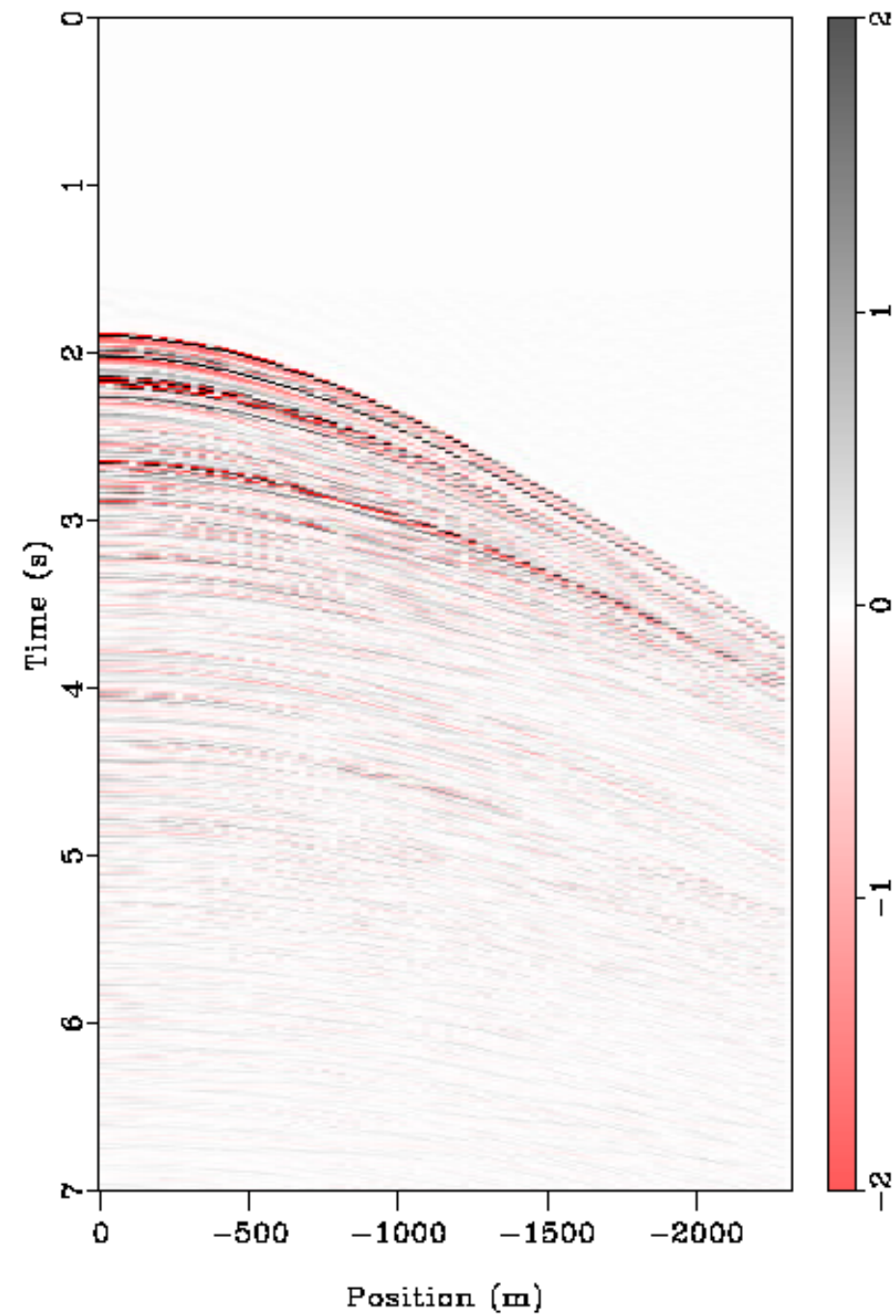
b) Deblended (CMP)



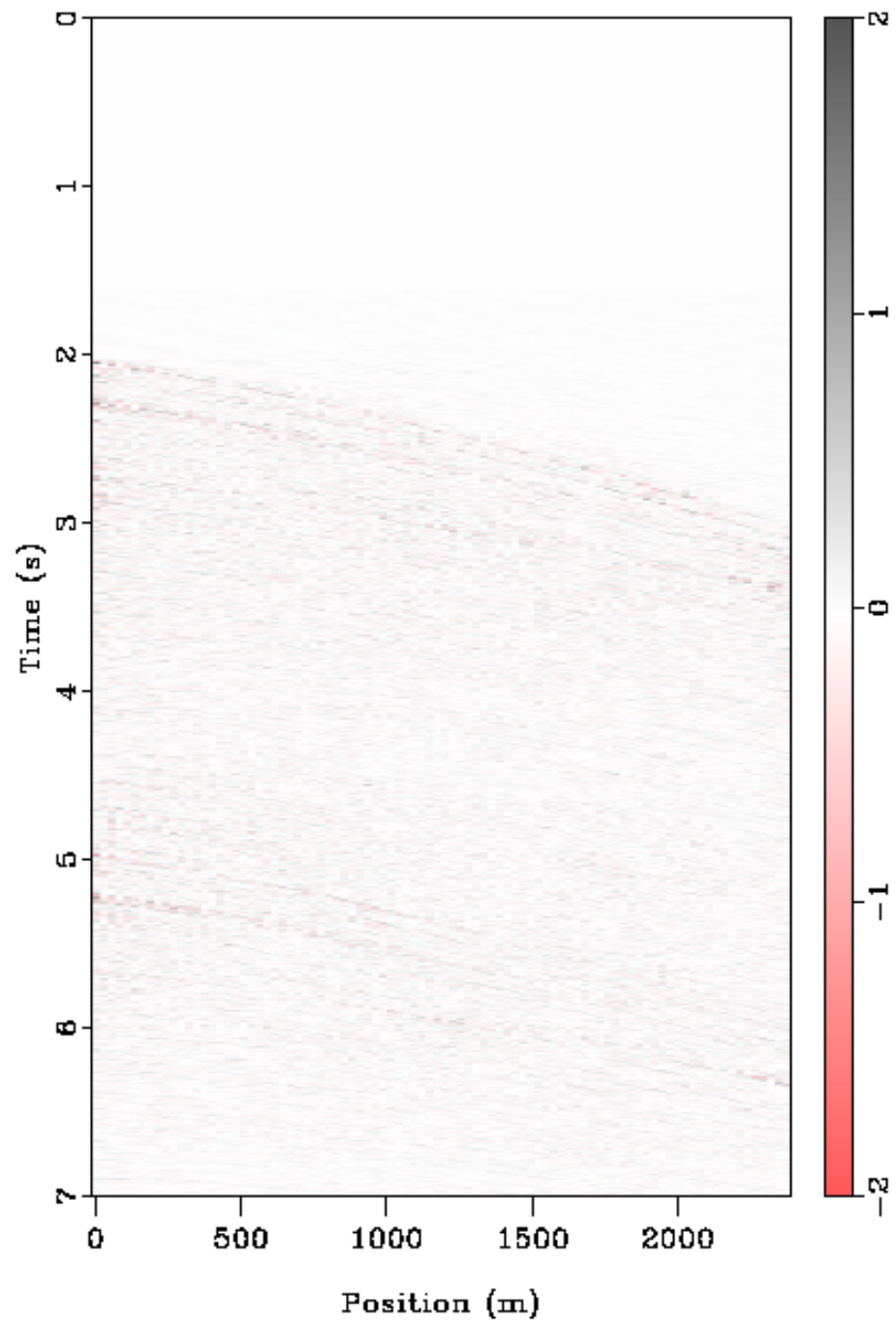
Original (CSG)



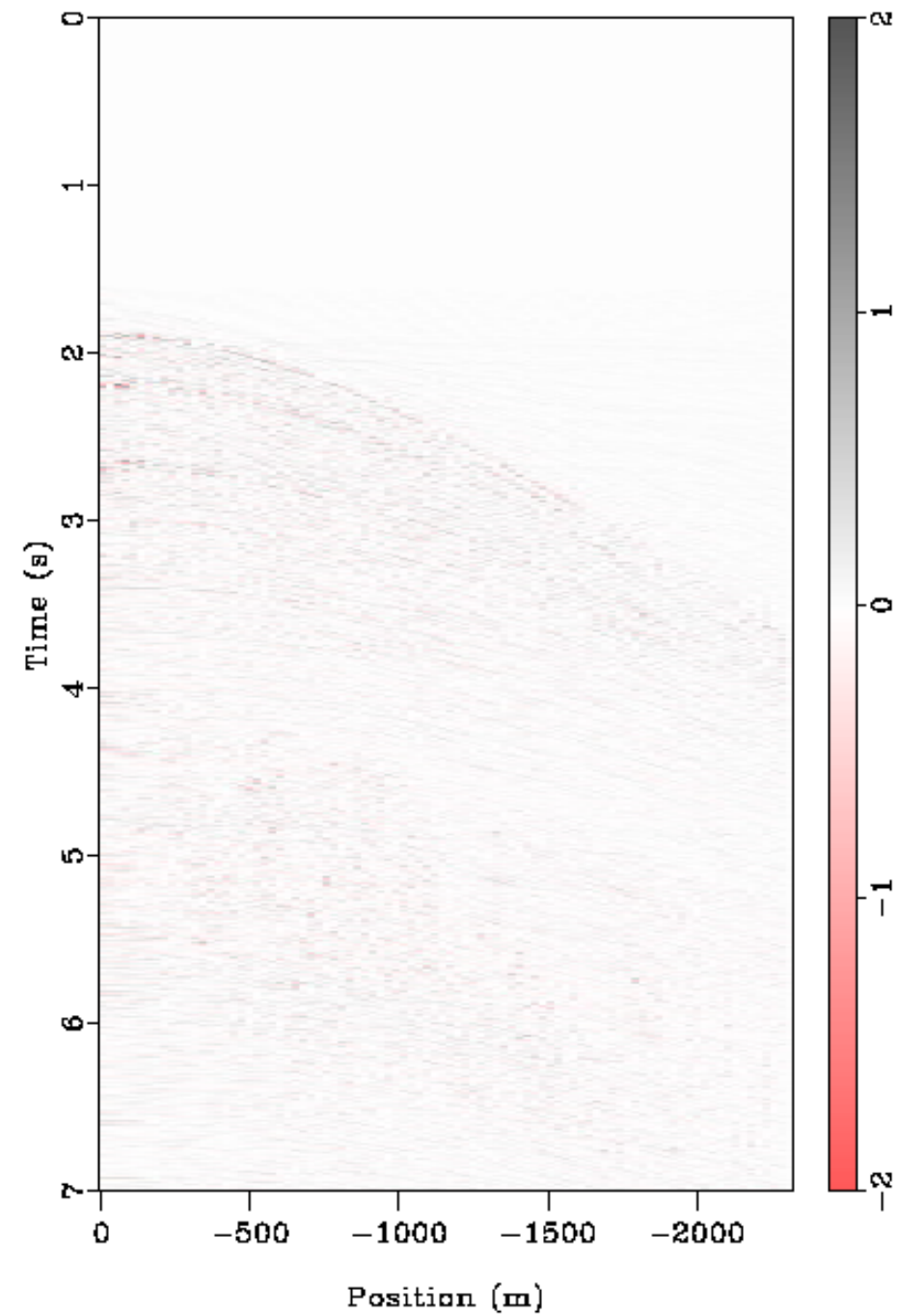
Original (CMP)



c) Difference (CSG)



c) Difference (CMP)





Extend Radon deblending to 3D applications

First need to find best high efficiency operator outlined below

Hybrid Radon transform

Using a hybrid linear-hyperbolic radon to map ground roll and direct arrivals as well as reflections for separation

Local windowing using linear radon

To deal with amplitude issues with diffractions using local instead of global helps preserve low amplitude events



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